Lens-based fluorescence nanoscopy

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Abstract. The majority of studies of the living cell rely on capturing images using fluorescence microscopy. Unfortunately, for centuries, diffraction of light was limiting the spatial resolution in the optical microscope: structural and molecular details much finer than about half the wavelength of visible light (~200 nm) could not be visualized, imposing significant limitations on this otherwise so promising method. The surpassing of this resolution limit in far-field microscopy is currently one of the most momentous developments for studying the living cell, as the move from microscopy to super-resolution microscopy or 'nanoscopy' offers opportunities to study problems in biophysical and biomedical research at a new level of detail. This review describes the principles and modalities of present fluorescence nanoscopes, as well as their potential for biophysical and cellular experiments. All the existing nanoscopy variants separate neighboring features by transiently preparing their fluorescent molecules in states of different emission characteristics in order to make the features discernible. Usually these are fluorescent 'on' and off states causing the adjacent molecules to emit sequentially in time. Each of the variants can in principle reach molecular spatial resolution and has its own advantages and disadvantages. Some require specific transitions and states that can be found only in certain fluorophore subfamilies, such as photoswitchable fluorophores, while other variants can be realized with standard fluorescent labels. Similar to conventional far-field microscopy, nanoscopy can be utilized for dynamical, multi-color and three-dimensional imaging of fixed and live cells, tissues or organisms. Lens-based fluorescence nanoscopy is poised for a high impact on future developments in the life sciences, with the potential to help solve long-standing quests in different areas of scientific research.

1. Introduction: from far-field light microscopy to nanoscopy 179

- 1.1. The diffraction limit 181
- 1.2. Pushing the limits of the diffraction barrier 183
- 1.3. Breaking the diffraction barrier 184

2. The coordinate-targeted approach 186

- 2.1. STED nanoscopy 187
 - 2.1.1. Multicolor STED nanoscopy 188
 - 2.1.2. 3D STED nanoscopy 190
 - 2.1.3. Photo-physical and -chemical considerations in STED nanoscopy 191
 - 2.1.4. Cluster analysis in STED nanoscopy 194

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- 2.1.5. Live-cell and in-vivo STED nanoscopy 198
- 2.1.6. Lasers for STED 199
- 2.1.7. Gated CW-STED nanoscopy 201
- 2.1.8. STED-FCS: nanoscale single-molecule dynamics 203
- 2.1.9. STED-FCS: live-cell membrane dynamics 205
- 2.2. Generalization: STED, GSD, SSIM/SPEM and RESOLFT 208
 - 2.2.1. STED: stimulated emission 208
 - 2.2.2. GSD: transient dark state shelving 208
 - 2.2.3. SPEM/SSIM: GSD via saturated excitation 212
 - 2.2.4. RESOLFT: reversible photoswitchable labels 212
 - 2.2.5. Parallelization 213
 - 2.2.6. Nanoscale writing 214
- 2.3. Ultimate limit 214

3. The coordinate-stochastic approach 215

- 3.1. Basics: (F)PALM/STORM 215
- 3.2. Molecular transitions 216
- 3.3. Continuous recording 218
- 3.4. SOFI 220
- 3.5. General aspects 220
- 3.6. 3D imaging 222
- 3.7. Dynamics 223
- 3.8. Multi-colour recordings 223
- 4. Conclusions: coordinate-targeted versus -stochastic 224
- 5. Acknowledgements 226
- 6. References 227

1. Introduction: from far-field light microscopy to nanoscopy

Biophysical studies strongly rely on microscopy, since it can directly deliver images of the distributions of specific molecules in the living cell. Among all the different microscopes, optical fluorescence microscopes have been established as key instruments in the life sciences. This stems from the fact that the use of light allows least-invasive access to the interior of living cells and organisms and, when combined with fluorescence readout, offers the specific and highly sensitive detection of cellular constituents. To keep these advantages, optical microscopy of the living cell is usually applied in the far-field: a lens-based system allows the excitation and detection of fluorescent molecules micrometers to millimeters away from any optical element, preserving the non-invasiveness and the ability to image deep inside living cells or tissue. However, the concomitant focusing of light introduces the most prominent limit of this technique: due to the diffraction of light, details far below the wavelength of light λ , i.e. in the range of below 200–300 nm, cannot be directly resolved in an image and remain hidden to the observer (Abbe, 1873). This diffraction barrier has major implications for biophysical studies of the cell, since a complete understanding of cellular structure and function requires observations at the molecular level, i.e. with molecular-scale resolution. Until not very long ago, obtaining a spatial resolution on the nanometer scale with a far-field fluorescence microscope was considered impossible (Alberts et al. 2002).

Several ideas had been put forward to improve the resolution, including special illumination patterns and mathematical approaches (Bertero *et al.* 1990; Toraldo di Francia, 1952). One of them is structured illumination microscopy (SIM) (Ash & Nicholls, 1972; Bailey *et al.* 1993; Frohn *et al.* 2000; Gustafsson, 2000; Gustafsson *et al.* 2008; Lukosz, 1966; Schermelleh *et al.* 2008). SIM allows (three-dimensional (3D) live-cell) imaging with a two-fold increase in spatial resolution over the conventional diffraction limit, i.e. ~100 nm. Similarly, 4-Pi or I⁵M microscopy significantly improve the axial resolution of far-field microscopy (Gustafsson *et al.* 1995, 1996, 1999; Hell, 1992; Hell *et al.* 1994; Hell & Stelzer, 1992). Unfortunately, these techniques are rather complex with respect to both instrumentation and image processing, and they do not break the diffraction barrier, because they are still limited by diffraction; they only push diffraction to its very limits.

It was not until the early 1990s that viable concepts emerged to truly break the physical barrier given by diffraction. It was realized that this could be achieved using basic molecular transitions (Hell, 1994; Hell & Kroug, 1995; Hell & Wichmann, 1994). By exploiting a transition between states of different emission properties of the fluorescent molecules, such as between a dark and a bright state, it would become possible to control the fluorescence emission in such a way that adjacent molecules emit sequentially in time (Hell, 2004; Hell et al. 2003). This has led to far-field imaging of fluorescently tagged objects with unprecedented spatial resolving power and heralded the move from microscopy to 'super-resolution' microscopy or 'nanoscopy'. For further reviews see, for example, (Bates et al. 2008; Chi, 2009; Clausen et al. 2013; Dedecker et al. 2008; Dempsey et al. 2011; Eggeling et al. 2013; Evanko, 2009; Fernandez-Suarez & Ting, 2008; Heilemann et al. 2009a; Heintzmann & Ficz, 2007; Heintzmann & Gustafsson, 2009; Hell, 2003, 2007, 2009a, b; Hell et al. 2004; Huang, 2010; Huang et al. 2009, 2010; Lippincott-Schwartz & Manley, 2009; Moerner, 2006; Muller et al. 2012; Patterson et al. 2010; Rice, 2007; Tinnefeld et al. 2015). Two major concepts have evolved so far: (1) the coordinate-targeted approach, as realized in a stimulated emission depletion (STED) (Hell & Wichmann, 1994), ground state depletion (GSD) (Hell & Kroug, 1995) or reversible saturable/switchable optical linear (fluorescence) transition (RESOLFT) (Hell, 2003, 2004; Hell et al. 2003) nanoscope, reversibly inhibits the occupation of a molecular state (such as the bright, emissive state) everywhere but at specific points in space such that a detected signal (such as the spontaneous fluorescence) is only allowed in coordinate regions of sub-diffraction size. Scanning of these points realizes a super-resolved image. (2) The coordinate-stochastic approach such as realized in fluorescence photoactivated localization microcopy ((F)PALM) (Betzig et al. 2006; Hess et al. 2006) or stochastic optical reconstruction microscopy (STORM) (Rust et al. 2006) inhibits the population of a molecular state (the bright, emissive state) everywhere but from single molecules per region of diffraction (i.e. the spatial extent in which the diffraction limit applies), whose spatial position can then be determined with sub-diffraction precision. Subsequent stochastic state transitions of all (individual) molecules and the determination of their positions allow the reconstruction of a superresolved image.

In this review we will describe the fundamentals of far-field microscopy and its diffraction barrier, outline the details of breaking this barrier using different fluorophore transitions and detail the basics and different modalities of the current far-field nanoscopes. We will however not review every work in this field. By outlining the basic concepts of the various superresolution microscopy or nanoscopy approaches, we rather aim at presenting the prospects and any current limitations of these nanoscopes for their use in biophysical and biomedical studies.

1.1 The diffraction limit

Far-field fluorescence microscopy (or far-field optical light microscopy in general) employs focused light. A lens system (the objective lens) is used to excite and collect fluorescence in the sample and to image it onto a photon detector. This is usually realized in a wide-field mode, where a large area is excited at once and imaged onto a camera, or in a point-scanning approach (e.g. the confocal microscope), where only a small spot (volume) is excited, its fluorescence detected by a point detector, and the final image formed by scanning the spot over the sample (Fig. 1*a*, *b*). The lens causes the focused propagating light to interfere constructively at a certain point in space, called the focal point. Diffraction, however, results in a light intensity pattern which features a central maximum and a width whose full-width-at-half-maximum (FWHM) is $d \approx \lambda/(2n \sin \alpha)$ along the lateral and $\Delta z \approx \lambda/(n \sin^2 \alpha)$ along the optic axis, governed by the wavelength λ of the light and the focusing strength of the lens (given by its semi-aperture angle α and the refractive index *n* of the object medium, $NA = n \sin \alpha$ is referred to as the numerical aperture of the objective lens) (Born & Wolf, 2002). This finite-width point-spread-function (PSF) of the lens rules both the fluorescence excitation and collection process, and for both the wide-field and single-point scanning variant precludes the discerning of simultaneously emitting molecules which lie within this PSF. For visible light ($\lambda \approx 500$ nm) structural details below approximately 200 nm thus appear blurred and indiscernible in the final image (Box in Fig. 1).

Several strategies have been thought of to push this resolution barrier. A straightforward way is to reduce the wavelength λ of the light. Ultraviolet (UV) light is however known to introduce photostress on the sample, stronger photobleaching of the fluorescent molecules under study, significant autofluorescence (especially in the cellular environment), and a demand for UV-specific optics, thus making it rather impractical for live-cell studies. An increase of the numerical aperture is ultimately limited by the technical feasibilities of manufacturing objective lenses, currently delivering maximum NA in the range of 1.4–1.5.

A logical consequence of the limits brought about by using focused light was to give up the use of the far-field objective lenses and confine the light by means of a sub-diffraction-sized aperture or tip (Ash & Nicholls, 1972; Synge, 1928). The light evolves out of the tip as an evanescent field, meaning that it fades out exponentially within a distance of $\sim \lambda/2$. Keeping the tip within a distance of $\cong \langle \langle \lambda/2 \rangle$ (i.e. a few nm) and scanning it across the sample allows the recording of images with a spatial resolution far better than the diffraction limit, given approximately by the size of the tip itself (Lewis et al. 1984; Pohl et al. 1984). Such near-field scanning optical microscopy (NSOM) has been applied in many areas (Novotny & Hecht, 2006), including biological imaging (Betzig et al. 1993; Kirsch et al. 1996). For example, with spatial resolutions of down to 80 nm, NSOM has given insights into the nanoscale organization of proteins on the plasma membrane of (living) cells (de Bakker et al. 2007; van Zanten et al. 2010). Unfortunately, the requirement of keeping the tip very close to the sample comes at a high cost: on one hand, an elaborate feedback mechanism has to be applied to keep the sample-tip distance constant (especially for dynamic living cells) (Koopman et al. 2004). On the other hand, one is bound to imaging surfaces, and this precludes the use of NSOM to explore the (3D) nanoscopic interior of the living cell. With this drawback, the applicability of NSOM will remain limited, which may be a reason why most biophyiscal observations keep on relying on far-field optics.

Total-internal-reflection fluorescence (TIRF) microscopy relies on evanescent fields as well. Here the evanescent field is created at the microscope's cover glass–sample interface by illuminating with (laser) light that is totally internally reflected at the glass–water interface (Axelrod,



Fig. 1. Diffraction-limited far-field fluorescence microscopy. An object is illuminated with excitation light (blue) and its fluorescence (green) imaged onto a detector using a lens system, whereby the object is placed $\geq \mu m$ away from any optics. (a) In a wide-field microscope a large area of the object is illuminated at once and signal imaged onto a camera. (b) In a point-scanning confocal microscope a diffraction-limited volume is illuminated, signal detected on a point-detector through a pinhole, and the final image formed by scanning the spot over the object. The size of the focused and observed spot is governed by the focusing strength of the objective lens (given by the angle α), the wavelength λ of the applied light, and the refractive index *n* of the object medium. Bax: Due to the focusing of light one cannot image point-like objects to dimensions smaller than approximately 200 nm in the lateral (x,y) and 600 nm in the axial (z) directions for visible light. This finite-sized, diffraction-limited point spread function (PSF) precludes the discerning of alike objects closer together than these 200 nm and results in blurred images at these spatial scales. Different versions of far-field microscopy have been implemented with the goal to push the diffraction barrier to its limits. (c) A two-fold increase in spatial resolution has been realized by SIM using, for example, a standing wave pattern in a wide-field mode with the pattern maxima separated by more than the 200 nm. (d) Using two opposing objective lenses for illumination and/or detection, the axial resolution of a wide-field or point-scanning/confocal microscope can be enhanced multi-fold, denoted I³M or 4Pi, respectively. (Here, red: excitation, and green: fluorescence)

1981). With a finite penetration depth of the evanescent excitation field of typically <100 nm, TIRF microscopy only detects the fluorescence emitted from near the cover glass–sample interface. Consequently, TIRF microscopy is not a far-field optical technique, but virtually a two-dimensional (2D) microscopy technique that is not really applicable to explore the interior of a

cell. Nevertheless, TIRF efficiently suppresses the background from out-of-focus structures, and it is therefore well suited to explore the cellular boundaries, such as the plasma membrane and ligand–receptor interactions (see, e.g. Lieto *et al.* 2003).

Starting in 2000, the idea was put forward to use negative refractive index metamaterials (Pendry, 2000) for imaging with sub-diffraction resolution in the far-field. Introduced as a hyperlens (Liu *et al.* 2007; Smolyaninov *et al.* 2007), evanescent waves were converted into propagating waves forming a magnified image of the sample on a distant screen. Considered as a far-field image projection, the use of negative refractive index metamaterials (the hyperlens) also relies on collecting an evanescent wave, i.e. it requires the placing of the sample into very close proximity to the hyperlens – more specifically into its near-field. Hence, although it introduces a very interesting approach of employing evanescent waves, the hyperlens in its current state cannot be regarded as a far-field imaging device capable of observing inner-cellular structures (Podolskiy & Narimanov, 2005).

1.2 Pushing the limits of the diffraction barrier

It is due to the above limits of other techniques why most biophysical and biomedical applications still relied on the use of far-field optics, and several ideas have been put forth to address the resolution problem. These ideas included the use of special illumination patterns, like first suggested in 1952 by Toraldo di Francia (1952) or later on followed by Cremer and Cremer (1978). The use of these concepts was rendered impractical by either strong side lobes of the focused light (Toraldo di Francia, 1952), or the fact that it is impossible to achieve light convergence to a sub-diffraction focal spot (in the absence of relayed near-field components) (Cremer & Cremer, 1978). Purely mathematical processing of the imaging data has also been suggested several times to overcome the diffraction barrier (Bertero & Boccacci, 1998; Bertero et al. 1990; Conchello & McNally, 1996). Such computational methods usually required a priori knowledge of parameters of the imaging system (e.g. the PSF) and/or of the imaged object. Due to a potential lack of accurate *a priori* information, these approaches were however prone to artifacts and rarely exceeded a two-fold increase in spatial resolution. These limitations might be partially mitigated through additional a priori constraints such as the objects featuring different absorption or emission spectra (Burns et al. 1985), but marking all features in the sample with different labels – and hence achieving a general imaging strategy for the sub-diffraction interrogation of arbitrary structures - becomes itself difficult, if not impossible.

In a spot-scanning confocal microscope the sample is illuminated with a diffraction-limited focused spot and the fluorescence emission confocally detected with a symmetrically arranged point detector, which is usually realized by inserting a detection pinhole (Fig. 1*b*). The confocal detection does, however, not really provide a higher resolution. Theoretically, the width of the effective focal spot or PSF is reduced by a factor of $\sqrt{2}$ (Minsky, 1961; Pawley, 2006; Wilson & Sheppard, 1984). This improved spatial information is however usually heavily damped and thus lost in noise. The biggest benefit of detecting through a pinhole is a superb background rejection, which significantly improves 3D-imaging and which is the reason why the confocal laser scanning microscope can be considered as the workhorse of fluorescence 3D-microscopy (Pawley, 2006; Wilson & Sheppard, 1984).

Another approach that has often been connected with resolution improvement is the use of two-photon excitation. Here, the simultaneous absorption of two photons results in excitation of the fluorophore. The wavelength of the excitation light is thereby usually chosen to be double the wavelength λ that would be used for conventional one-photon excitation (Bloembergen, 1965; Denk *et al.* 1990; Sheppard & Kompfner, 1978). The resulting non-linear squared dependence of the fluorescence emission on the excitation intensity establishes a clear reduction of the width of the effective focal spot or PSF by a factor of $\sqrt{2}$. Unfortunately, doubling the wavelength (2λ) comes with a doubling of the size of the diffraction spot (Denk *et al.* 1990), i.e. in total the spatial resolution of a two-photon microscope is usually slightly poorer than its one-photon counterpart (Schönle *et al.* 1999). The same arguments are valid for *m*-photon absorption processes, because they usually require an even longer wavelength $m\lambda$. The advantage of a multiphoton microscope lies in other factors such as a deep penetration depth, low scattering and the restriction of photobleaching to the focal spot.

