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Atomic and mesoscopic structure of Dy-based surface alloys on noble metals

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Abstract

Surface alloys are a highly flexible class of low dimensional materials with the opportunity to tune and control the spin and charge carrier functionalities on the nanoscale. Here, we focus on the atomic and mesoscopic structural details of three distinct binary rare-earth-noble metals (NM) surface alloys by employing scanning tunneling microscopy and low energy electron diffraction. Using Dysprosium as the guest element on fcc(111) NM substrates, we identify the formation of non-commensurate surface alloy superstructures, which lead to homogeneous moiré patterns for DyCu₂/Cu(111) and DyAu₂/Au(111), while an inhomogeneous one is found for DyAg₂/Ag(111). The local structure was analyzed for these samples and the observed differences are discussed in the light of the lattice mismatches of the alloy layer with respect to the underlying substrate. For the particularly intriguing case of a DyAg₂ surface alloy, the surface alloy layer does not show a uniform long-range periodic structure, but consists of local hexagonal tiles separated by extended domain walls, which occur likely to relieve the in-plane strain within the DyAg₂ surface alloy layer. Our findings clearly demonstrate that surface alloying is an intriguing tool to tailor the local atomic structure as well as the mesoscopic moiré structures of metallic heterostructures.

1. Introduction

The growing demand for future technological applications to transport, process and store digital information on ever smaller length scales has triggered the search for novel low dimensional materials with unconventional spin and charge carrier functionalities. Apart from intrinsically 2D materials such as atomically thin honeycomb structures [1, 2] or transition metal dichalcogenides [3, 4], binary surface alloys have become an intriguing choice for engineering ultrathin structures with tunable material properties. Surface alloys can be fabricated with long-range order and high structural quality on noble metal (NM) surfaces by replacing surface atoms of the NM host materials with different kinds of metallic guest atoms. This allows the investigation of bonding mechanisms for otherwise immiscible metals and to design the spin-dependent band dispersion of surfaces states [5–11].

The most frequently studied class of surface alloys is heavy metal NM surface alloys grown on fcc(111) NM surfaces. Typical examples for this class of surface alloys are BiAg₂, PbAg₂, Bi_xPb_{1-x} [12–15] surface alloys which all exhibit a giant Rashba split surface state in the vicinity of the Fermi energy. Crucially, the spin-splitting, as well as the energetic position of this Rashba-type surface state, strongly depends on the spin-orbit coupling strength of the guest and host materials as well as on the vertical surface relaxation of the guest atoms [16–22]. This offers an intriguing opportunity to control the spin-split band structure of

the material at the Fermi energy and hence to tailor the corresponding spin functionalities of these materials for spintronic applications.

Recently, the observation of ferromagnetism in a rare-earth (RE)-based surface alloy with high Curie temperature [23] and topological characteristic [23–26] have revived the research on surface alloys. Interestingly, RE-based surface alloys exhibit intriguing structural properties that are clearly distinct from those of heavy metal-based surface alloys. All heavy-metal NM surface alloys on fcc(111) substrates form the same $\sqrt{3} \times \sqrt{3}R30^\circ$ superstructure in which one guest atom per unit cell replaces one host atom of the surface layer. This results in an equal density of atoms in the first and second layers of the material. The situation is significantly more complex for RE-based surface alloys for which the density of atoms in the alloy layer (first layer) and the substrate's top layer (second layer) are typically different. This results in the formation of moiré patterns for RE/NM surface alloys depending on the element of the guest and host atoms. It is established that the density of states of the alloy layer is periodically modulated within the moiré superstructure [26]. An interesting consequence of this complex pattern is the moiré-driven hybridization of electronic states near the Fermi level for various RE/NM surface alloys [24] that can arise due to the lattice strain within the alloy layer as well as the partial vertical buckling of the guest atoms [24, 27]. For instance, Correa *et al* observed electronic states for the GdAg₂ surface alloy that depend on the parameters of the moiré lattice [27]. In addition to the atomic superstructures, recent studies reported the existence of long-range ordered moiré patterns for the GdAg₂/Ag(111) and GdAu₂/Au(111) surface alloys with periodicities of the surface alloy layer of nearly (12 × 12) on a (13 × 13) grid of the bare Au(111) and Ag(111) substrates [23, 28].

A study of the GdAg₂ reports strain within the alloy layer (1%–7%) that can be tuned by changing the substrate's temperature during the Gd deposition and can result in a further tessellation of the alloy layer [27]. CeAu₂/Au(111) and LaAu₂/Au(111) exhibit lattice periodicities of (10.6 × 10.6) of the CeAu₂ surface alloy on a (11.6 × 11.6) grid of the bare Au(111) surface, and of a (10.4 × 10.4) LaAu₂ lattice on a (11.4 × 11.4) Au(111) grid [24]. Similarly, ErCu₂/Cu(111) has a lattice periodicity of (8.7 × 8.7) the ErCu₂ alloy layer on the (9.6 × 9.6) grid of Cu(111) [29]. Despite these numerous investigations of a variety of RE/NM surface alloys [5, 23, 24, 28–30], there is still no clear model that can predict the observed superstructures based on the chemical composition and surface orientation of the constituents of the surface alloy. In this regard, these characteristic structural (superstructure and moiré pattern) and corresponding electronic properties make RE-based surface alloys a compelling substrate for potentially functionalizing the properties of organic and inorganic adsorbate structures grown on top [23, 31–35].

