

Sheinman, Sharma, and MacKintosh Reply: The authors of the preceding Comment [1] raise an interesting question about ambiguities in defining the Fisher exponent τ . Ordinarily, such critical exponents are determined by the behavior in the thermodynamic limit. In the percolation theory context the number of connected clusters with mass s scales as [2,3]

$$n_s \propto s^{-\tau} \quad (1)$$

in the infinite size limit, $M \rightarrow \infty$, up to possible logarithmic corrections. To estimate the value of τ numerically, however, one must consider systems with finite M , together with an appropriate finite-size scaling consistent with Eq. (1) as $M \rightarrow \infty$. As in the Comment [1], one approach often used in the percolation literature [3] is

$$n_s = Ms^{-\tau} f\left(\frac{s}{M^{d_f/d}}\right), \quad (2)$$

where d is the dimensionality ($d = 2$ here) and d_f is the fractal dimension of the clusters. The function $f(s/M^{d_f/d})$ is constrained to have no power-law dependence in the regime $1 \ll s \ll M$ and has to vanish for $s > M$. In random percolation (RP) $d_f < 2$ and $\tau = d/d_f + 1 > 2$ [3]. Demanding conservation,

$$\int_1^\infty sn_s ds = M, \quad (3)$$

means that Eq. (2) is consistent with (1) only for $\tau \geq 2$. Thus, the approach in the Comment [1] presupposes that

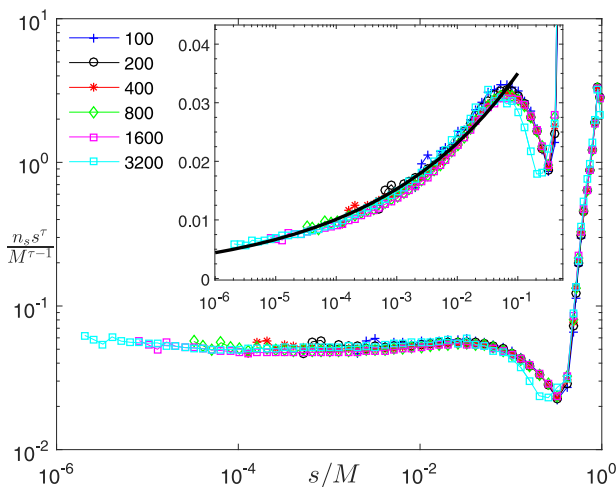


FIG. 1. Collapse attempts of the cluster masses distribution of the NEP model [4] at $p = p_c$ using $\tau = 1.82 < 2$ (main figure) with definition (4) and $\tau = 2$ with equivalent (for this value of τ) definitions (2) and (4) (inset) for different system sizes (see the values of \sqrt{M} in the legend). The line in the inset corresponds to the power law with $0.18 = 2 - 1.82$ exponent.

$\tau \geq 2$ and is incapable of identifying possible values of $\tau < 2$.

For this reason, in addition to the standard RP ansatz, we also used an ansatz consistent with Eq. (1), while allowing for possible $\tau < 2$:

$$n_s = M^{\tau-1} s^{-\tau} f\left(\frac{s}{M}\right). \quad (4)$$

This is consistent with Eq. (1), while satisfying Eq. (3) for $\tau < 2$. In general, with no information about τ being larger or smaller than 2, one should analyze the numerical data for both cases. We do this in Fig. 1, e.g., by plotting $s^\tau n_s / M^{\tau-1}$ vs s/M for the case $\tau < 2$. We find good collapse and near constancy of $s^\tau n_s / M^{\tau-1}$ for $\tau = 1.82$ and over a wide range of s/M up to ~ 0.1 . By contrast, attempting the same collapse for $\tau = 2$, where both our ansatz and that of the Comment [1] are equivalent, we do not find the expected near constancy of $s^2 n_s / M$. Thus, while it may not be possible to entirely rule out $\tau = 2$ with significant logarithmic corrections, our results appear to be more consistent with $\tau = 1.82$. In the inset, however, we have plotted the distribution log-linear, in a way closely analogous to the Comment [1]. Here, we do not find evidence of a logarithmic dependence. Our data are, in fact, consistent with a weak exponent 0.18, as indicated by the thick line.

We thank the authors of the Comment [1] for their interest and the useful discussion of subtleties in interpreting the numerical data. But, we fundamentally disagree with their approach that tacitly assumes $\tau \geq 2$.

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