Several approaches have suggested the use of structured illumination for increasing the spatial resolution of a far-field fluorescence microscope (e.g. Ash & Nicholls, 1972; Bailey et al. 1993; Lukosz, 1966). Structured Illumination Microscopy (SIM) by a standing wave pattern (Fig. 1d) is nowadays a well-established microscopy technique allowing the far-field imaging of living cells with a two-fold improvement in the lateral and axial resolution (Frohn et al. 2000; Gustafsson, 2000; Gustafsson et al. 2008; Schermelleh et al. 2008). Similarly, SIM has also been realized based on a software-based confocal CCD detection approach using scanning single-(Muller & Enderlein, 2010) or multi-spot (York et al. 2012) illumination, or it has been combined with TIRF (Fiolka et al. 2008). The use of two opposing objectives in either a spot-scanning 4Pi (Hell, 1992; Hell & Stelzer, 1992; Hell et al. 1994) or a widefield I⁵M (Gustafsson et al. 1995, 1996, 1999) microscope realized an improvement of the axial resolution of a far-field microscope from 400-800 nm down to 70-150 nm (Fig. 1d). The latter approaches are often of special interest to microscope users since the axial resolution of any standard far-field light microscope is at least 3-times poorer than the lateral resolution in the focal plane. This particularly limits the 3D imaging of transparent objects such as cells. Both SIM and 4Pi microscopes are nowadays commercially available systems, and the enhanced resolution of both techniques has allowed the observation of live cellular structures with larger detail, giving a significantly improved insight into cellular functions (Bewersdorf et al. 2006; Egner & Hell, 2005; Egner et al. 2002, 2004; Gugel et al. 2004; Gustafsson et al. 2008; Schermelleh et al. 2008; Weil et al. 2012). However, the spatial resolution of these microscopes is still limited, i.e. they do not break the diffraction barrier, but they rather push diffraction to its limits.

1.3 Breaking the diffraction barrier

While the rationales of all previously mentioned methods such as SIM or 4Pi/I⁵M, or NSOM, are based on modifying the propagation of light in one way or another, a real breakthrough for the surpassing of the diffraction barrier was the insight that the properties of the fluorophore itself can be used to attain in principle unlimited (actually molecular-size) spatial resolution in the far-field (Hell, 1994; Hell & Kroug, 1995; Hell & Wichmann, 1994). It was realized that one can take advantage of the transitions between different states (ground, excited and dark states) of the fluorescent label, i.e. its spectroscopic properties, to modify the fluorescence emission in such a way as to neutralize the limiting role of diffraction (Hell, 1994). Until then, fluorophores were primarily regarded as indicators of molecular species or environmental conditions (such as pH, ion concentrations). That they should also hold the key to nanoscale resolution in a far-field microscope was thus a major change in the perception of the fluorophores' role and capability in microscopy. The implementation of this idea started with STED (Hell &



Fig. 2. Sub-diffraction imaging by the coordinate-targeted (deterministic) approach (STED/RESOLFT): driving molecular transitions in space. (a) Sub-diffraction imaging is based on reversibly inducing transitions between molecular states of different fluorescence emission properties (such as a bright ONand a dark OFF-state), where at least one of the transitions such as the ON-to-OFF transition is driven by light (left). Increasing the intensity of the turn-off light above a certain threshold turns off the fluorescence emission (right). (b) In its single-spot scanning version the diffraction-limited spot of the fluorescence excitation or turn-on laser (green) is overlaid with an additional turn-off laser which features a central intensity zero (red). Increasing the intensity I of the turn-off laser far above a threshold value

Wichmann, 1994; Klar & Hell, 1999; Klar et al. 2000), GSD (Bretschneider et al. 2007; Hell & Kroug, 1995) and RESOLFT (Hell, 2004; Hell et al. 2003; Hofmann et al. 2005) microscopy, which thus emerged as the first concrete and viable physical concepts to overcome the limiting role of diffraction in a lens-based optical microscope. While these approaches reversibly inhibit the occupation of a molecular state (usually the emissive state) at defined spatial coordinates using deterministic scanning, subsequent developments such as (F)PALM (Betzig et al. 2006; Hess et al. 2006) or STORM (Rust et al. 2006) transfer the fluorophores to their emissive state stochastically in space and utilize the spatial localization of single isolated molecules based on the emitted fluorescence pattern of the individual molecules, to assemble the final image. Still, the basic requirement remains the same: the preparation of at least two transient states of the fluorescent labels with discernible emission properties. The most prominent example is a pair of a bright (fluorescent) ON- and a dark (non-fluorescent) OFF-state, where at least one transition such as the ON-to-OFF transition is driven by light. The molecular states involved do not necessarily have to be dark and bright states. They can also differ in other fluorescence properties such as absorption cross-section, emission wavelength, fluorescence lifetime or another property, i.e. their detected signal has to be discernible. For simplicity, we keep to the notation of ON- and OFF-states and denote the light driving the OFF-ON and ON-OFF transition by 'turn-on' and 'turn-off' light.

The prospects of these super-resolution microscopes or nanoscopes to image the living cell with conceptually unlimited (presently $\sim 10-50$ nm) spatial resolution is revolutionizing modern microscopy and has a major impact on biophysical and biomedical research.

2. The coordinate-targeted approach

The initially developed coordinate-targeted approaches STED, GSD or RESOLFT utilize an illumination pattern. Specifically, an intensity distribution of either the turn-on or turn-off laser is created that features at least one intensity zero to transiently confine the occupation of usually the ON-state, i.e. the fluorescence emission, to sub-diffraction sized areas or volumes (Fig. 2). Increasing the intensity of this modified laser above a certain threshold basically then turns off the detected fluorescence emission (Fig. 2*a*). The restriction of the occupation of ON-states and thus (detected) fluorescence emission to sub-diffraction dimensions is ensured by (1) an overlay of the turn-off laser with the fluorescence excitation (or turn-on) laser, and (2) an intensity of the turn-off laser above the mentioned threshold.

A unique feature of this principle is that the size of the effective observation area/volume and thus the spatial resolution of the microscope is tuned by the intensity of the turn-off laser. More specifically, it has been shown that, for example, the lateral resolution as given by the diameter (or

 $⁽I_S)$ confines the volume in which fluorescence emission is allowed to sub-diffraction dimensions, i.e. it creates an observation spot with diameter d << 200 nm (orange). Insets: respective focal intensity distributions. Lower right: Diameter of the observation spot *versus* intensity of the turn-off laser (example data for STED). With the spatial coordinates known, scanning of this spot realizes imaging with sub-diffraction resolution, and thus the discerning of alike objects closer together than 200 nm (upper panel). (c) In a multi-spot realization, the added turn-off light features several intensity zeros, such as realized for a wide-field microscope by a standing-wave pattern or many doughnuts with the pattern maxima or doughnut minima separated by more than the 200 nm. Increasing $I >> I_S$ restricts fluorescence emission to multiple spots or lines of sub-diffraction dimension, and scanning of these spots or lines over the sample realizes images with sub-diffraction resolution.

FWHM) of the observation area $d \approx \lambda/(NA\sqrt{(1 + I/I_s)})$ approximately scales with the inverse square-root of the intensity *I* of the turn-off laser (Harke *et al.* 2008a; Hell, 2004; Hell *et al.* 2003). Here, I_s is the above-mentioned threshold intensity (often denoted saturation intensity), which is a characteristic of the fluorophore (involving the light absorption cross-section of the ON–OFF transition and the lifetime of the involved states) and of the steepness of the edges of the intensity zeros. Driving the intensity *I* further and further up thus creates continuously smaller observation areas down to the size of a single molecule.

In usual practice, the wavefront of the turn-off laser is modified by the insertion of a phase plate or grating in such a way that the focusing creates one or multiple intensity zeros. In the case of the single-point scanning microscope usually a doughnut-like intensity distribution with a central intensity zero is preferred (Fig. 2b) (Keller, 2006; Willig et al. 2006a). Scanning of the reduced-size observation spot then renders a direct image of the distribution of fluorescently marked molecules with nanoscale spatial resolution. However, as will be discussed later on, other intensity distributions have been realized as well, for example confining the fluorescence along the axial z-direction (Klar et al. 2000) or even along all spatial directions, creating an almost isotropic spot (Harke, 2008; Harke et al. 2008a, b; Schmidt et al. 2008). In the case of the wide-field microscope, usually a standing-wave-like pattern with multiple zero-intensity lines such as in SIM is created. The camera images recorded for multiple scanning positions of the zeros are then post-processed to reconstruct the final image (Gustafsson, 2005; Heintzmann et al. 2002; Rego et al. 2012; Schwentker et al. 2007). As shown recently, a preferred mode is to scan multiple points or doughnuts instead of rotating entire lines (Chmyrov et al. 2013). In any case, for $I \gg I_S$ alike features closer together than the diffraction-limited 200 nm are now distinguishable, since they are switched on and thus detected separately in time. For the wide-field approach, this requires neighboring intensity zeros to be separated by more than the diffractionlimited 200 nm.

It is obvious that the increased image resolution comes along with a reduction of the scanning step size; the molecules that were 'off' initially have to be turned 'on' later, etc. Therefore, an accurate acquisition of nanoscale details requires an increased number of scanning steps and consequently longer acquisition times. Nevertheless, this coordinate-targeted approach offers all features of a conventional microscope from multicolor and 3D image acquisition over single-molecule detection to deep-tissue or *in-vivo* imaging. In the following, we will present these capabilities of coordinate-targeted scanning nanoscopy, starting with the so far most developed technique, STED nanoscopy.

2.1 STED nanoscopy

In STED nanoscopy, the pair of molecular states are the fluorophore's ground (dark OFF) state S_0 and the excited (fluorescent ON) state S_1 , respectively. Being initially in the S_0 OFF-state, excitation to the S_1 ON-state and thus fluorescence emission is driven by the excitation laser, while switching back to S_0 is realized by stimulated emission using a second laser, the STED laser. The wavelength of the STED laser is usually chosen in the far red part of the fluorophore's emission spectrum to ensure for the STED light (1) a sufficiently large cross-section for stimulated S_1 to S_0 de-excitation, (2) a close-to-zero probability for S_0 to S_1 excitation and (3) a straightforward way to block the stimulated emission and STED light from the detection of the spontaneous fluorescence emission. Above a certain threshold intensity the STED light causes a more efficient stimulated than spontaneous S_1 to S_0 de-excitation, i.e. an inhibition of the detected (spontaneous) emission. The threshold or saturation intensity $I_S = (\tau \sigma_{STED})^{-1}$ of the STED light is defined by the photon cross-section σ_{STED} of stimulated emission at the wavelength λ_{STED} of the STED laser and the lifetime τ of the excited S_1 state. With lifetimes in the range of 1–4 ns and stimulated emission cross-sections in the range of 10^{-17} cm² (i.e. photon cross-sections $\sigma_{STED} \approx 25-30$ cm²/J) STED intensities of usually $I_S \gg 1-10$ MW/cm² have to be applied to realize a sufficiently large fluorescence inhibition. Therefore, a preferred implementation of the STED concept is the use of pulsed excitation and STED lasers, where the concomitant high pulse peak intensities and the optimized timing (with the STED laser swiftly following the excitation pulse) result in very efficient stimulated emission (Donnert *et al.* 2009; Klar *et al.* 2000) (compare chapter 2.1.6).

One of the first biologically relevant experiments in STED imaging related to the observation of synaptic vesicles (Willig *et al.* 2006c). Synaptic transmission is mediated by neurotransmitters that are stored in synaptic vesicles and released by exocytosis upon activation. The vesicular membrane is retrieved by endocytosis, and synaptic vesicles are regenerated and re-filled with neurotransmitter. While many aspects of vesicle recycling are well understood, the fate of vesicle membranes after fusion was still unclear. Do their components diffuse on the plasma membrane, or do they remain together? This question had been difficult to answer because, with a size of approximately 40 nm in diameter, synaptic vesicles are too small to be resolved by conventional diffraction-limited fluorescence microscopes. With STED microscopy, individual synaptic vesicles were visualized in the synapse at a resolution of 65 nm (Fig. 3*a*). It was shown that synaptotagmin I, a protein resident in the membrane, remains clustered in isolated patches on the presynaptic plasma membrane.

Similarly, with its improved spatial resolution STED nanoscopy could uncover new details of various cellular structures, protein clusters or DNA (e.g. Blom *et al.* 2011; Dyba *et al.* 2003; Kellner *et al.* 2007; Kittel *et al.* 2006; Lau *et al.* 2012; Muller *et al.* 2012; Opazo *et al.* 2012; Persson *et al.* 2011; Schmidt *et al.* 2008, 2009; Sieber *et al.* 2007; Wagner *et al.* 2012), making a STED microscope a uniquely helpful tool nowadays in cell-biological laboratories (Clausen *et al.* 2013). Furthermore, STED has important applications outside biology, ranging from nanoscale imaging of assemblies of colloidal particles and polymeric structures (Friedemann *et al.* 2011; Harke *et al.* 2008b; Ullal *et al.* 2009, 2011) to solid-state physics (Wildanger *et al.* 2011). With its capabilities and simplifications steadily growing, as outlined further on, and commercial instrumentation improving (Clausen *et al.* 2013), STED nanoscopy may become a workhorse of imaging facilities, greatly extending the resolving power of confocal microscopes.

2.1.1 Multicolor STED nanoscopy

In most cellular applications it is desirable not only to resolve a single structure at a time, but to highlight the relative sites and proximities of different molecules. In fluorescence microscopy this is usually realized by tagging the different molecules with different fluorescent labels, whose emission is then distinguished by its specific color, lifetime or potentially other fluorescence parameters. In a preferred implementation, the wavelength of the emitted light is chosen as a delimiter, and the fluorescence emission of the different labels is excited with lasers of different wavelength and detected on separate detectors monitoring different wavelength ranges. This principle is transferable to STED microscopy, however with the requirement of supplying a multitude of additional STED lasers, strictly speaking one for each label used. While this approach has rendered two-color STED imaging (Donnert *et al.* 2007b) possible, and revealed the co-localization of different proteins and structures on the nanometer-scale (Meyer *et al.* 2008), it entails a rather



Fig. 3. STED nanoscopy. (a) A reversible molecular transition is realized by stimulated emission (inset): the turn-on light excites (Exc) the fluorophores from their (dark) ground S_0 to their (bright) excited S_1 state, where de-excitation by spontaneous fluorescence emission (Flu) is overruled by the addition of the STED laser inducing stimulated emission. Example scanning STED nanoscopy image of fluorescently labeled synaptotagmin I in fixed cultured hippocampal neurons, exemplifying the superior spatial resolution over conventional confocal microscopy and revealing that this protein is clustered in isolated patches on the presynaptic plasma membrane after synaptic vesicle exocytosis (adapted from (Willig et al. 2006c)). Scale bar: 1 µm. (b) Confocal (upper right) and STED images of immunolabeled microtubules in fixed mammalian cells (adapted from Wurm et al. 2012). Scale bar: 500 nm. (c) Multi-color STED nanoscopy determining the co-localization of different molecules with sub-diffraction resolution, as exemplified for the D1 dopamine receptor and Na1,K1-ATPase in cultured striatal neurons (lower image: confocal recording, adapted from (Blom et al. 2012)). Scale bars: 1 µm (in enlarged image: 200 nm). (d) Multi-color STED and confocal (peripheral parts) recordings of immunolabeled subunits in amphibian nuclear pore complexes (NPCs) of cultured Xenopus cells with close-ups (right) of the spatial organization of the peripheral gp210 and central pore pan-FG proteins in a single NPC (adapted from Göttfert et al. 2013). Scale bar: 500 nm. (e) 3D STED nanoscopy realized by overlapping two STED beams featuring confinement along the lateral x/y and axial z direction, respectively (left: x-y (upper) and $x-\gamma$ (lower) projections of the intensity distributions of the two STED lasers, scale bars: 200 nm), and by the use of two opposing microscope objectives (O1 and O2, right). The resulting isotropic observation spot of diameter below 40 nm allows the recording of super-resolved 3D images, as exemplified by resolving mitochondrial christae (middle, scale bar: 1 µm, adapted from (Schmidt et al. 2009)). (f) RESCue STED: Reduction of photobleaching in 3D STED imaging by applying an intelligent light exposure scheme that minimizes the number of excitation/de-excitation events a fluorophore has to undergo during recording of a scanning image: conventional (upper) and RESCue (lower) 3D STED

complex setup with the correct alignment of four lasers, two excitation and two STED beams. Furthermore, the simultaneous recording of the two colors proves itself somewhat difficult, since the more blue-shifted STED laser usually leads to a strong excitation and thus massive photobleaching of the more red-emitting dye. Therefore, initial two-color STED images were recorded sequentially. This limitation has been solved by straightforward optimizations of the choices of labels and wavelengths: (1) the combination of two labels with overlapping emission spectra and with a long (Stokes) shift between the excitation and emission spectrum of one of the labels allows the recording of two-color STED images with two excitation lasers but only one STED laser (serving both labels) (Clausen et al. 2013; Dean et al. 2012; Friedemann et al. 2011; Pellett et al. 2011; Schmidt et al. 2008). (Quasi-) simultaneous recording of both colors is possible in either a line-by-line or a pulse-interleaved excitation scheme, in both cases rapidly switching between the two excitation lasers. (2) Nanoscopic co-localization studies of various different proteins have been enabled by a carefully optimized choice of two conventional Stokes-shifted fluorophores, whose spectra differ by only about 60 nm, the use of two pairs of excitation/ STED lasers timed in a pulsed interleaved excitation scheme, and with an elimination of the detection cross-talk by applying linear unmixing algorithms (Fig. 3c, d) (Blom et al. 2012; Dean et al. 2012; Neumann et al. 2010; Opazo et al. 2010; Reisinger et al. 2011; Osseforth et al. 2013). In this scheme, the number of distinguishable labels could be increased to four by separating the emission based on emission wavelength and lifetime (Bückers et al. 2011). (3) Recent two-color STED imaging has been realized using two excitation and a single STED laser only, e.g. 594 and 640nm excitation in combination with a 775nm STED laser (Göttfert et al. 2013). (4) Instituting rigorous linear unmixing with a single excitation and a single STED laser were sufficient to record twocolor STED images of labels such as the yellow fluorescent protein (YFP) and green fluorescent protein (GFP), whose spectra are separated by about 20 nm (Tonnesen et al. 2011). Similarly, combining two reversibly photoswitchable fluorescent proteins (RSFPs) with opposite activation properties, two-color STED images were recorded with just one pair of excitation and STED lasers, without the necessity of applying linear unmixing, but with the addition of blue-light photoswitching (Willig et al. 2011). With the ongoing development of fluorescent labels and lasers, the number of fluorophores and matching excitation/STED laser pairs useful for multicolor STED imaging schemes will increase further.

2.1.2 3D STED nanoscopy

So far we have presented images recorded with STED nanoscopes which confine fluorescence emission and thus improve spatial resolution along the lateral direction only (using, e.g. the previously mentioned doughnut-like intensity distribution). The combination of this modality with an evanescent wave illumination (TIRF) scheme for excitation (Gould *et al.* 2011; Leutenegger *et al.* 2012) is sufficient for selectively imaging membranes of flat cells with penetration depths of <100 nm, and the combination with two-photon excitation realized imaging in ~800 nm thick sections with deep penetration depths (Bethge *et al.* 2013; Bianchini & Diaspro, 2012; Ding *et al.* 2009; Li *et al.* 2009b; Moneron & Hell, 2009; Takasaki *et al.* 2013). However, the imaging of intra-cellular structures such as the Golgi apparatus or mitochondria often requires both a

recordings of fluorescent immunostained nuclear lamina in fixed neuroblastoma cells (arrow: third dimension scanning direction (y), adapted from (Staudt *et al.* 2011)). Length of coordinate bars: $x/z \perp \mu$ m, $y \perp 0.5 \mu$ m.

deeper penetration depth and an improvement of the spatial resolution along the axial z-direction as well. Four approaches have been applied so far: (1) The use of a phase plate that, upon interference, inhibits fluorescence along γ and preferentially its combination with the doughnut-shaping plate creates the desired fluorescence restriction along all spatial directions (Fig. 3e) (Harke et al. 2008a, b; Klar et al. 2000; Wildanger et al. 2009b; Osseforth et al. 2013). (2) The use of the doughnut-shaped STED focus in conjunction with illumination by two opposing objectives (as for 4Pi) has realized spatial resolution along the axial direction of down to 33 nm (Dyba & Hell, 2002; Dyba et al. 2003), or was used to create an effective isotropic observation volume with a spatial resolution of down to 30 nm along all spatial directions (Hell et al. 2009; Schmidt et al. 2008). Such an isoSTED microscope has given new insights into mitochrondrial structure, for example for the first time resolving the mitochondrial cristae with an optical microscope (Fig. 3f) (Schmidt et al. 2009). (3) Recently, a combination of STED with single plane illumination microscopy (SPIM) realized an almost two-fold improvement in axial resolution along with an 1.3-fold improvement along the lateral directions compared to conventional SPIM. Applying this illumination scheme, STED-SPIM should allow penetration depths of $>100 \,\mu\text{m}$ and thus realize imaging inside zebra fish (Friedrich et al. 2011). (4) Adaptive optics allows the correction of aberrations occurring predominantly when imaging in 3D deep inside tissue (Gould et al. 2012, 2013).

2.1.3 Photo-physical and -chemical considerations in STED nanoscopy

The signal strength and observation time of fluorescence experiments is limited by the population of metastable dark states and the photobleaching of the fluorophore label (e.g. Eggeling et al. 1998, 1999; Tsien et al. 2006). Fluorescence emission follows the excitation of the fluorophore from its ground to its excited electronic state by, for example, laser light. The frequency and number of emitted photons depend on how fast and how many times one can cycle the fluorophore between the ground and excited state, respectively. In the excited state, the fluorophore becomes more fragile as reaction pathways to non-fluorescent species (such as ionization and/or breaking of double bonds) are opened up which can result in photobleaching, an irreversible loss of the ability to fluoresce. Furthermore, in the excited state the fluorophore may cross to metastable dark states of microsecond- to second-long lifetimes (such as the triplet state or radical states for usual organic dyes or fluorescent proteins), where the fluorophore is disengaged from the fluorescence cycling process, thus reducing the number of emitted photons. These long-lived dark states are much more prone to photobleaching than the first excited singlet state. For example, the triplet state efficiently interacts with molecular oxygen, generating highly reactive singlet oxygen (for a review see e.g. Eggeling et al. 1999). On the other hand, high laser irradiances as for example used in scanning confocal microscopy open up new efficient photobleaching pathways by further exciting the already excited fluorophore to higher electronic states (e.g. Eggeling et al. 1998, 2005; Widengren & Rigler, 1996). In aqueous environments, these excited species couple quite efficiently with ionic states and are thus highly reactive (e.g. Anbar & Hart, 1964; Reuther et al. 1996), usually characterized by more than ten-fold higher photobleaching probabilities than found from the first excited electronic states (e.g. Eggeling et al. 1998, 2005). Such non-linear photobleaching mechanisms are exceedingly efficient from the dark states due to their relatively long lifetime.

The accommodation of a large number of continuous excitation/de-excitation cycles and thus the maximization of the fluorescence signal has been approached by choosing experimental conditions which minimize the reactivity of the excited states as well as the populations of dark and higher excited states. This can either be done by choosing an appropriate dye with low photobleaching probabilities, low absorption cross-sections of the excited states and low dark state populations (e.g. Dittrich & Schwille, 2001; Eggeling et al. 1999, 2006; Tsien et al. 2006), or by the addition of chemicals (such as radical quencher or mercapto-compounds) that result in a reduction of photobleaching probabilities (especially of the higher excited electronic states) or in a quenching of the dark states (e.g. Dave et al. 2009; Dittrich & Schwille, 2001; Eggeling et al. 1999, 2006; Rasnik et al. 2006; Vogelsang et al. 2008; Widengren et al. 2007). Unfortunately, an appropriate fluorophore may not always exist, or the addition of (sometimes toxic) chemicals is often invasive and not live-cell compatible. The minimization of dark state populations and non-linear photobleaching processes therefrom was approached with a method termed dark- or triplet-state relaxation (D- or T-Rex) microscopy (Donnert et al. 2006, 2007a). The D- or T-Rex principle makes use of low-repetition pulsed laser light (Donnert et al. 2006, 2007a) or of ultra-fast scanners (Donnert et al. 2009) to allow for an efficient depopulation of any dark state population in-between excitation events, thereby minimizing dark-state build-up and non-linear photobleaching from these states. The use of fast beam-scanning microscopes, where D-/T-Rex is effectively implemented, is especially suitable for live-cell fluorescence imaging experiments (Borlinghaus, 2006; Conchello & Lichtman, 2005; Tsien et al. 2006; Vukojevic et al. 2008; Webb et al. 1990).

In STED, the fluorophores are forced to undergo numerous transitions between their ground and excited state from which photobleaching or a dark-state transition may occur (Fig. 4*a*) (Donnert *et al.* 2006; Dyba & Hell, 2003). In addition, increasing the irradiance of the STED laser to increase the gain in spatial resolution requires an adaptation of the scanning imaging process, with smaller pixel sizes and thus a larger number of scanning steps, unfortunately increasing the number of cycles that a molecule has to undergo during the recording of an image. Therefore, a key to sub-diffraction STED (or, similarly, GSD and RESOLFT) imaging is to ensure that the marker is able to switch repeatedly between its ON and OFF states in the presence of both the switch-on and switch-off light.

Stimulated emission reduces the lifetime of the excited state and therefore in principle increases the photostability of the fluorophore in comparison to action of the excitation laser only (Fig. 4b). However, unwanted excitation to the higher excited states usually antagonizes this process (Fig. 4a). As a consequence, it was the realization of D- or T-Rex (see above) STED imaging that demonstrated for the first time down to 20 nm macro-molecular spatial resolution in cells (Donnert et al. 2006), and it is the implementation of fast beam-scanning that nowadays allows routine live-cell STED nanoscopy (compare Section 2.1.5) (Fig. 4c) (Moneron et al. 2010). Additionally, STED nanoscopy becomes much more feasible by choosing fluorophores with a low absorption cross-section of the first excited state at the wavelength of the STED laser (Hotta et al. 2010), or by appropriately adapting the latter to minimize non-linear photobleaching (Fig. 4d) (Rankin et al. 2011). This has recently allowed STED imaging in an intact living organism, namely Caenorhabditis elegans expressing eGFP (Rankin et al. 2011). STED at nitrogen temperatures attempted to minimize photobleaching and to maximize the efficiency of stimulated emission (Fig. 4e) (Giske, 2007), unfortunately making live-cell studies less feasible. The choice of other promising emitters such as the very photostable nitrogen vacancy (NV) centers in diamond has recently allowed STED imaging with a spatial resolution of down to 5 nm (see Section 2.3) (Han et al. 2012; Rittweger et al. 2009a). Similarly, special quantum dots (QDs) could be used in a STED-like fashion (Irvine et al. 2008). Unfortunately, the use of most conventional QDs for STED is so far impeded by their low Stokes shift and narrow band of emission. Nevertheless, a large range of appropriate fluorophores for STED nanoscopy is now known. Still, the



Fig. 4. STED nanoscopy: photophysics and bleaching. (a) Photobleaching pathways: excitation (Exc) elevates a fluorophore from its ground S_0 to its first excited electronic state S_1 , from where it either returns to S_0 by spontaneous fluorescence emission (Flu) or by STED, or it traverses with probability Φ_D to a dark state whose lifetime τ_D (time before return to S_0) is much longer than that of S_1 . Photobleaching may occur from S_1 and the dark state, and is most pronounced from higher excited electronic states after further absorption of excitation or STED light (higher-order photobleaching, dashed lines). Horizontal lines: electronic states (thick) and vibrational sub-states (thin). Curved lines: vibrational transitions. (b) Suppression of photobleaching rate by STED: stimulated emission shortens the lifetime of S_1 and thus the probability of photobleaching as exemplified by the percentage of signal bleached after scanning a layer of the organic dye KK114 with and without the addition of STED light (excitation at 488 nm with 9 kW/cm² and STED at 760 nm with 0.8 GW/cm², repetition rate 76 MHz, scanning dwell time 10 ms). (c) Higher-order photobleaching from long-lived dark states, as exemplified by subsequent scanning STED images of 40-nm sized fluorescent beads, showing a significant loss of signal due to irreversible photobleaching (upper images). D-Rex illumination, i.e. increasing the time ΔT between subsequent pairs of excitation and STED pulses (i.e. decreasing the repetition rate $1/\Delta T$) above the dark states lifetime τ_D allows the dark states to relax before incidence of the next pulses, avoiding higher-order photobleaching (lower images). D-Rex illumination by fast beam scanning (lower panel): for a fluorophore the incidence of only a few excitation-STED pulse pairs of high repetition rate (e.g. 80 MHz) is followed by a long resting period ΔT until the scanned beam pair hits the same spot again. (d) Higher-order photobleaching from the first excited electronic state S_1 , as exemplified for the organic dyes pDI and pTDI and for eGFP. Absorption spectra of S_0 (blue) and S_1 (red) and fluorescence

development of new bright and photostable dyes, often specialized for STED applications, has and continuously will enhance the applicability and flexibility of experiments using this super-resolution technique (Boyarskiy *et al.* 2008; Kolmakov *et al.* 2010a, 2010b, 2012; Mitronova *et al.* 2010; Wurm *et al.* 2012).

The number of cycles that a molecule has to undergo is severely increased when recording 3D images, where one plane after the other is scanned at different optical (z) axis positions. Here, an intelligent light exposure scheme was put into practice. Related to controlled light exposure microscopy – introduced for decreasing photobleaching and increasing the number of detected fluorescence photons in scanning microscopy (Hoebe *et al.* 2007) – the reduction of state transition cycles (RESCue)-STED scheme uses an online feedback algorithm that rapidly switches off the excitation and STED light during a scanning step when no or only low signal is detected (Staudt *et al.* 2011). Thereby, the cycling of nearby fluorophores is minimized and the total number of on–off cycles significantly reduced. For 3D scanning imaging, this reduces the probability of dark state transitions and photobleaching in the adjacent axial planes, consequently increasing the number of planes that can be successively recorded (Fig. 3f).

2.1.4 Cluster analysis in STED nanoscopy

Clustering of molecules is key in a lot of cellular processes. Unfortunately, these clusters can often not be characterized accurately, especially in the living cell, mainly because their sizes are usually below the diffraction barrier and thus cannot be determined with conventional light microscopy. The use of a STED nanoscope is an obvious way to overcome this limitation. STED was applied to image various molecular assemblies in different cells, tissue or membranes. To name a few, STED imaging was used to study the clustering to ~70-nm large spots of a synaptic vesicle protein after exocytosis (Fig. 3*a*) (Willig *et al.* 2006c), the anatomy of supra-molecular membrane protein clusters of approximately 50–60 nm in diameter (Sieber *et al.* 2007), the dynamics of approximately 80-nm large synaptic vesicle movements (Westphal *et al.* 2008), or the formation of domains in phase separated membrane bilayers of down to below 40 nm in diameter (Honigmann *et al.* 2013b, 2012). These examples have in common that previously blurred structures are now revealed as a multitude of single isolated clusters. Besides the cluster size, STED

emission spectra (green) show that excitation to higher excited states from S_1 by the STED light may be significant for pDI and for eGFP at >595 nm, but not for pTDI, and for eGFP at <595 nm, resulting in far less photobleaching for pTDI, exemplified in CW-STED images of single pDI and pTDI molecules (confocal images were taken prior to STED recordings, pTDI: STED (white circle) and confocal recording (outer region), scale bar 500 nm, adapted from (Hotta et al. 2010), and for eGFP the STED wavelength between 556 and 592 nm, exemplified in STED recordings of live Vero cells expressing eGFP in the endoplasmic reticulum (middle panel, lower left corner: confocal image, scale bar: 1 µm, adapted from (Rankin et al. 2011)). (e) STED at nitrogen temperatures. (Left) The cross-section of stimulated emission is highest at wavelengths close to the fluorescence emission maximum as exemplified for the organic dye Atto532 (columns: cross-sections of stimulated emission at selected wavelengths, black line: fluorescence emission spectrum scaled to the cross-section value at 568 nm). (Middle) As a consequence, less intensity of STED light is required for 568 nm compared to 605 nm to increase the spatial resolution in STED images of 80 nm-large Atto532-labeled beads, as determined for different intensities of the STED laser. (Right) STED imaging at 568 nm is however only possible at nitrogen temperatures, since the relative fluorescence emission evoked by the STED light increases for wavelengths closer to the emission maximum, but this anti-Stokes fluorescence excitation is efficiently suppressed at nitrogen temperatures <100 K, as exemplified for the dye Atto532 in polyvinyl-alcohol (PVA) (adapted from Giske 2007).

imaging also gives access to further parameters such as cluster brightness (and thus an estimate of the number of molecules per cluster) and the cluster density. An advantage of the STED approach is that it gives a direct image, i.e. cluster parameters such as cluster size can directly be inferred from the recorded image without having to introduce considerable image processing. In the following we will give an example of such a cluster analysis using STED nanoscopy.

We had previously shown that syntaxin 1A, a protein of the soluable N-ethylmaleimide-sensitive factor attachment protein receptors (SNARE) family of receptors which are involved in exocytosis, forms clusters of about 50-60 nm in diameter in the plasma membrane of PC12 cells (Sieber et al. 2006, 2007). An important question remains how these clusters change with increasing expression levels of syntaxin. For this, we created membrane sheets of PC12 cells, after fixation added labelled antibodies against syntaxin (HPC-1 monoclonal antibody and a secondary antibody decorated with the green-emitting dye Atto 532) and imaged their distribution using a custom-built STED nanoscope, as described previously (Sieber et al. 2006). To test the performance of our STED cluster analysis, we artificially created syntaxin clusters with a broad range of sizes and densities, as follows: (1) direct fixed: the cells were fixed directly after the membrane sheet preparation (i.e. after removing the upper part of the cell). (2) Patched 1: the sheets were incubated for 1 h at 37 °C prior to fixation (in 200 µl/CS sonication buffer with 1% BSA). (3) Patched 2: preparation as for patched 1 but with a polyclonal antibody during the 1 h incubation. For cases (2) and (3) we expect an enhanced (artificial) clustering of syntaxin, which should result in larger and brighter but less dense protein assemblies. Figure 5a shows representative STED images together with conventional confocal counterparts (circles) of these three different preparations. Clearly, the clusters can be much more accurately resolved with STED, and their density behaves as expected.

We applied three different statistical approaches to gain accurate values of cluster size, brightness and density. (1) Single cluster analysis (SCA): using an image analysis algorithm for identifying single isolated spots, clusters were separated and their brightness, diameter and the number of clusters per area determined (Willig et al. 2006c). (2) Image correlation analysis (ICS) (Petersen et al. 1986): the calculation and analysis of the autocorrelation function of the number of counts in the image pixels over space allows the determination of cluster size and density. (3) Fluorescence intensity distribution analysis (FIDA) or photon-counting-histogram (PCH) image analysis (Chen et al. 1999; Kask et al. 1999): The assembly and analysis of the histogram of the number of counts in the image pixels establishes relative values of cluster brightness and density (compare Digman et al. 2008; Sergeev et al. 2006). Applied to the STED images of the three different syntaxin preparations (direct fixed, patched 1 and patched 2), the three different analysis approaches (SCA, ICS and FIDA) congruently confirmed larger cluster brightness and sizes and lower densities for the patched compared to the direct fixed preparations, as expected (Fig. 5a). The advantage of ICS and FIDA over SCA is that these two analysis methods may still be applied to images with higher cluster densities, where SCA starts to fail at clearly separating single isolated spots, similar to advantages of fluorescence correlation spectroscopy (FCS) and FIDA over single fluorescence burst analysis in the study of diffusing molecules (e.g. Eggeling et al. 2001b).

With the cluster analysis of the STED images tested, we now studied the formation of syntaxin clusters under different levels of syntaxin expression. Figure 5b depicts a representative STED image and its confocal counterpart of the syntaxin clusters of the membrane sheets of three PC12 cells, each expressing different levels of syntaxin. The preparation and labelling of these sheets was performed as for the direct fixed case. Again, clusters can be much better resolved with STED, and their sizes, brightness and densities accurately determined from subsets of the STED images with ICS and FIDA, even for the highly expressing cell. We used the average



Fig. 5. STED nanoscopy: Cluster analysis. (a) ICS, FIDA and SCA analysis of syntaxin clusters recorded by STED. Upper panels: STED and confocal (circled areas) images of membrane sheets of PC12 cells immunolabeled for syntaxin for three different preparations (directly fixed (left) and patched 1 (middle) and 2 (right)). For the latter two, clustering is reinforced and cluster density decreased, dashed rectangles: analysed area, scale bar: 500 nm. Lower panels: values of cluster density (left), brightness (middle) and size (right) determined for different cells of the different preparations (dots: direct fixed, triangles: patched 1, diamonds: patched 2); left panel: 3D data (black) and projections to different value pairs (blue, green, red) of cluster density by ICS, FIDA and SCA, showing agreeing results by the different analysis techniques. (b) Syntaxin cluster morphology is independent of its expression level. Left panel: STED and confocal (left part) image of three representative membrane sheets generated from PC12 cells expressing different levels of immunolabeled myc syntaxin 1A (cell 1 with a low (probably endogenous) level of syntaxin, and cells 2 and 3 with different overexpression levels, adapted from (Sieber et al. 2006)). Plot of cluster brightness (upper middle), size (lower middle) and density (right) against the expression level (~average pixel brightness) determined by ICS (black) and FIDA (red) from the STED images of different cells, revealing no variation of brightness and size with expression level, and a linear increase of density with expression level.



Fig. 6. Live-cell STED nanoscopy. (*a*) Time-lapse STED imaging of dendritic processes in a living hippocampal slice culture labeled with the fluorescent protein YFP (1 frame every 40 s, adapted from (Nägerl *et al.* 2008)). Arrows indicate a change in shape over time of a cup-like spine head. Scale bar: 1 μ m. (*b*) *In-vivo* STED nanoscopy of a YFP-labeled neuron in the molecular layer of the somatosensory cortex of a mouse (left, inset depicts imaging setup). A maximum intensity projection of dendritic and axonal structures proves a spatial resolution of <70 nm (upper right). Temporal dynamics of spine morphology (lower right). Scale bar: 1 μ m. Adapted from (Berning *et al.* 2012). (*c*) Two-color *in-vivo* STED imaging of astrocytes and neurons offers the possibility to study the influence of the astrocyte on

number of counts per pixel as a relative measure of the expression level in each image subset. As a result we could recognize that the expression level only determined the density but not the size and brightness (i.e. number of molecules) of the clusters. This is an important insight into the characteristics of the protein clusters (Sieber *et al.* 2006, 2007): increasing the concentration of the protein more than ten-fold seems to increase only the number of clusters formed, but not their composition.

2.1.5 Live-cell and in-vivo STED nanoscopy

Due to the aforementioned potential phototoxic effects of the image recording schemes, STED imaging was for long believed to be non-compatible with the study of living cells. However, first images of YFP-labeled endoplasmatic reticulum (ER) and microtubular networks in PtK2 cells proved the opposite (Hein et al. 2008). Especially the use of fast scanning units nowadays allows a straightforward use of STED nanoscopy for the study of the living cell using genetically encoded markers such as fluorescent proteins (Bethge et al. 2013; Eggeling et al. 2009; Hein et al. 2008; Li et al. 2009b; Moneron & Hell, 2009; Morozova et al. 2010; Nägerl et al. 2008; Rankin et al. 2011; Tonnesen et al. 2011; Urban et al. 2011; Willig et al. 2006b), or tagging proteins such as SNAP-, HALO- or CLIP-tags for proteins (Eggeling et al. 2009; Hein et al. 2010; Lukinavicius et al. 2013; Pellett et al. 2011; Schröder et al. 2008) or specifically for actin or microtubule-networks (Lukinavicius et al. 2014), or fluorogen-activating tags (Fitzpatrick et al. 2009) that covalently bind functionalized and membrane-permeable organic dyes. Ranging from the study of the nanoscale dynamics of different cellular molecules, molecular assemblies and structures such as the cytoskeleton, ER, mitochondria, peroxisomes, caveolae, membrane lipids and proteins or vesicles (e.g. Eggeling et al. 2009; Hein et al. 2008, 2010; Moneron & Hell, 2009; Morozova et al. 2010; Muller et al. 2012; Pellett et al. 2011; Rankin et al. 2011; Tonnesen et al. 2011; Westphal et al. 2008; Willig et al. 2011), live-cell STED nanoscopy experiments have also been realized with multi-color detection (Bethge et al. 2013; Pellett et al. 2011; Tonnesen et al. 2011; Willig et al. 2011), and video-rate STED imaging has been pushed to a time resolution of up to 80-200 frames per second. The STED method is therefore the fastest reported superresolution imaging mode to date (Lauterbach et al. 2010a, b; Westphal et al. 2007, 2008).

In an application to neurobiology it was shown that it is possible to image dendritic spines of YFP-positive or organic-dye-filled hippocampal neurons in organotypic slices (Fig. 6*a*) (Ding *et al.* 2009; Nägerl *et al.* 2008; Urban *et al.* 2011). Spines are the dendritic processes that form the postsynaptic part of most excitatory synapses in the mammalian brain. In neurobiology, confocal and two-photon microscopy are widely used to study activity-dependent changes in synaptic morphology by recording time lapse images. However, the diffraction-limited resolution of light microscopy is often inadequate, forcing researchers to complement the live-cell imaging strategy by electron microscopy. Time-lapse STED nanoscopy outperforms confocal microscopy in revealing important structural details and can be used for quantification of morphological parameters, such as the neck width and curvature of the heads of spines, which play critical roles for the function and plasticity of synaptic connections (Urban *et al.* 2011), and can be correlated to

synaptic transmission *in vivo*. Confocal overview (left, $100 \times 100 \mu$ m, scale bar: 10μ m) and STED close-up image (right, scale bar: 500 nm) of the somatosensory cortex in a double transgenic mouse expressing cytosolic EYFP in neurons (TgN(Thy1-EYFP)) and cytosolic GFP in astrocytes (TgN(GFAP-EGFP) GFEC).

199

synaptic signaling (Tonnesen *et al.* 2014). Here, the use of aberration-reducing optics has realized STED imaging deep inside scattering biological tissue with penetration depth of up to 120 μ m (Urban *et al.* 2011).

With STED nanoscopy available to study the living cell it will be exciting to see where it can unravel fundamental details. The imaging of spines is a good example because synaptic function is related to its shape. Super-resolution is necessary because the size of the spine neck is below the diffraction barrier. However, the main function of neurons is information processing by forming connections with their neighbours. This can only be studied where they are embedded in their natural environment and, if possible, in the living animal. Therefore, STED imaging was adapted to resolve neurons and their subtle dynamics in the cerebral cortex of a living mouse with so far unachieved spatial resolution. An upright STED nanoscope was constructed and adapted to the spectroscopic properties of YFP. The somatosensory cortex of the anaesthetised mouse was exposed through a glass-sealed hole in the skull (Berning et al. 2012). Figure 6b shows an image of the setup as well as of dendritic processes within the molecular layer of a TgN (Thy1-YFP) mouse taken by STED. The line profile shows that the smallest structures are <70 nm in diameter, indicating that the resolution is at least of that order. Recording images over 30 min in the living organism revealed that the dendritic spine can undergo morphologic changes and movements on the time scale of minutes. Furthermore, multi-colour STED recordings of the somatosensory cortex in double transgenic mice have the potential to study the influence of astrocytes on synaptic transmission in vivo (Fig. 6c). This shows that STED nanoscopy can be a tool to study brain function or the origin of brain diseases which are related to a structural change.

2.1.6 Lasers for STED

The development of the STED method has significantly benefited from improvements in laser technologies. STED nanoscopy was first realized with pulsed and high-repetition (~80 MHz) Ti: Sa laser systems for stimulated emission and laser diodes for excitation (Klar et al. 2000). This configuration requires the exact timing of both lasers. This is usually accomplished by triggering the laser diodes using custom-built delay electronics, and stretching of the Ti:Sa pulses to 50-300 ps by, for example, glass rods and fibers. The triggering and pulse stretching optimize the timing and efficiency of the stimulated emission relative to the excitation laser pulses, and minimize bias due to polarization effects, jitters in the timing of the excitation and the STED pulses, multiphoton excitation processes, non-linear photobleaching via higher excited electronic states and direct excitation by the STED light (e.g. Dyba & Hell, 2003). While the Ti:Sa laser with wavelengths typically around 700-800 nm may directly be used for STED imaging of dyes emitting in the red spectrum (>600 nm), fluorescent labels such as GFP, YFP, Alexa 488, TMR and similar emit at around 500-590 nm and require STED wavelengths in the range of 590-650 nm. Pulsed laser light in this wavelength range and with average powers of 100-150 mW is delivered by an optical parametric oscillator (OPO) pumped by a Ti:Sa laser (Willig et al. 2006b, c). Such Ti: Sa arrangements are usually rather complex and costly. Nevertheless, the use of Ti:Sa lasers is still one of the preferred options for STED nanoscopy (e.g. Auksorius et al. 2008; Berning et al. 2012; Eggeling et al. 2009; Gould et al. 2011; Lau et al. 2012; Leutenegger et al. 2012; Nägerl et al. 2008; Pellett et al. 2011; Sieber et al. 2006, 2007; Westphal et al. 2008; Willig et al. 2006b, 2006c). Ti: Sa-based laser systems were employed in the first demonstration of two-color STED imaging (Donnert et al. 2007b; Meyer et al. 2008), have been integrated in a commercial system (Clausen et al. 2013; Fitzpatrick et al. 2009; Morozova et al. 2010; Schröder et al. 2008) and have facilitated the D- or T-Rex modality (using a regenerative amplified (Rega) mode-locked Ti: sapphire oscillator) (Donnert *et al.* 2006).

Several options have been presented to reduce complexity and cost of the laser setup. Giving up the wavelength tunability, the use of single-wavelength pico- or nanosecond laser modules allows reducing costs (Westphal et al. 2003), and their high pulse peak powers have facilitated imaging with spatial resolutions of <10-20 nm (Göttfert et al. 2013; Rittweger et al. 2009a). The lowest-cost STED nanoscope to date has been realized by pulsing a 660 nm DVD-diode, i.e. a compact off-the-shelf laser diode (Schrof et al. 2011). Strong and compact single-wavelength lasers are therefore increasingly applied for STED, especially in new commercial STED nanoscopes. Multiple laser lines for STED and excitation can simultaneously be chosen from a pulsed white light or supercontinuum laser, which offers highest flexibility for wavelength optimization, and disburdens from the necessity of synchronizing several lasers (Auksorius et al. 2008; Blom et al. 2011; Wildanger et al. 2008, 2009b). The advent of white light lasers alleviated the setup of multi-color STED instruments (Blom et al. 2012; Bückers et al. 2011; Neumann et al. 2010). In another development, a ~530 nm pico- or nanosecond microchip or fiber-amplified, frequency doubled laser was coupled into a standard single-mode fiber to produce a tunable spectrum of discrete peaks between 530 and 620 nm via stimulated Raman scattering (SRS) (Rankin & Hell, 2009; Rankin et al. 2008). This again allowed a flexible choice of STED laser wavelengths, demonstrating STED imaging with spatial resolution down to 20-30 nm (Rankin & Hell, 2009; Rankin et al. 2008, 2011).

Further simplification of the setup was achieved by realizing STED nanoscopy with continuous-wave (CW) lasers, since no laser-pulse preparation is required (Willig et al. 2007). CW-STED imaging was first realized with strong Argon-Krypton lasers (Willig et al. 2007) or Ti:Sa lasers running in CW mode (Ding et al. 2009; Harke, 2008), but since then it has been shown that it is possible to utilize compact fibre lasers (Bianchini & Diaspro, 2012; Moneron & Hell, 2009; Moneron et al. 2010), diode-pumped solid-state (DPSS) lasers (Honigmann et al. 2012; Mueller et al. 2012) or amplified diode lasers (Honigmann et al. 2013a) at wavelengths between 560 and 765 nm, also on commercial systems (Clausen et al. 2013; Friedemann et al. 2011). However, CW-STED comes with two drawbacks compared to the pulsed STED modality. Firstly, much higher average laser powers have to be applied (Harke, 2008; Willig et al. 2007). This follows from the fact that tightly synchronized trains of excitation and STED pulses, as realized in the pulsed modality, yield an optimized efficiency of stimulated emission: the pulses of the STED beam reach the focal plane virtually simultaneously with or a few picoseconds after the excitation pulses so as to instantly inhibit fluorescence emission from excited molecules. In contrast, in the CW-STED beam implementation the STED intensity and thereby the probability of stimulated de-excitation is lower. As a consequence, to achieve the same fluorescence inhibition efficiency by stimulated emission, $(\ln(2) f \tau)^{-1}$ -fold larger time-averaged powers of the CW than of a pulsed STED laser have to be supplied (with fluorescence lifetime τ of the label and repetition rate f of the pulsed STED modality) (Harke, 2008; Willig et al. 2007). For usual parameters f = 80 MHz and $\tau = 3.5$ ns this amounts to about five-fold larger time-averaged CW powers, for example 800 mW in the CW compared to 160 mW in the pulsed case. Secondly, a further consequence of the CW STED modality is that a non-negligible fraction of the molecules emit fluorescence before having been exposed to much of the STED light, and thus residual fluorescence outside the zero-intensity point of the STED light leads to a pedestal in the effective observation spot, resulting in somewhat lower-contrast images (Leutenegger et al. 2010).

Besides the aforementioned simplifications of the laser arrangements (Kastrup et al. 2010), compact and more robust STED setups have been created by using optimized phase plates

for realizing the focal intensity distribution of the STED laser (Reuss et al. 2010; Wildanger et al. 2009a). Based on diffractive optical elements, a single-beam-path STED nanoscope has been constructed, which includes a phase plate that selectively modulates the STED beam but leaves the excitation beam unchanged. In this configuration the beams are aligned by design and the alignment is hence insensitive to mechanical drift (easySTED) (Wildanger et al. 2009a). Similarly, a birefringent device has been instituted which produces the doughnut-shaped focal spot with suitable polarization for the STED laser while leaving the excitation spot virtually intact, and which in addition can be adapted to reveal, through the resulting fluorescence image, the orientation of fluorophores in the sample, thus directly providing sub-diffraction resolution images of molecular orientation (Reuss et al. 2010). Using Wollaston prisms, a common beamshaping device realized a parallelized STED nanoscope featuring four pairs of scanning excitation and STED beams. This arrangement provides four-fold increased imaging speed of a given sample area, while maintaining the advantages of a single-beam easy STED instrument (Bingen et al. 2011). Further increases in image acquisition speed are achieved by the use of even more parallelized scanning excitation and STED beams, as recently introduced by camera-based detection and wide-field excitation together with well-designed optical patterns for STED (Yang et al. 2014; Bergermann et al. 2015). Spatial light modulators have been applied to auto-align a STED nanoscope (Gould et al. 2013).

Overall, it is to be expected that further developments in laser and optical technology will create more and more compact and less costly systems, and thus will further facilitate the use of STED imaging in day-to-day biophysical and medical research.

2.1.7 Gated CW-STED nanoscopy

The problem of the pedestal inherent to the CW-STED modality can be solved by implementing a pulsed-laser excitation in combination with the CW-STED laser and a time-gated detection scheme (Moffitt et al. 2011; Vicidomini et al. 2011). Time-gated detection is often used in fluorescence microscopy for suppressing background (e.g. Eggeling et al. 2001a; Shera et al. 1990), and, in a pulsed STED scheme, it is well known that photons should be detected after the STED pulse has left (Schrader et al. 1995; Westphal & Hell, 2005), as shown in a recent experiment using time-correlated single photon counting (Auksorius et al. 2008). This is due to the fact that scattered laser light or residual fluorescence signal only occurs during the laser pulses. Time-gated detection also improves the contrast of CW-STED images by selectively suppressing image contents (or spatial frequencies) of low spatial resolution, i.e. the aforementioned pedestal or blurring (Fig. 7) (Moffitt et al. 2011; Vicidomini et al. 2011, 2013). This follows from the fact that fluorescence inhibition is lowest during the duration of the excitation pulse (usually <150 ps), while right afterwards only the CW-STED beam is acting and inhibiting fluorescence emission: the longer it lasts, the more likely it becomes that a fluorophore is switched off, i.e. the spatial resolution not only depends on the intensity of the STED light but also on the time span of the STED beam action (Hell et al. 2003; Vicidomini et al. 2013). This can also be rationalized in the sense that STED reduces the fluorescence lifetime τ of the excited fluorescent state. Ensuring that photons are collected only for delays significantly after the excitation pulse largely suppresses signal from strongly inhibited molecules: fluorescence light is recorded mainly from fluorophores from the zero-intensity doughnut center, where the STED beam is inherently weak (and thus the fluorescence lifetime rather long). Along with the improved image contrast, the selection of high spatial frequencies by the gated detection scheme also allows to apply lower



Fig. 7. gSTED nanoscopy. (a) Principle: the fluorescence lifetime of a fluorophore decreases with increasing STED power as depicted for representative fluorescence lifetime decays for different STED powers (left): using pulsed excitation (blue, Exc) and CW-STED (red) in conjunction with gated detection (detection within the time period ΔT (green) with a time lag T_g (grey) relative to the exciting pulse) favors signal from points of low STED power, i.e. from areas at or close to the intensity zero. (b) Scanning fluorescence intensity (left and upper right) and lifetime (lower right) images of a single fluorophore for confocal diffraction-limited (upper left), CW-STED (intensity: lower left, lifetime: lower right) and gSTED (upper right) recordings (scale bar: 200 nm), and (right panel) intensity line profiles through the middle images, indicating the removal of the pedestal of the CW-STED recordings (black) by the gated detection (gSTED, red). (c) Confocal and gSTED images (right: magnification of central area marked by the dashed white box) of keratin fused to the fluorescent protein citrine in a living PtK2 cell with low CW STED laser power. Scale bar: 1 µm. Adapted from (Vicidomini *et al.* 2011).

CW-STED powers compared to the non-gated CW-STED scheme to be able to similarly discern alike features (Vicidomini *et al.* 2011). This, and the fact that CW in comparison to pulsed beams may be less prone to induce phototoxic multiphoton processes, reduces light-induced stress on the sample. It is worth noting that these improvements always come with a reduction in signal, since the gating suppresses valuable signal as well (Vicidomini *et al.* 2013). Gated-STED (gSTED) nanoscopy has been realized for different fluorophores and in living cells, and has now been incorporated into a commercial system, allowing the recording of live-cell images with sub-diffraction spatial resolution at moderate CW STED powers <80 mW (Clausen *et al.* 2013; Vicidomini *et al.* 2011). Data acquisition for gSTED has been demonstrated by offline processing of time-correlated single-photon counting data, or in real-time using a fast electronic gate. As for CW-STED, gSTED nanoscopy can be realized with compact CW lasers, which are nowadays available at various wavelengths (Honigmann *et al.* 2012, 2013a; Mueller, 2012) and show improved performance with reduced noise levels (Hernandez *et al.* 2014a). Of all current STED modalities, gSTED provides the sharpest STED images at the lowest peak laser powers.

Besides the aforementioned improvement in image contrast, gated detection also allows to specifically suppress background signal. On one hand, discarding signal during the excitation pulse (as done for gSTED) reduces scattering signal from the excitation laser (e.g. Eggeling *et al.* 2001a; Shera *et al.* 1990). On the other hand, the rejection of signal for time delays after the excitation pulse much longer than the fluorescence lifetime τ of the fluorophore specifically suppresses continuous background signal such as fluorescence light excited by the CW-STED laser or detector noise. This allows using wavelengths of the STED laser closer to the fluorescence emission maximum, which reduces the required laser powers (Vicidomini *et al.* 2012; Hernandez *et al.* 2014b). Consequently, gated detection introduces high flexibility, especially if the acquired data is postprocessed by software. This will not only allow an optimization of the image contrast, but also the investigation of the very same data for different image contrasts, i.e. for different gating positions (Vicidomini *et al.* 2011).

2.1.8 STED-FCS: nanoscale single-molecule dynamics

The ongoing quest to study molecular dynamics not in the ensemble but at the molecular level calls for measurements both of molecular numbers and, crucially, with access to molecular spatial scales. Compared to ensemble measurements, studies at the single-molecule level reach a much increased sensitivity as they may reveal heterogeneities hidden in the ensemble and disclose deviations from the ergodic theorem (i.e. a time-averaged ensemble measurement may not be the same as the ensemble average of a large number of single-molecule measurements). Fluorescence microscopy has reached single-molecule detection sensitivity (Moerner & Kador, 1989; Orrit & Bernard, 1990; Shera et al. 1990; Weiss, 1999; Zander et al. 2002), and studies of single-molecule dynamics have given many new, detailed insights into physical, chemical and biological problems (e.g. Lord et al. 2010; Moerner, 2007). In this context, statistical analysis tools such as Fluorescence Correlation Spectroscopy (FCS) (Ehrenberg & Rigler, 1974; Haustein & Schwille, 2003; Magde et al. 1972) or photon-counting histogram analysis (PCH) (Chen et al. 1999) and Fluorescence Intensity Distribution Analysis (FIDA) (Kask et al. 1999) have been extremely helpful. However, further insights into a lot of (single-molecule) dynamical processes have been again impeded by the limited spatial resolution of common diffraction-limited fluorescence microscopy. 1) The concentration of fluorescently labeled molecules has to be very low (<nM) to reach the single-molecule level with conventional confocal observation volumes - a concentration which is often far below that of endogenous (biological) conditions. In contrast to performing measurements in zero-mode waveguides (Leutenegger et al. 2006; Levene et al. 2003; Wenger et al. 2007), or to photobleach (Moertelmaier et al. 2005) or switch off (Eggeling et al. 2007) large parts of the ensemble, the most obvious way to handle larger, endogenous concentrations would be to lower the observation spot's length scale (its size) (Blom et al. 2006; Kastrup et al. 2005; Weiss, 2000). 2) The conventional confocal observation spot usually averages over details of nanoscale molecular dynamics. For example, strongly localized trapping cannot directly be distinguished from slow but regular molecular diffusion (Eggeling et al. 2009). In the case of confocal FCS observations of molecular membrane dynamics, such discrimination has indirectly been realized, for example, by searching for anomalies in diffusion (Schwille et al. 1999), by extrapolating to the nanoscopic case (Wawrezinieck et al. 2005), or by probing in the near-field on nanostructures or -holes (Leutenegger et al. 2006; Manzo et al. 2011; Wenger et al. 2007). However, very direct measurements at the length scale of interest (i.e. observing diffusion dynamics through sub-diffraction-sized far-field observation spots) deliver much more reliable and model-independent results about nanoscopic details of molecular diffusion and interactions and, at the same time, allow indirect methods to access even smaller length scales.

In an attempt to access smaller length scales, non-invasive far-field microscopy was thus combined with single-particle tracking (SPT), utilizing the high spatial localization precision of down to the 1-nanometer level for bright marker particles (Geerts *et al.* 1987; Kusumi *et al.* 2005; Schutz *et al.* 1997; Sheetz *et al.* 1989; Yildiz *et al.* 2003). Yet this introduces other restrictions: to reach the desired spatial localization precision, SPT often applies bright but rather large signal markers, which potentially influence the system under study (Clausen & Lagerholm, 2011). When using conventional fluorophore labeling the temporal resolution is lower. And while important insights can be gained in carefully optimized SPT experiments, for example if the full spatiotemporal resolution afforded by the fluorophore photon budget is harnessed in fast molecular tracking schemes (Sahl *et al.* 2010, 2014), the amount of data to be gathered for an accurate statement on an average molecular behavior is higher for SPT compared to FCS. In addition to the concentration issue, the stochastic sampling concomitant with SPT yields low statistics and random coverage from a single measurement only.

A remedy for these limitations is the combination of FCS with the STED principle (Eggeling et al. 2009; Kastrup et al. 2005; Ringemann et al. 2009). STED-FCS delivers high temporal and spatial resolution together with a high degree of statistical averaging. The most straightforward parameters measured with FCS are the average transit time τ_D of the fluorescent molecules through the observation area/volume and the average number N of fluorescing molecules in the observation volume. One expects both τ_D and N to decrease with the confinement of the observation spot, i.e. with the STED power. Figure 8a shows exemplarily FCS data for fluorophores in solution exhibiting 3D free diffusion. While the expected decrease of τ_D is observed, N does not decrease as strongly, and even increases for high STED powers due to a reduced signal-to-background ratio (SBR) (Ringemann et al. 2009). The low SBR is caused by noninhibited, low-brightness fluorescence signals from out-of-plane volume shells. Contributions of the latter to the overall signal grow relative to the declining fluorescence signal from the more and more confined observation spot (Fig. 8a) (Ringemann et al. 2009). This degradation in SBR has on the one hand been observed for confinement along x/y only, but also for confinement along z or along all three spatial directions (Kastrup et al. 2005; Ringemann et al. 2009), even when using two-photon excitation (Moneron & Hell, 2009) or two opposing objectives in an iso-STED arrangement (Schmidt *et al.* 2008). The biased values of N can straightforwardly be corrected for by, for example, a combined or global FCS-FIDA analysis (Fig. 8a, right) (Ringemann et al. 2009). Therefore, while such reduction effects on the SBR might limit the sensitivity of STED-FCS experiments for 3D diffusion, it does not necessarily preclude such measurements, such as assessments of nanoscale molecular diffusion dynamics inside living cells.

The above out-of-plane background vanishes for 2D diffusion measurements such as within membranes, where no out-of-plane signal is present (Fig. 8b). Here, both τ_D and N decrease with increasing STED power, i.e. with the confinement of the observation area, as expected (Fig. δc) (Ringemann et al. 2009). Recently, STED-FCS has also been combined with evanescent (TIRF) illumination to reject out-of-plane background (Leutenegger et al. 2012). However, the maximum achievable resolution of the TIRF-STED-FCS setup was only 50-60 nm due to side lobes inherent to the confocal TIRF illumination scheme. An important observation is that the STED mode reduces the transit times but hardly the detected fluorescence brightness (if the intensity zero of the STED focus is properly aligned, i.e. it really is close to zero). In Fig. 8d, the detected photon count-rate of a typical molecular trace of fluorescent lipids in multi-lamellar membrane layers peaks at 300-400 kHz which enables the analysis of single-molecule STED data at a good signal-to-noise ratio. Most importantly, signatures of single-molecule transits are only observable for small, sub-diffraction sized spots as created by STED, while the concentration is too high for conventional confocal recordings (Fig. 8d). Therefore, STED allows accurate single-molecule measurements on the cellular plasma membrane of living cells, and thus is a powerful tool for shedding new light on long-standing biological questions.



Fig. 8. STED-FCS. (a) STED-FCS analysis of free 3D-diffusion of the organic dye Atto647N in aqueous solution. Representative correlation data (left panels, left: normalized amplitudes, right: original data) for confocal (black) and STED recordings (open dots) and (right panel) relative values of transit time τ_D (black), particle number N (original open dots, background-corrected grey triangles), and signal fraction of apparent background (grey crosses) determined from FCS and FIDA data recorded for increasing power of the doughnut-shaped (inset left) STED laser. The size reduction of the observation spot by increasing the STED power shortens the dye's transit time, but also introduces an increasing contribution of apparent un-depleted low-brightness background, which introduces noise and dampens the FCS data's amplitude and thus results in an apparent increase of N, which can be corrected for by a global FCS-FIDA analysis. (b) Relative apparent background for the STED-FCS recordings for two different pinhole sizes (decrease from left to right), and for a fluorescent lipid analog diffusing in a multi-lamellar membrane. Reduction of the pinhole size reduces un-depleted out-of-plane low-brightness fluorescence signal (apparent background), which diminishes further when measuring two-dimensional diffusion in membranes, where out-of-plane signal is absent. (c) STED-FCS analysis of free 2D-diffusion of a fluorescent lipid analog in a multi-lamellar membrane. Representative correlation data (left panels, left: normalized amplitudes, right: original data) for confocal (black) and STED recordings (open dots) and (right panel) relative values of transit time τ_D (black) and particle number N (original open dots, background-corrected grey triangles) determined from FCS and FIDA data recorded for increasing power of the doughnut-shaped STED laser. The confinement of the observation spot by increasing the STED power reduces both τ_D and N, without an influence by out-of-plane signal contributions. (d) STED allows single-molecule observations at high concentrations. Fluorescence signal over time for the same concentration of a fluorescent lipid analog diffusing in a multi-lamellar membrane indicates diffusion of single molecules only for the STED (right) but not for the confocal (left) recordings. Adapted from (Ringemann et al. 2009).

2.1.9 STED-FCS: live-cell membrane dynamics

Many membrane-associated processes such as signaling events are considered to be closely related to cholesterol-mediated interactions of some lipids such as sphingolipids (Brown & London, 2000; Fielding, 2006; Hanzal-Bayer & Hancock, 2007; Jacobson *et al.* 2007; Simons & Ikonen, 1997). In contrast to phosphoglycerolipids, these lipids are assumed to form molecular complexes or integrate, assisted by cholesterol, into <200 nm sized lipid nanodomains, usually denoted 'rafts' (Simons & Ikonen, 1997). These interactions may disturb the diffusion of lipids and proteins in the plasma membrane, and on the other hand may compartmentalize cellular signaling (Pike, 2006). Although several experiments indicate their existence, such complexes and/or lipid 'rafts' remained controversial due to the lack of suitable techniques for detecting these small-sized objects in living cells (Hancock, 2006; Jacobson *et al.* 2007; Lommerse *et al.* 2004; Munro, 2003; Shaw, 2006). A common problem is once again that the <200 nm sized domains cannot be resolved by conventional confocal microscopes, and thus common fluorescence recovery after photobleaching (Feder *et al.* 1996; Yechiel & Edidin, 1987) or confocal FCS measurements (Fahey *et al.* 1977; Schwille *et al.* 1999; Wawrezinieck *et al.* 2005) average over nanoscale details of molecular diffusion. STED nanoscopy opens up a new avenue to elucidate lipid diffusion.

Figure 9 shows FCS analysis of lipid diffusion in the plasma membrane of living mammalian cells recorded with a STED nanoscope. The unique feature of the STED method to continuously downscale the size of the observation area with laser intensity and/or gated detection allows the determination of the average transit time τ_D for different diameters d of the observation, revealing different modes of diffusion (Fig. 9d) (Eggeling et al. 2009; He & Marguet, 2011; Ruprecht et al. 2011; Wawrezinieck et al. 2005). Unlike the confocal recordings, the STED-FCS data reveal distinct differences between fluorescent phosphoglycerolipid (PE) and sphingolipid (SM) analogs. Most importantly, it is revealed that while the PE lipids diffuse freely, the SM lipids diffuse heterogeneously on small spatial scales, being transiently (~10-20 ms) trapped in cholesterol-mediated molecular complexes with relatively slow-moving or immobilized binding partners. Such previously inaccessible molecular details depict how the noninvasive optical recording of molecular time traces and fluctuation data in tunable nanoscale domains is a powerful new approach to study the dynamics of biomolecules in living cells. Recent work could not detect any correlation between the nanoscale trapping as observed by STED-FCS in living cells and partitioning characteristics of the labeled lipids into liquid ordered domains of phase separated model membranes (which is often assumed as a physical model of lipid 'rafts') (Fig. 9f) (Eggeling, 2012; Mueller et al. 2011, 2013; Sezgin et al. 2012; Honigmann et al. 2014). Rather, the trapping characteristics and the dependence on cholesterol are highly dependent on the molecular structure of the lipid (however not on the dye label or the labeling position), identifying the ceramide or sphingosine group close to the water-lipid interface as well as the lipid's headgroup as the driving forces for molecular interactions (Fig. 9g) (Mueller et al. 2011). Therefore, we may recall our previous statement (Eggeling, 2012; Mueller et al. 2011, 2013), 'that the observed transient trapping with its rather strong binding to other membrane constituents follows a different molecular mechanism than that of the weak interactions responsible for the formation of ordered phases in model membranes. [...] If one pictures the STED-FCS observations in the context of lipid 'rafts', one may support a current view that (sphingo)lipid rafts may establish fluctuating nanoscale assemblies of sphingolipid, cholesterol and proteins that can be stabilized to coalesce, forming platforms that function in membrane signaling and trafficking (Lingwood & Simons, 2010). Here, the STED-FCS experiments may highlight the fluctuating nanoscale assemblies, which then seem to be highly diverse and strongly depending on the lipid structure. It remains to be shown whether these fluctuating nanoscale assemblies may be stabilized to coalesce to maybe more tightly packed domains (Joly, 2004; Lingwood & Simons, 2010). A fluorescent lipid analog that partitions



Fig. 9. STED-FCS analysis of lipid plasma membrane diffusion. (a) Lipids and proteins are heterogeneously distributed in the cellular plasma membrane, stemming from often cholesterol-assisted lipid-protein interactions (which may be the basis for the coalescence of transient signaling platforms, denoted membrane domains or lipid 'rafts', i.e. spatially confined molecular assemblies of different lipids and proteins which are essential for a cellular signaling event), an asymmetric molecular distribution to the inner and outer leaflet of the bilayer, the underlying cytoskeleton (which is membrane-anchored via proteins), and from membrane curvature and pits. Adapted from (Lingwood & Simons, 2010). (b) Structures of the fluorescent lipid analogs phosphoethanolamine (PE) and sphingomyelin (SM), both tagged with the organic dye Atto647N. Grey shaded area: ceramide or sphingosine group of the SM lipid. (c) Representative confocal and STED (observation diameter d = 40 nm) FCS data of PE (red), SM (black) and SM after cholesterol depletion by Cholesterol Oxidase (grey, SM+COase). The SM STED-FCS data can only be described by anomalous diffusion, revealing cholesterol-assisted hindered diffusion of the SM lipid analog. (d) The dependence of the transit time τ_D for different sub-diffraction sized observation areas $\sim d^2$ (as tuned by the STED laser power) shows an almost free diffusion (linear dependence, dark grey line diffusion coefficient $0.5 \,\mu m^2/s$) for PE (red squares) and SM after cholesterol depletion (open circles), and a hindered diffusion (non-linear dependence) for SM (grey circles). The minimal change of τ_D for very small observation areas (grey horizontal line) and Monte-Carlo simulations indicate that the hindrance in diffusion is caused by transient complexes with either relatively slow-moving or immobilized membrane molecules (red dotted line) and not by incorporation into ≥ 20 nm large domains, where diffusion is slowed down (green dotted line). The direct observation of these transient interactions is impossible with the large diffraction-limited confocal observation area (grey shaded area). (e) Schematic drawing of normal free (red) and hindered SM diffusion (blue, dots: points of interactions or complexes). (f) Comparison of live-cell and model membrane data. Phase separation into liquid-disordered (Ld) and liquid-ordered (Lo) domains of a model membrane bilayer composed of a ternary mixture: both the fluorescent PE and SM lipid analogs hardly enter the Lo phase (upper panel: confocal scanning fluorescence image, black: low signal, white: high signal, adapted from (Mueller et al. 2011)). Partitioning in model membranes and trapping characteristics observed by STED-FCS on live-cell plasma membranes are not correlated (lower panel): Trapping time (red, left axis, live-cell) and

208

into the liquid ordered phase of model membranes (like its natural counterpart) may be able to report on this coalescence.' Recently, such a lipid analog has successfully been tested in STED experiments (Honigmann *et al.* 2013b), and initial experiments in live-cell membranes indicated no difference to the liquid-disordered partitioning of fluorescent lipid analogs (Sezgin *et al.* 2012; Honigmann *et al.* 2014). Caution has to be taken when designating any lipid-based interaction or heterogeneous organization as a 'raft', since the basis of these may be highly diverse (Eggeling, 2012; Mueller *et al.* 2011, 2013; Sezgin *et al.* 2012).

2.2 Generalization: STED, GSD, SSIM/SPEM and RESOLFT

Stimulated emission is only one way to reversibly transfer molecules between states of different fluorescence properties. Similarly, other state transitions may be applied for sub-diffraction optical microscopy (nanoscopy). The key is to identify a pair of ON- and OFF-states between which at least one transition can be driven by light (Hell, 2004, 2009b; Hell *et al.* 2003). The different mechanisms used so far are summarized in Fig. 10*a*; they most significantly differ in the molecular states involved, the required laser intensities and the choice of label.

2.2.1 STED: stimulated emission

STED requires rather large laser intensities in order to induce de-excitation from S_1 more efficiently than the spontaneous decay (usually around 2–4 ns). Therefore, the threshold or saturation intensities required to inhibit half of the fluorescence are in the range of $I_S = 1-10$ MW/ cm² (Fig. 10*a*). As mentioned in Section 2.1.6, a preferred implementation of STED is the use of pulsed lasers supplying high peak intensities. This STED modality provides an exponential, i.e. a very steep, dependence of the fluorescence inhibition on the STED laser, realizing a very sharp confinement of fluorescence emission (Harke *et al.* 2008a; Hell, 2009b). Inhibition of fluorescence by stimulated emission can be realized with basically any fluorophore. The spatial resolution of the STED concept is in principle limited only by the size of the quantum system to be imaged, i.e. by the molecule. (Section 2.3).

2.2.2 GSD: transient dark state shelving

GSD imaging was the second far-field nanoscopy concept concretely laid out (Hell & Kroug, 1995). In GSD, inhibition of fluorescence emission is realized by transiently shelving the fluorophore in a metastable dark state such as the triplet (Kasha, 1950) or other dark (redox) states populated therefrom (e.g. Vogelsang *et al.* 2008; Zondervan *et al.* 2003). Since the lifetime of the involved dark states is usually much longer (μ s to s) than that of the S_1 (ns), GSD allows using

fraction of signal in Lo phase (grey, right axis, model membranes) of PE and SM (adapted from Sezgin *et al.* 2012). (g) STED-FCS analysis of the plasma membrane diffusion of different fluorescent lipid analogs, revealing lipid-specific interactions and independence on dye and label position. Average transit time τ_D for confocal ($d \approx 250$ nm, upper panel) and STED ($d \approx 40$ nm, lower panel) recordings of the Atto647N-or Atto532-labeled phosphoethanolamine (PE: head group and PE1: acyl-chain labeled), sphingomyelin (SM: acyl-chain and CPE: head-group labeled), ganglioside GM1 (GM1: acyl-chain, GM1[#]: head-group and GM1^{##}: chain addition), and of an Atto647N-tagged transfected GPI-anchor. The meshed bars in the lower panel indicate the values of τ_D determined after cholesterol depletion by COase treatment. Error bars result from averaging over more than thirty measurements. No dependence of the STED-FCS data on the dye-label position has been observed, apart from using the dye Atto532 on the lipid's acyl chain, which accelerates diffusion and lowers trapping probability. Adapted from (Eggeling *et al.* 2009).



Fig. 10. Generalization of coordinate-targeted (deterministic) nanoscopy: the RESOLFT concept. (*a*) Different molecular states and transitions can be applied to reversibly inhibit fluorescence for coordinate-targeted nanoscopy ranging from STED (stimulated emission), over GSD (metastable dark states), SPEM/SSIM/GSD (ground state depletion by saturated excitation) to RESOLFT (e.g. photoswitchable fluorophores, different conformational states): acronyms (left), molecular states (middle) with energy level diagram of a fluorophore (ground S_0 , excited S_1 and dark states) and transitions for ON (left middle) and OFF (right middle) direction (middle: ON-OFF transitions with excitation (Exc), fluorescence (Flu), stimulated emission (STED), metastable dark states (with crossing probability Φ_D and lifetime τ_D), bright (ON) and dark (OFF) conformational states (with on- and off-switching light and potential spontaneous transition lifetime τ) and intensity I of the corresponding lasers), intensity I dependence of switching with threshold intensities I_S (right), and approximate values of I_S . Adapted

much lower intensities than STED, in the range of 100-300 kW/cm² (Fig. 10b) (Bretschneider et al. 2007; Hell & Kroug, 1995). Since both dark state shelving and fluorescence excitation occur via S_1 , i.e. most efficiently by the same laser line, a pump-probe scheme has been introduced in the experimental realization of GSD nanoscopy (Bretschneider et al. 2007). Here, the pump beam is arranged with one or several zero intensity points (such as the doughnut-shaped intensity distribution) and essentially prepares the observation area by restricting molecules that are left in the bright S_0 - S_1 system to sub-diffraction sized volumes. A subsequent conventional, diffractionlimited fluorescence excitation beam probes these residual bright molecules. Super-resolution images are again realized by scanning the resulting nanoscopic observation spot over the sample, as depicted for immunolabeled SNAP-25 protein clusters on a cell membrane in Fig. 10h. The silenced fluorophores have to return to the S_0 - S_1 system before each scanning step, which puts a lower limit on the image acquisition time (e.g. pixel dwell times of 60 ms in Fig. 10b). The implementation of the GSD concept is further challenged by the increased involvement of the dark states in photobleaching. Therefore, the experimental realization of GSD had to discover conditions for which (1) the dark state lifetime is within a reasonable range (1-100 ms) to minimize laser intensity for optical pumping but also to reduce pixel dwell and thus image acquisition times, and (2) photobleaching is low enough to allow a reasonable number of pump-probe cycles per fluorophore (Bretschneider et al. 2007). This has, for example, been realized using special mounting media (Bretschneider et al. 2007) or nitrogen temperatures (Schwentker, 2007) increasing both the dark state lifetime as well as the photostability. On the other hand, it was shown that the addition of UV or IR light after probing may shorten the return time to the S_0 - S_1 system by reverse dark state/intersystem crossing (Giske, 2007; Ringemann et al. 2008), introducing an additional degree of freedom for the optimization of GSD data acquisition (Schwentker, 2007). A large list of fluorophores was introduced as potential labels for GSD nanoscopy (Bretschneider et al. 2007). Recently, GSD was realized with NV centers in diamond, featuring down to 12 nm spatial resolution (compare Fig. 11b) (Han et al. 2010). GSD nanoscopy will benefit from the

from (Hell, 2007). (b) GSD nanoscopy: (left) dependence of the inhibition of fluorescence on the excitation laser intensity, which is based on transient shelving into a metastable dark state (inset). (Middle) Pump-probe principle with pump light inducing dark state transitions and probe light exciting fluorescence of those molecules that are left in the bright state, resulting in a sub-diffraction observation spot. (Right) GSD and confocal (upper marked areas) images of immunolabeled SNAP-25 protein clusters on a fixed cell membrane (left) and an organic dye with a high triplet intersystem crossing rate, filling up a grooved nanostructure (right). Scale bars: 500 nm. Adapted from (Bretschneider et al. 2007). (c) RESOLFT nanoscopy using the reversibly photoswitchable protein rsGFP. (Left) rsGFP fulfills all requirements for coordinate-targeted nanoscopy: fast photoswitching (upper panel: fluorescence signal following repetitive on-off switching (red) with comparison to the RSFP Dronpa (blue)) with low switching fatigue (lower left panel: 'on' fluorescence versus number of on-off switching cycle (red) and comparison to Dronpa (blue)), and a long lifetime of the 'off' state (lower right panel: spontaneous temporal recovery of fluorescence after off-switching with half of the fluorescence recovered after 23 min). (Right) RESOLFT and confocal (lower or upper left corner) of an Escherichia coli bacterium expressing rsGFP-MreB (left) and a live mammalian cell expressing keratin-19-rsGFP (right). Scale bar: 1 µm. Adapted from (Grotjohann et al. 2011). (d) RESOLFT nanoscopy with more than hundred-thousand doughnuts. (Left) By overlapping the diffraction pattern generated by two perpendicularly arranged gratings, an illumination pattern of the switch-off light is generated, which features a large number of intensity zeros (PBS: polarization beam-splitter, Obj: objective lens) and which results in multiple simultaneous scanning points, whose dimension decreases with increasing intensity of the switch-off light (middle). (Right) Conventional (left part) and RESOLFT (right part) wide-field images of keratin 19-rsEGFP(N205S) in live mammalian cells (scale bar: 1 µm, adapted from (Chmyrov et al. 2013)).



Fig. 11. The resolution of coordinate-targeted nanoscopy is in principle limited only by the size of the quantum system (molecule or emitter) to be distinguished: imaging nitrogen-vacancy (NV) centers in diamond. (a) STED imaging of NV centers. (Upper left) NV centers (inset: molecular structure) are a nearly perfect switch: fluorescence inhibition versus STED laser intensity. (Upper middle) STED images of single isolated NV centers in bulk diamond (inset: scanning image, with confocal counterpart in the upper left corner) reveal down to 6 nm spatial resolution (or diameters of the observation area) with increasing STED laser intensity. Scale bar: 100 nm. (Upper right) Scanning image of a single isolated NV center (fast axis along y) with STED laser switched on only in the marked area, exemplifying the vast increase in spatial resolution from confocal 225 nm down to 8 nm. Scale bar: 100 nm. (Lower left) Repetitive STED images of single isolated NV centers in diamond (frame number in the upper right corner), showing the ultimate stability of these emitters. Scale bar: 200 nm. (Lower right) Confocal (left) and STED (right) images of 35 nm large NV-containing nanodiamonds. Scale bar: 100 nm. Adapted from (Han et al. 2009; Rittweger et al. 2009a). (b, c) GSD nanoscopy of NV centers. (b) GSD by reversible laser-driven transitions into a long-lived dark state. (Upper panel) Energy level diagram of an NV center with ground ³A, excited ³E and dark states, transitions driven by red (excitation Exc and OFF-switching) and blue light (ON-switching), spontaneous fluorescence emission (Flu) and dark state return (dashed line, >100 s lifetime). (Lower panel) Spatial resolution versus power of the red laser driving the OFF transition, as determined by scanning images of isolated NV centers and respective intensity line profiles (insets, scale bar is 100 nm). Adapted from (Han et al. 2010). (c) GSD by saturated excitation. (Upper left panel) Energy level diagram of an NV center with ³A (OFF) and ³E (ON) states, and excitation by green light (Exc) and spontaneous fluorescence emission (Flu). (Upper right panel) Saturation of fluorescence signal: dependence of fluorescence signal of a single NV center on the power of the excitation laser. (Middle panel) Experimental setup with green 532 nm excitation laser, phase plate (PM) generating the doughnut-shaped intensity distribution (inset), dichroic mirror (DC), fluorescence signal (orange), and detector (Det). (Lower panels) Scanning images of a single NV center for increasing intensity of the excitation laser (left to right), depicting the confinement of the area in which no fluorescence is elicited. Adapted from (Rittweger et al. 2009b). Scale bar: 50 nm.

exploration of fluorophores and mounting or buffer conditions which realize large and controllable dark-state populations (Kolmakov *et al.* 2010a; Vogelsang *et al.* 2008). For example, special redox buffers have allowed the controlled and efficient photoswitching of conventional organic dyes by promoting the population of their dark states as well as their photostability (Vogelsang *et al.* 2008). Figure 10*b* on the other hand depicts GSD imaging in aqueous environment, where fluorophores usually exhibit dark state lifetimes in the range of μ s. The image has been recorded with an organic dye which is characterized by a high intersystem crossing rate, i.e. a high triplet state yield (Chmyrov *et al.* 2008) and using somewhat larger laser intensities (Bretschneider *et al.* 2007). The use of dark states that are normally involved in bleaching pathways has however so far hampered the practicability of GSD for (live-) cell nanoscopy.

2.2.3 SPEM/SSIM: GSD via saturated excitation

Saturated Patterned Excitation Microscopy (SPEM) (Heintzmann et al. 2002) or Saturated Structured Illumination Microscopy (SSIM) (Gustafsson, 2005) also depletes the ground state, as in GSD. It differs from GSD (or STED) in that it confines the dark state S_0 rather than the emitting state S_1 , thus creating sub-diffraction sized dark regions that are surrounded by bright areas. Scanning of such spots consequently produces 'negative data' and the final 'positive' images have to be reconstructed computationally (Gustafsson, 2005). The intensities necessary to create dark regions of sub-diffraction sized extent, i.e. to efficiently deplete S_0 and saturate the population of S_1 are of similar magnitude as in the STED concept, because both rely on the same states. Introduced theoretically a decade ago and also promising in principle molecular resolution (Heintzmann et al. 2002), SPEM/SSIM has so far experimentally been realized once with fluorescent beads, displaying a lateral resolution of 50 nm (Gustafsson, 2005). The limitations of this technique result from the use of very large excitation intensities, which cause enhanced photobleaching from higher excited (dark) states, as well as an optically induced depopulation of dark states, which prevents saturation of the S_1 (Giske, 2007; Ringemann et al. 2008; Schwentker, 2007). The aforementioned SPEM/SSIM experiment therefore implemented a D-/T-Rex-like illumination scheme, avoiding significant populations of long-lived dark states using a 5 kHz laser for excitation (Gustafsson, 2005). In other work, saturated excitation of ultrastable NV centers in diamond yielded single-spot scanning GSD images with a spatial resolution of <10 nm (compare Fig. 11c) (Han et al. 2012; Rittweger et al. 2009b).

2.2.4 RESOLFT: reversible photoswitchable labels

All of the above approaches may be summarized under a general name, RESOLFT nanoscopy (Hell, 2004; Hell *et al.* 2003, 2004). The realization of STED or GSD led to the consideration of molecular switches between states of very long lifetimes (even longer than the metastable dark states introduced in the GSD concept). The advantage is obvious: the utilization of states with very long lifetimes τ (or even the elimination of spontaneous transitions) would allow applying very low laser intensities for driving a fluorophore to a certain state (Hell *et al.* 2003). Reversible photoswitching between states with very long τ can be realized through changes in molecular conformations. A prominent example is photoinduced cis–trans isomerization involving fluorescent and dark (or non-detectable) isomeric counterparts, which can be switched back and forth by light of different wavelengths. Cis–trans isomerization is for example known for cyanine dyes. The lifetime of these states for cyanines is however $\tau < \mu$ s in aqueous solution (Widengren & Schwille, 2000), impeding the move to very low intensities. Isomeric states may

be stabilized (and τ prolonged) for other molecules such as reversible switchable fluorescent proteins (RSFPs) or spiro-compounds, and/or by fixation in rigid environments (Ando et al. 2004; Bossi et al. 2006; Dickson et al. 1997; Feringa, 2001; Irie et al. 2002; Lukyanov et al. 2000; Sakata et al. 2005). In RSFPs the differently isomerized states are usually stabilized by the protein barrel surrounding the chromophore (and often involve differently protonated states) (Andresen et al. 2005, 2007; Habuchi et al. 2006; Wilmann et al. 2005). It was therefore an RSFP, asFP595 (Lukyanov et al. 2000), that was first used to experimentally prove the viability of the general RESOLFT concept in 2005 (Hofmann et al. 2005), asFP595 can be reversibly switched between a dark trans and a bright cis state with light of 405-460 and 560 nm, respectively, and the thermal lifetimes of $\tau > ms$ in aqueous solution enabled for the first time the use of ultra-low intensities (<kW/cm²) for super-resolution microscopy. Similar sub-diffraction images were realized when using other RSFPs such as Dronpa (Ando et al. 2004; Bock, 2008; Dedecker et al. 2007; Hofmann, 2007), or when switching between an open and a closed form of a photochromic organic compound of the furyl-fulgides family in a polymeric matrix (Bossi et al. 2006). In the latter, the difference in fluorescence signal between the two forms had been realized by the photochromic compound serving as a reversible switchable energy acceptor for a fluorescent compound. Unfortunately, the uses of both asFP595 and the photochromic organic compound for cellular RESOLFT nanoscopy were limited. First of all, specific labeling with either was not feasible, since asFP595 was only present in a tetrameric form, and the organic compound could not successfully be functionalized. Furthermore, under the final imaging conditions the signal could not be switched off completely due to cross-talk between laser lines (e.g. >30% of the ON-state fluorescence in the case of asFP595), requiring computational post-processing of the recorded image (through, e.g. deconvolution) in order to fully extract the sub-diffraction image contents - a procedure which can be prone to noise and biases. In addition, the switching speed was rather slow, entailing scanning dwell times of >100 ms. Finally, and most importantly, both labels exhibited considerable switching fatigue. Therefore, deliberate screening for fast and high-contrast switching monomeric RSFPs which should hardly show spontaneous decay of the involved states and, most importantly, survive >1000 and more photoswitching cycles was performed (Stiel et al. 2007). This screen ended in a RSFP variant of GFP (rsGFP: reversible switchable GFP), and its use in RESOLFT nanoscopy realized down to 40 nm spatial resolution in live-cell imaging (Grotjohann et al. 2011). Similarly, the RSFP Dreiklang was created and applied to RESOLFT imaging, where suitable wavelengths for on and off switching and fluorescence excitation were completely disentangled, minimizing any action cross-talk (Brakemann et al. 2011). Applying laser intensities of only 1 kW/cm², the RESOLFT concept applying RSFPs is highly suited for live-cell applications. RESOLFT nanoscopy has in the meantime enabled the recording of live-cell dynamics even in 3D (Testa et al. 2012). Further improvements have come with the development of RSFPs with faster photoswitching times and decreased switching fatigue (Grotjohann et al. 2012), as well as with additional emission wavelength ranges (Stiel et al. 2008) for multi-color observations. Phototoxic effects of the (often UV) photoswitching light may be avoided by the use of IR light in a two-photon mode (Denk, 1996).

2.2.5 Parallelization

The image acquisition in coordinate-targeted nanoscopy can be accelerated significantly by employing multiple observation spots simultaneously. As already outlined in Section 2.1.6, this has been realized in STED nanoscopy with four parallel scanning spots using Wollaston prisms (Bingen et al. 2011), or 100 or even 2000 parallel spots using optical standing wave patterns (Yang et al. 2014; Bergermann et al. 2015). Unfortunately, the laser intensities required for STED are still too high to allow further parallelization with currently available laser powers. The required average laser intensities in $GSD - 10^5$ -fold lower compared to STED – allowed the use of larger numbers of intensity zeros in parallel (Schwentker, 2007). SSIM has so far been experimentally shown with structured illumination, i.e. with a multitude of zero-intensity lines (Gustafsson, 2005). The high laser intensities were delivered by a laser with large transient pulse peak powers but very low repetition rate, which again slows down the image acquisition process and makes live-cell imaging less feasible. This restriction has been lifted by employing RSFPs: the ultra-low intensities required for the RESOLFT concept allowed scanning with several intensity zeros and thus several sub-diffraction sized observation areas in parallel for live-cell nanoscopy (Rego et al. 2012; Schwentker et al. 2007). The combination of RESOLFT and structured illumination therefore promises <50-60 nm with sub-second image acquisition times of $>50 \times 50 \ \mu\text{m}^2$ fields of view (Rego et al. 2012). A more advanced illumination pattern than using parallel lines of high intensities as in conventional SIM is the scanning with thousands of parallelized points as in spinning-disc microscopy (McCabe et al. 1996) or in multifocal SIM (York et al. 2012). Similarly, more than 100 000 doughnuts were generated simultaneously for ultra-fast live-cell RESOLFT imaging of large fields of view with down to 70 nm spatial resolution (Chmyrov et al. 2013) (Fig. 10d). With the development of further optimized photoswitchers, RESOLFT is therefore a very promising tool for revolutionizing live-cell optical nanoscopy.

2.2.6 Nanoscale writing

Concurrently to the imaging of various nanostructures, the RESOLFT concept was extended to the writing of structures with sub-diffraction size and spacing using visible light. Proposed in the early times (Hell, 2004), writing of nanostructures based on the STED and RESOLFT concept has been experimentally realized using photochromic materials (Andrew *et al.* 2009; Fischer *et al.* 2010; Harke *et al.* 2012; Li *et al.* 2009a; Scott *et al.* 2009; Wiesbauer *et al.* 2013; Wollhofen *et al.* 2013) or RSFPs (Grotjohann *et al.* 2011). Analogously to imaging sub-diffraction features, an intensity distribution of a photoswitching laser exhibiting one or several intensity zeros is used to maintain molecules in a reactive ON-state (i.e. in a writable state that, in contrast to the OFF-state, can be transferred to a permanent state) only at the sub-diffraction spots defined by the zeros. Scanning then realizes writing of nanostructures. RESOLFT has thus evolved to a versatile concept to reach the nanoscale in far-field optical applications.

2.3 Ultimate limit

The spatial resolution of all of the above approaches scales inversely with the square root of the intensity of the laser light featuring the intensity zero(s) (Harke *et al.* 2008a; Hell, 2004; Hell *et al.* 2003). Therefore, driving up the intensity should entail observation spots going down to the size of a single emitter. Several test samples containing different fluorophores have been chosen to prove this. For example, STED on the organic dye JA26 in a polyvinyl-alcohol (PVA) matrix could for the first time experimentally prove the square-root law down to a spatial resolution of 16 nm along one lateral dimension (Westphal & Hell, 2005). T-Rex STED nanoscopy of protein assemblies in cells provided spatial resolution down to 20 nm along all lateral directions (Donnert *et al.* 2006). The square-root dependence and spatial resolutions of <20–30 nm were also demonstrated for STED measurements on fluorescent beads or single fluorescent molecules

under special photostabilizing buffer conditions (reducing and oxidizing system (ROXS) buffer) (Harke et al. 2008a; Kasper et al. 2010). Going beyond this, RESOLFT imaging was applied to NV centers in diamond (Han et al. 2009, 2010; Rittweger et al. 2009a, 2009b). These fluorescent color centers are extremely photostable, and were imaged by STED nanoscopy as well using very high laser intensities, exemplifying a nearly perfect switch in fluorescence emission. These experiments once again proved the square-root intensity dependence with spatial resolutions down to 6 nm (Fig. 11a), only limited by the insufficient stability of the microscope stage. The use of a solid-immersion lens has recently enabled imaging of single NV centers with a spatial resolution of below 3 nm (Wildanger et al. 2012). The NV centers could be imaged multiple times without any sign of photobleaching (Fig. 11a). With fluorescence lifetimes >10 ns, these fluorescent centers perform almost equally well in the pulsed or CW STED mode (Han et al. 2009), with further improvements realized through gated detection (Vicidomini et al. 2011). 20-35 nm large 'nanodiamonds' containing one or more NV centers could be imaged equally well (Fig. 11a) (Han et al. 2009; Vicidomini et al. 2011), and progress in their size reduction down to 5 nm (Smith et al. 2009) and functionalization (Fu et al. 2007; Krueger, 2008) aims at their applicability in cellular nanoscopy (Tzeng et al. 2011). Apart from cellular imaging, STED nanoscopy has allowed the optical detection of electron spin resonances from single NV centers in diamond located at subdiffraction proximities (Wildanger et al. 2011), which is an important development for diverse areas of research such as quantum computation or magnetic resonance imaging (Balasubramanian et al. 2008; Jelezko & Wrachtrup, 2006; Maze et al. 2008).

The NV centers also exhibit dark states, transitions to which can specifically be addressed by light of different wavelengths: while red light (>600 nm) 'dumps' the NV centers into a >100 s long dark state, blue light efficiently depopulates this state (Han et al. 2010, 2012). Therefore, NV centers are also perfect candidates for GSD nanoscopy. Using this switching mechanism, the square-root law could be ascertained for the GSD approach with down to 12 nm spatial resolution (Fig. 11b), again limited by the stability of the microscope table and signal-to-noise (Han et al. 2010). The NV centers' ground state could be equally well inhibited, and emission of the fluorescence saturated, by simply raising the excitation intensity (Fig. 11a). Shaping the focal intensity distribution of the excitation laser in a way to present a local intensity zero (such as for the doughnut-shaped intensity distribution) and driving up its intensity consequently creates subdiffraction sized dark holes, as presented above for the GSD-based SPEM/SSIM approaches (Section 2.2.3). Scanning of these dark spots over the sample and subsequent computations created images of single isolated NV centers in diamond with down to <10 nm spatial resolution, proving the square-root dependence also for this approach (Han et al. 2012; Rittweger et al. 2009b). Furthermore, optical nanoscopy of NVs was achieved by combining spin manipulation and optical read-out, allowing individual electronic spins to be detected, imaged and manipulated coherently with nanoscale resolution (Maurer et al. 2010).

3. The coordinate-stochastic approach

3.1 Basics: (F)PALM/STORM

The challenges posed by repeated cycling between molecular states for the coordinate-targeted STED/RESOLFT approaches are alleviated when transferring individual molecules between different states stochastically in space. For example, molecules that are initially OFF may be individually driven to their ON-state at unknown spatial coordinates. The molecules' coordinates can be determined with sub-diffraction precision from their images on a camera. While the image of a

single molecule is again blurred by diffraction, the molecular position can be determined by calculating the centroid of the blurred image spot (Bobroff, 1986; Heisenberg, 1930). Restrictions are: (1) only single isolated molecules further apart than the distance given by diffraction can be imaged at a time to avoid any bias in localization of molecular positions from overlapping (blurred) spots, and (2) molecules, once in their ON-state, have to emit a sufficient number of photons N, since the localization precision scales with the inverse square root of N (Thompson et al. 2002). It is however important to realize that localization per se cannot provide super-resolution, i.e. finding a position of an object with arbitrary precision is not the same as resolution. Resolution is about separating similar objects at small distances. This is why, although it had routinely been applied for decades, specifically for spatiotemporal tracking of single isolated particles or molecules, localization on its own did not provide nanoscale images. Resolution requires a criterion to discern neighboring molecules such as realized by driving molecular transitions between different states (Hell, 2009b; Hell & Kroug, 1995; Hell & Wichmann, 1994). Therefore, an approach first suggested as (F)PALM (Betzig et al. 2006; Hess et al. 2006) or STORM (Rust et al. 2006) assembles a super-resolved image by determining spatial positions molecule by molecule using molecular transitions: (1) only a few isolated molecules are stochastically transferred (or activated) into their ON-state at once; (2) these molecules are imaged onto a camera and their spatial coordinates are determined through localization and saved; (3) molecules are transferred into an OFF-state; (4) stochastic activation of another subset of isolated molecules allows the read-out of neighboring molecules; and (5) repetition of this cycle realizes the reconstruction of an image with sub-diffraction resolution from the spatial coordinates of all imaged molecules (Fig. 12a). Similar to upgrading conventional confocal scanning or SIM systems for RESOLFT-type nanoscopy, the setup for this stochastic-switching based nanoscopy concept is a simple expansion of a conventional cameraequipped wide-field or TIRF microscope, updated by a stronger excitation laser and/or a second laser for controlling the switching of molecules (Fig. 12b, where an implementation with two separate detection channels is shown).

3.2 Molecular transitions

Various ways of preparing molecular states with different fluorescence properties such as an ONand an OFF-state have been suggested and implemented for this coordinate-stochastic nanoscopy. The strategy of combining stochastic molecular switching with localization was first used in methods called single-molecule high-resolution imaging with photobleaching (SHRImP) (Gordon *et al.* 2004) and nanometer-localized multiple single-molecule (NALMS) (Qu *et al.* 2004) imaging, in which the position of a small number of bright regular fluorophores was mapped by bleaching them (i.e. switching them off) consecutively, individually and stochastically. However, these methods start out from many bright molecules and hence from a bright total signal. They can therefore, in contrast to (F)PALM/STORM, accommodate only a small number of fluorophores. Similarly, the moleculespecific temporal characteristics of the blinking of nearby quantum-dots as recorded over consecutive camera frames were enough to separate two nearby emitters (Lidke *et al.* 2005), but it remains to be shown how many close-by emitters can be distinguished using the presented algorithms.

The original (F)PALM experiments employed photoactivatable fluorescent proteins (Patterson & Lippincott-Schwartz, 2002), with the switch-on and -off accomplished using dedicated laser light and irreversible photobleaching, respectively (Fig. 12*t*) (Betzig *et al.* 2006; Hess *et al.* 2006). Similarly, photoactivatable organic dyes can be used (Fig. 12*e*) (Fölling *et al.* 2007, 2008a). This unfortunately comes at the expense of not being able to record a molecule several



Fig. 12. Coordinate-stochastic (single-marker/single-molecule switching-based) nanoscopy ((F)PALM/ STORM). (a) Images with sub-diffraction spatial resolution are reconstructed from consecutive camera frames with simultaneous imaging and position-localization of single isolated (sparse) molecules only, which are switched on and off one after the other. (b) The setup is typically based on a conventional wide-field (TIRF) microscope with an excitation laser and, if required, an additional switching (or activation) laser, a microscope objective, dichroic mirrors (DC) for overlaying the lasers, de-coupling the fluorescence signal from the laser light and if required splitting up the fluorescence signal into two different wavelength ranges, fluorescence filters (here F1 and F2) for rejecting any residual laser scattering light and selecting the detected wavelength range, and a CCD camera detecting the fluorescence potentially in two channels (Ch. 1 and Ch. 2). (c-f) Various modes of (F)PALM/ STORM-based nanoscopy differing in the labels and molecular transitions: (*i*) the original (F)PALM approach using photoactivatable proteins that are initially dark or non-detectable, sparsely switched on by, for example, UV light and switched off by photobleaching. (d) The original STORM approach: Organic dyes such as Cy5 (or also fluorescent proteins) can be switched on and off by laser light of the same or different color or by spontaneous recovery (τ) , with on- and off-switching potentially assisted by an additional activator dye such as Cy3 and by photobleaching, respectively. (e) Single-cycle switching using photoactivatable organic dyes that are initially dark or non-detectable, sparsely switched on by UV light and switched off by photobleaching or rarely by a spontaneous dark state return (τ). (f) Multiple-cycle switching using RSFPs that can be switched between a dark and bright isomer using the excitation and UV light (or spontaneous transitions (τ) and photobleaching). (g) Example PALM/ STORM image of a tubulin network in a fixed PtK2 cell stained with a photoactivatable rhodamine

times, i.e. to acquire structural changes in the specimen over time. The original STORM experiments applied reversible photoswitchable organic fluorophores such as cyanines (Fig. 12*d*) (Rust *et al.* 2006): under certain buffer conditions they can be transferred between a bright ON- and a dark OFF-state using red and green light, mediated by nearby activator fluorophores (Bates *et al.* 2005). Photoswitching in cyanines and other organic dyes may also be accomplished by other molecular transitions such as via the transient population of metastable dark states including the dyes' triplet states or redox states populated therefrom (Bock *et al.* 2007; Heilemann *et al.* 2008; Hu *et al.* 2008; Rust *et al.* 2006; Steinhauer *et al.* 2008; van de Linde *et al.* 2008). Similarly, RSFPs may be employed (Fig. 12*f*) (Dickson *et al.* 1997; Egner *et al.* 2007; Geisler *et al.* 2007). Harnessing reversible molecular transitions allows the recording of a molecule's position several times, i.e. to acquire a sequence of super-resolution images (Endesfelder *et al.* 2010; Jones *et al.* 2011; Shroff *et al.* 2008; Stiel *et al.* 2008). Beside fluorescent proteins and organic dyes, (F)PALM/STORM-like recordings were realized with other emitters such as luminescent singlewalled carbon nanotubes (Cognet *et al.* 2008) or QDs (Hoyer *et al.* 2010; Lagerholm *et al.* 2006).

3.3 Continuous recording

The use of reversible molecular transitions led to the idea to continuously (and still stochastically) drive molecules between a bright and a dark state. Modalities termed 'PALM with independently running acquisition' (PALMIRA) (Egner et al. 2007; Geisler et al. 2007) and 'ground state depletion followed by individual molecule return' (GSDIM) (Fölling et al. 2008b) apply no activation or switch-on beam, and isolated fluorophores are allowed to blink stochastically and subsequently in time (not only in space) (Fig. 13a) (Fölling et al. 2008b; Hell, 2007). A single CW laser beam is used to generate the N photons and to switch the fluorophores off by transferring them into dark states. Dark state return is either promoted by switching cross-talk of the laser or by a spontaneous decay. The camera is run freely and the laser intensity and frame rate adjusted such that the average duration of the N-photon burst coincides with the duration of a camera frame. These purely stochastic concepts probably are the simplest far-field nanoscopy systems at present, because they require just uniform laser illumination, a freely running camera, and appropriate software. A straightforward advantage of such an acquisition mode is that it allows the use of conventional fluorophores such as many organic dyes or fluorescent proteins. Starting with STORM (Rust et al. 2006) and later GSDIM (Fölling et al. 2008b), experiments termed direct-STORM (dSTORM) (Heilemann et al. 2008; van de Linde et al. 2008) and Blinking Microscopy (Steinhauer et al. 2008), or single-molecule active control microscopy (SMACM) (Biteen et al. 2008, 2009; Sahl & Moerner, 2013; Sahl et al. 2012), spectral precision distance microscopy/spectral position determination microscopy with physically modifiable fluorochromes (SPDM/SPDM_{Phymod}) (Lemmer et al. 2008, 2009), or reversible photobleaching microscopy (RPM) (Baddeley et al. 2009) adapt buffer conditions and laser intensities to tune transitions to metastable dark states such as radical states of standard labels, producing super-resolution images of conventionally labelled samples (Fig. 13b, c) or even of autofluorescent cellular structures (Bierwagen et al. 2010). The return from long-lived metastable states can often be accelerated with additional UV or IR laser light, adding another parameter to optimize the acquisition of

⁽sub-diffraction (left) and diffraction-limited (right) counterparts, scale bar: 2 μm, adapted from (Fölling *et al.* 2007)). (*b*) Example STORM image of Alexa647-immunolabeled actin in a fixed COS-7 cell (scale bar: 2 μm, adapted from (Xu *et al.* 2012)).



Fig. 13. Coordinate-stochastic single-marker/single-molecule switching: stochasticity in space and time (GSDIM, (d)STORM, ...) and SOFI. (a) A fluorophore can continuously be cycled between its bright singlet (S_0 and S_1 , emitting fluorescence (Flu)) and dark state (triplet T and other long-lived (μ s-ms) dark states) system with a single excitation (Exc) laser, eliciting on-off blinking of fluorescence in time (as highlighted by a fluorescence time trace of a single Atto532 fluorophore in PVA, adapted from (Fölling et al. 2008b)) and space (as sketched in the lower panel for three different single molecules). (b) GSDIM/(d)STORM/... images of Rh6G-immunostained microtubules in PtK2 cells in aqueous buffer (left) and of the microtubule cytoskeleton of living PtK2 cells labeled with the fluorescent protein Citrine-Map2 (right). Upper left corner: Diffraction-limited wide-field recordings. Scale bars: 1 µm. Adapted from (Fölling et al. 2008b). (c) GSDIM/(d)STORM/... allows the use of a whole gamut of conventional organic dyes with different emission spectra as highlighted by super-resolution (lower panels) and corresponding diffraction-limited wide-field (upper panels) images of the cytoskeletal network of mammalian cells immunolabeled with eight different Alexa Fluor and Atto dyes spanning the visible wavelength range (emission maxima in upper color bar) according to the dSTORM principle (scale bar: 1 µm, adapted from (Heilemann et al. 2009b)). (d) Principle of SOFI imaging. SOFI is based on higher-order statistical analysis of temporal fluctuations recorded in a sequence of images. The spatial resolution increases with the order as exemplified by SOFI images of different order (as indicated) of two blinking quantum dots deposited on a cover slip (left, scale bars: 250 nm, adapted from (Dertinger et al. 2009)). (Right) Diffraction-limited wide-field (left) and SOFI (right) images of quantum-dot immunolabeled tubulin network of a 3T3 fibroblast (scale bar: 10 µm, adapted from (Dertinger et al. 2010)).

the single-molecule data (e.g. Fölling et al. 2008b). Transient stochastic on-switching may also be effected by molecular collisions or chemical reactions, where a fluorophore is only activated once interacting with other specific molecules such as single-walled carbon nanotubes (Cognet et al. 2008) or chemical reaction centres as in trajectory time distribution optical microscopy (TTDOM) (Mei & Hochstrasser, 2006), points accumulation for imaging in nanoscale topography (PAINT) (Sharonov & Hochstrasser, 2006), universal PAINT (uPAINT) (Giannone et al. 2010), NASCA (nanometer accuracy by stochastic chemical reactions) (Roeffaers et al. 2009), or CHemically Improved Resolution for Optical Nanoscopy (CHIRON) (Schwering et al. 2011). We have to note that albeit a whole gamut of different notations have been introduced ((F)PALM, STORM, PALMIRA, dSTORM, GSDIM, Blinking Microscopy, SMACM, SPDM, SPDM_{Phymod}, RPM, TTDOM, PAINT, uPAINT, NASCA, CHIRON or photoactuated unimolecular logical switching attained reconstruction (PULSAR) microscopy (Hu et al. 2008), they are all based on the same principle, namely, modulating the fluorescence emission of single molecules using molecular transitions. Differences appear only in details of the experimental design, i.e. switching mechanism, how many lasers used, camera running mode, choice of label, buffer conditions, etc.

3.4 SOFI

Molecule-specific ON-OFF blinking (Lidke et al. 2005) is the basis of a recent stochastic nanoscopy approach termed super-resolution optical fluctuation imaging (SOFI) (Fig. 13d) (Dertinger et al. 2009). Higher-order statistical analysis of the temporal fluctuations (recorded in a sequence of images) allows the identification of molecular positions with sub-diffraction spatial resolution. An example of such higher-order statistical analysis is the calculation of higher-order cumulants or autocorrelation functions (Dertinger et al. 2009, 2010; Geissbuehler et al. 2011, 2012). Similarly to FCS-based analysis of diffusing molecules, SOFI does not require temporal fluctuations recorded for single isolated molecules, but can be applied to up to ten-fold larger molecular densities than conventional (F)PALM/STORM. Furthermore, autocorrelations may be used to acquire, along with the spatial coordinates, temporal molecular parameters such as dark state kinetics, which might be, for example, a read-out for local oxygen concentrations (Geissbuehler et al. 2012). The spatial resolution increases with the order number, and images reconstructed from up to the 4th order cumulants have been demonstrated so far (Fig. 13d) (Dedecker et al. 2012; Dertinger et al. 2009, 2010; Geissbuchler et al. 2011, 2012). A face-to-face comparison to (F)PALM/STORM nanoscopy revealed 'that localization-based super-resolution can deliver higher resolution enhancements but imposes significant constraints on the blinking behavior of the probes, which limits its applicability for live-cell imaging. SOFI, on the other hand, works more consistently over different photo-switching kinetics and also delivers information about the specific blinking statistics. Its suitability for low SNR acquisition reveals SOFI's potential as a high-speed superresolution imaging technique' (Geissbuehler et al. 2011).

3.5 General aspects

It becomes obvious that in the coordinate-stochastic approaches there is a tradeoff between spatial resolution, image acquisition speed and error rates: the spatial resolution of the final image may be increased by selecting only single-molecule emission events with high photon count numbers, and the acquisition time may be reduced by activating more molecules per imaging cycle, however introducing errors due to the neglect of some molecular positions (and thus lower sampling of



(in e,f: Separation at the single-fluorophore detection level: 1 Laser, 2 Det. Ch.)

Fig. 14. 3D and multi-color imaging with coordinate-stochastic single-marker/single-molecule switching-based nanoscopy. (a) Optical sectioning and out-of-plane signal rejection achieved by two-photon on-switching or activation: Super-resolution images of lamin of a U373MG cell stained with a photoactivatable rhodamine (inset: equatorial slice as marked by the line, scale bar: 2 µm, adapted from (Fölling et al. 2007)). (b) (Left) Different approaches of 3D (F)PALM/STORM-based imaging: astigmatism using a cylindrical lens results in an elliptical distortion of the images of out-of-plane (axial z-direction) molecules, double plane imaging comparing focused and defocused camera images, 4Pi using two opposing objectives, and double-helix detection employing a 'doubled' detection of each single molecule where the orientation of the two lobes of intensity changes with the z-position of the molecule. (Right) Two-color STORM image of immunolabeled bII-spectrin (green) and adducin (magenta) in fixed axons reveals that actin, spectrin and adducin form a coordinated, quasi-1D lattice structure in axons (scale bar: 500 nm, adapted from (Xu et al. 2013), where 3D astigmatic imaging was also performed). (c) Two-color image of the microtubular network in a PtK2 cell stained with the reversibly photoswitchable protein rsFastLime (green) and the organic dye Cy5 (red) generated by subsequent recordings using two excitation lasers and two detection channels (upper left corner: diffraction-limited wide-field recording, scale bar: 1 µm, adapted from (Bock et al. 2007)). (d) Fast two-color 3D-STORM images of live BSC-1 cells using one activation and two excitation lasers inducing fluorescence blinking over time: Alexa 568-labeled transferrin (green) and clathrin-coated pits labeled with Alexa647 via a SNAP tag (magenta), x/y-projection of the recordings of multiple sections along z (upper panel), and different cross-sections through two objects (i, ii) indicated in the upper panel (x/y) near the plasma membrane (left), x/z cutting through the middle of the invaginating pits (middle) and corresponding x/z cross-section of the clathrin channel only (right)). Scale bars: 500 nm (upper panel) and 100 nm (lower panels), adapted from (Jones et al. 2011). (e, f) Multi-color imaging via single-molecule signatures using one continuously running laser and two detection channels. Color separation is realized by applying fluorescence labels with slightly

the structure) and the risks of producing overlapping images of single molecules which hide information on molecular positions (e.g. Nieuwenhuizen *et al.* 2013; Shroff *et al.* 2008; Small, 2009). Therefore, quite a number of improvements in determining molecular positions from the isolated blurred spots of the camera frames have been promoted for (F)PALM/STORM-based nanoscopy, especially aiming at image reconstructions for more densely labeled samples, at low SNR, with improved localization precision, with increased acquisition and analysis speeds, and for different blinking/photoswitching statistics (e.g. Cox *et al.* 2012; Cronin *et al.* 2009; Endesfelder *et al.* 2010; Hedde *et al.* 2009; Henriques *et al.* 2010; Holden *et al.* 2011; Huang *et al.* 2011; Jones *et al.* 2011; Larson, 2010; Laurence & Chromy, 2010; Mortensen *et al.* 2010; Nieuwenhuizen *et al.* 2013; Pertsinidis *et al.* 2010; Smith *et al.* 2010; Wolter *et al.* 2010). In addition, one should bear in mind that rather immobile molecular orientations and out-of-focus sites may potentially result in significantly biased determinations of molecular positions (e.g. Enderlein *et al.* 2006; Engelhardt *et al.* 2011). Strategies to diagnose, mitigate and even fully correct molecular dipole orientation-related position artifacts have recently been emerging (Backer *et al.* 2014; Backlund *et al.* 2012, 2014; Lew *et al.* 2013; Lew & Moerner, 2014; Backer *et al.* 2013).

3.6 3D imaging

Sectioning or 3D imaging has been implemented for coordinate-stochastic switching-based nanoscopy. Sectioning along the axial direction is provided when activating molecules via two- or multi-photon processes (Fig. 14a) (Fölling et al. 2007, 2008a; York et al. 2011). On the other hand, most (F)PALM/STORM-based experiments have applied a TIRF illumination scheme from the very start, i.e. only planes of the sample that are within <100 nm near the microscope cover glass are selected and out-of-plane background rejected. Several different approaches have been proposed and demonstrated to supply real 3D resolution (Fig. 14b) (whether in wide-field or TIRF illumination mode), such as the introduction of astigmatism by the use of cylindrical lenses (Huang et al. 2008; Mlodzianoski et al. 2009; York et al. 2011) or adaptive optics (Izeddin et al. 2012), double-plane detection using two camera channels (Juette et al. 2008; Mlodzianoski et al. 2009), two opposing objectives in a 4Pi illumination and detection mode (Aquino et al. 2011; Shtengel et al. 2009), a double-helix modification to the emission path of the microscope (Lee et al. 2012, 2014; Pavani et al. 2009; Sahl & Moerner, 2013), bisected pupil 3D imaging (Backer et al. 2014), an Airy-beam point spread function (Jia et al. 2014), other novel information-optimal point spread function designs (Shechtman et al. 2014) or a combination of two opposing objectives and astigmatism (Xu et al. 2012). A nice example of 3D STORM nanoscopy recently presented novel details of the spatial organization of actin and other cytoskeletal filaments in mammalian cells (Fig. 12b) (Xu et al. 2012) and axons (Fig. 14b) (Xu et al. 2013). Observing single-molecule fluorescence from deep inside samples such as tissue may prove itself

shifted emission spectra, which emit differently into the two detection channels (lower panels: fluorescence emission spectra of the given fluorophores and (black) transmission spectrum of the applied dichroic mirror for splitting up the signal onto the two detection channels ch1 and ch2), and can be distinguished by a different ratio of photons detected in the two detection channels (upper left: two-dimensional histogram of photon pairs simultaneously registered in the two detection channels ch1 and ch2, allowing an accurate distinction of the three different fluorophores (color coded)). Super-resolution images and diffraction-limited counterparts (upper corners) of (*e*) Alexa488-labeled vimentin (blue), Alexa514-labeled clathrin (green), and Rhodamine 3c-labeled tubulin (red) in fixed PtK2 cells, and (*f*) Caveolin 1 (red) and Caveolin 2 (green) in live PtK2 cells labeled with TMR via SNAP tag and the fluorescent protein Citrine, respectively (scale bars: 2 µm, adapted from (Testa *et al.* 2010)).

difficult due to enhanced background signal stemming from scattered light or out-of-focus fluorescence. A remedy of this limitation may be the combination of the (F)PALM/STORM-based readout with selective-plane-illumination microscopy (SPIM) (Zanacchi *et al.* 2011) and/or the use of adaptive optics to correct for aberrations (Izeddin *et al.* 2012).

3.7 Dynamics

A limitation of stochastic single-molecule switching is the rather large total image acquisition time, since a sufficiently large number of single-molecule positions and thus camera frames (usually $>10\,000-100\,000$) have to be gathered for the reconstruction of an accurate and representative super-resolved image of a reasonably complex structure (Betzig et al. 2006). Furthermore, the initial use of photoactivatable, i.e. only one-cycle, photoswitchable fluorophores originally impeded the recording of multiple consecutive super-resolved images. However, the advent of reversibly photoswitchable labels (Fig. 12d, f) and the aforementioned sophisticated image reconstruction algorithms have since then enabled time-lapse studies of live-cell dynamics with (F)PALM/ STORM-based techniques (e.g. Dedecker et al. 2012; Endesfelder et al. 2010; Flors et al. 2009; Hess et al. 2007; Jones et al. 2011; Shroff et al. 2008; Stiel et al. 2008; Testa et al. 2010; Wilmes et al. 2012; Wombacher et al. 2010). Longer observation times can thereby be achieved by using, for example, transiently binding fluorescent markers (Lukinavicius & Johnsson, 2011), such as a peptide that is designed to bind reversibly to the F-actin cytoskeleton (Izeddin et al 2011). With further optimization of the label brightness, labeling protocol, camera technology and image acquisition and reconstruction, time resolutions of down to <1 s have been anticipated for stochastic single-molecule switching-based nanoscopy techniques (Dempsey et al. 2011; Huang et al. 2013; Jones et al. 2011; Ondrus et al. 2012). Importantly, as well, photoswitching and continuous determination of molecular positions may be combined to perform singlemolecule tracking at higher concentration of the labeled molecules (Eggeling et al. 2007; Hess et al. 2007; Manley et al. 2008).

3.8 Multi-colour recordings

Multi-color imaging is straightforward for the single-molecule-based nanoscopy techniques. The most obvious approach generates separate detection and localization of different labels by subsequently or simultaneously switching them on and off and detecting their emission at different colors using several dedicated laser lines and appropriate filtering (Fig. 14c, d) (e.g. Bates et al. 2007; Bock et al. 2007; Klein et al. 2011; Shroff et al. 2007; van de Linde et al. 2009; Wilmes et al. 2012). Discrimination of up to six different colors was introduced for the original STORM approach by applying different labels at different wavelengths for activation and emission (Bates et al. 2011). The simplest approach is to use single-molecule signatures not only for determining positions but also for identifying different species (Schoenle & Hell, 2007): a single continuously running excitation laser elicits fluorescence emission of various labels with slightly differing emission spectra (e.g. with their maxima 20-40 nm apart), two camera channels (preferably on the same chip) detect the fluorescence signal in nearby wavelength ranges, and single molecules are assigned through the ratios of photons detected in each channel (Bossi et al. 2008). Using this approach, up to four different colors have been separated with nanoscale resolution in fixed as well as living cells (Fig. 14e, f) (Gunewardene et al. 2011; Testa et al. 2010). Similarly, other spectroscopic parameters such as fluorescence anisotropy or lifetime may be used to distinguish between molecules of different rotational mobility (e.g. immobilized and freely diffusing molecules) or lifetime but same emission color (Schoenle & Hell, 2007; Testa *et al.* 2008), or to simply image molecular positions and mobilities (Gould *et al.* 2008).

(F)PALM/STORM or GSDIM/(d)STORM-based nanoscopes have nowadays been commercialized and found their ways into a lot of laboratories all over the world, adding to the toolset for solving long-standing biological problems.

4. Conclusions: coordinate-targeted versus -stochastic

Both branches of nanoscopy (super-resolution optical microscopy) – coordinate-targeted STED/ RESOLFT and coordinate-stochastic (F)PALM/STORM - are ultimately based on the same basic principle: transferring fluorescent labels between states of different emission characteristics (such as a bright ON- and a dark OFF-state) to allow the discerning of nearby objects (e.g. Hell, 2009b) (Fig. 15). Both branches are complementary and have their own advantages and disadvantages. The advantage of stochastically switching molecules is obvious: Whereas in the coordinatetargeted STED/RESOLFT read-out mode a molecule has to undergo many ON-OFF cycles, in the stochastic switching mode, a single OFF-ON-OFF cycle per molecule is in principle enough to produce an image, thus avoiding switching fatigue. However, in contrast to STED/RESOLFT nanoscopy, which usually creates a direct image of molecular distributions, computational algorithms are generally applied for (F)PALM/STORM to reconstruct the final image, a potential source of bias. For example, some molecules may be localized more precisely than others, because the number of photon emissions N follows a statistical distribution. Therefore, to ensure a certain resolution, the stochastic read-out mode usually defines a brightness threshold (e.g. N > 50) and molecules emitting less than this threshold in a bunch are discarded without contributing to the image. In a sense, this rejection of molecular events is to the stochastic read-out what switching fatigue (or photobleaching) is to its coordinate-targeted counterpart; the higher the required resolution, the more molecular events are discarded. Often, (F)PALM/STORM-based experiments have achieved focal plane resolution of <20 nm at the expense of discarding molecules (see e.g. Shroff et al. 2008; Small, 2009). In addition, some molecules may not be activated at all or counted several times, i.e. the molecular numbers assigned to the final image may be biased. While this imperfect assignment may not corrupt images of filament-like structures such as of microtubules, actin, mitochondrial or ER membrane renditions, it may compromise the accurate characterization of protein clusters (e.g. Annibale et al. 2011). In general, coming along with the increased sensitivity of the nanoscopy approach, greater care has to be taken when labelling cellular samples, especially with respect to unspecific background staining (Wurm et al. 2010). Artifacts due to, for example, improper fixation in immunolabeling or unspecific binding may not be observed in confocal but may be visible in nanoscopy images, due to the improved spatial resolution in the latter (Opazo et al. 2012; Tanaka et al. 2010). Also, due to the increased spatial resolution, the term "co-localization" may become invalid, since two objects (especially when labelled via a primary and secondary antibody as in most immunolabeling approaches) cannot occupy the same spot.

It is worth noting that the enhanced sensitivity of all nanoscopy concepts to artifacts calls for elaborate control measurements. For example, the results of previous protein cluster analyses using STED nanoscopy were ascertained using different labels as well as different STED setups, potentially introducing different switching fatigues (Sieber *et al.* 2007). At the same time, the multitude of different nanoscopy methods allows new ways of validating results. For example, both nanoscopy branches, the coordinate-targeted and the coordinate-stochastic, may



Fig. 15. Coordinate-targeted versus coordinate-stochastic nanoscopy. Both families of methods are based on transitions between molecular states of different fluorescence characteristics (such as a bright ON- and a dark OFF-state) realizing the separation of different molecules within a diffraction-limited area by subsequently confining emission either to sub-diffraction sized spots defined in space (coordinate-targeted (deterministic), left) or stochastically in space on single isolated molecules (coordinate-stochastic, right). Sub-diffraction coordinate-targeted and -stochastic imaging can be realized using the same fluorescence labels and switching mechanisms. (a) Coordinate-targeted STED (left) versus coordinate-stochastic (F)PALM/STORM images (right) of organic-dye-labeled microtubules in fixed PtK2 cells. (b) Coordinate-targeted GSD (left, scale bar 500 nm) versus coordinate-targeted RESOLFT (left) versus coordinate-stochastic (F)PALM/STORM images (right) of the RSFP Dreiklang expressed in live PtK2 cells at Keratin19 (left) and Map2-micotubules (right). Adapted from (Brakemann et al. 2011). Diffraction-limited counterparts in upper parts. All other scale bars: 1 µm.

exploit the same molecular transitions and may thus be applicable to the same samples. Figure 15 depicts examples of STED versus (F)PALM/STORM (Fölling et al. 2007), GSD versus GSDIM (Bretschneider et al. 2007; Fölling et al. 2008b), and RESOLFT versus PALM (Brakemann et al. 2011) nanoscopy experiments, where the same or similar labels have been used for nanoscale cellular imaging. Consequently, both techniques could be applied for the validation of a specific result. Of course, while complementary, one approach may be more suitable for a concrete measurement than the other, and this argues for research environments having access to several of the above methodologies. For example, STED/RESOLFT has proven to be able to record fast live-cell dynamics, even deep inside tissue and in vivo (at times through the combination with single-molecule spectroscopic tools such as FCS), yet, to maintain reasonable signal-to-noise or -background levels, brightly labeled samples are often favored. On the other hand, (F)PALM/STORM-based experiments have shown remarkable results when imaging faintly labeled structures such as actin, but due to their acquisition mode have proven to be less versatile for dynamic live-cell and deep-tissue imaging, even if recent developments may improve their applicability in this regard. Quite generally, one should keep in mind and expect that new research will address such limitations where they are not of a fundamental nature. Still one should not expect one microscope to be optimized in all aspects of microscopy: high spatial and temporal resolution, low phototoxicity (and thus large live-cell compatibility), and high image contrast. For example, while (F)PALM/STORM- and STEDbased nanoscopy approaches may suffer from still too low temporal resolution and potentially too high phototoxicity, respectively, recent ultrafast, low-phototoxic light-sheet based optical microscopes (Wu et al. 2013; Chen et al. 2014) so far do not give sub-diffraction spatial resolution.

It is becoming obvious that lens-based far-field fluorescence nanoscopy opens up unprecedented possibilities for biophysical and medical research. Wide-spread availability of instrumentation and expertise and the targeted application to important problems will enable the full impact of far-field nanoscopy to be realized, with many answers to long-standing scientific quests.

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