In the present work, we, therefore, focus on a comprehensive study of the atomic and mesoscopic structure of three surface alloys formed between the guest atom Dy and the (111) surfaces of the NMs Cu, Ag, and Au. Our results reveal identical stoichiometry for all three systems, i.e. a 2:1 ratio between the host and the guest elements. Each alloy forms a unique non-commensurate superstructure with different degrees of complexity. As a result of their atomic unit cells, all three surface alloys exhibit additional long-range ordered moiré patterns due to the atomic mismatch between the surface alloy layer and its respective substrate lattice. The DyAu₂ surface alloy exhibits a relatively straightforward periodic structure. In the case of DyCu₂, two mirror domains are developed and a highly periodic structure is maintained. In the case of DyAg₂, we find a non-uniform moiré pattern with complex electron density modulation in scanning tunneling microscopy (STM), which reveals a strain-relief mechanism in the form of surface tessellation. Despite an almost identical interatomic distance of the surface atoms of Au(111) and Ag(111), we observe significantly different surface structures.

2. Experimental details

Sample preparation. All samples were prepared in an ultra-high-vacuum (UHV) preparation chamber with a base pressure $< 5 \times 10^{-10}$ mbar. This preparation chamber is equipped with a low-energy electron diffraction (LEED) optics and a Dy evaporator.

The NM surfaces were prepared by Ar⁺ sputtering using energy ranges between 1.2–1.5 keV for 30 min and subsequent annealing at $T_{\text{Cu}} = 845$ K and $T_{\text{Ag}} = T_{\text{Au}} = 860$ K for 30–45 min. The cleanliness of the surface was confirmed by a low defect density of the surface in a large scale room temperature STM experiment and the narrow spot profile of the three-fold diffraction spots of the fcc(111) surfaces acquired by LEED for energies between 50–120 eV.

Dy was evaporated from a tungsten crucible using a FEM-3 FOCUS e-beam evaporator at a constant flux that was monitored using the flux monitor controller. The substrates were kept at constant temperatures (~ 570 – 630 K) during the Dy deposition (base pressure $< 5 \times 10^{-10}$ mbar). The sample temperatures are measured using a K-type thermocouple in contact with the sample plate. The freshly

prepared surface alloys were held at ~ 20 K lower temperatures for a few minutes after the deposition to improve surface quality.

STM. The STM measurements were performed in a UHV system directly connected to the preparation chamber (VT-AFM XA, Omicron GmbH, with base pressure $< 2 \times 10^{-11}$ mbar). All measurements were carried out in constant current mode. In our setup, the biased voltage is applied to the tip. The sample temperature was kept at 106 K using a liquid N₂ cooling system. Tungsten tips were electrochemically etched, and *in situ* cleaned by Ar⁺ sputtering (1.5–4.0 keV) and subsequently annealed using a direct current to reduce impurities and achieve an atomically sharp apex. The STM images were processed and analyzed using WSxM [36] and Gwydion [37] software.

LEED. LEED measurements were performed using a rearview four grid system from Scienta Omicron at room temperature. Images were acquired using a CCD camera attached directly at the viewport of the LEED optics. To visually enhance the image contrast, all images were post-processed using the ImageJ software. The simulation of the diffraction pattern was performed using the Spot-Plotter software [38]. The DyAu₂ data were acquired using an MCP LEED in another UHV chamber, for which the image was corrected using LEEDCal [39]. The error values of the superstructure matrixes are estimated by varying the superstructure matrix entries and visually comparing the simulated pattern with the experimental data. This is done by changing the radial and azimuthal parameters limited by the full width at half maximum of the spot profile. We then used the largest deviation value. To obtain the error bars for the real space unit cell parameters, LEED images are evaluated by computing the positions of the surface alloy and the substrate diffraction spots, which are obtained by profile fitting of the 2D Gaussian function. Error propagation of these quantities is based on the half width at half maximum of the fitted spot profile.

3. Results

In this section, we will present LEED and STM results for the surface alloy superstructures of Dy on Au(111), Cu(111), and finally, Ag(111).

4. DyAu₂/Au(111)

4.1. Periodic order of the DyAu₂/Au(111) surface alloy

Figure 1(a) shows the LEED pattern of the DyAu₂/Au(111) surface recorded for an electron energy of 65 eV. Besides the substrate spots (blue), the LEED pattern reveals a set of diffraction spots that point to the formation of a DyAu₂ surface alloy superstructure. The best agreement between the experimental data and the simulated LEED pattern was obtained for the structure with the superstructure matrix

$$\begin{bmatrix} 2.17 \pm 0.04 & 1.09 \pm 0.04 \\ -1.09 \pm 0.04 & 1.09 \pm 0.04 \end{bmatrix}$$
. The top left quarter of the LEED data is superimposed with the first-order

diffraction spot of the substrate (blue) as well as the first and second-order spots of the alloy (yellow). The corresponding alloy superstructure exhibits a hexagonal unit cell with a lattice constant of ~ 5.41 Å ($\sim 1.88 \times d_{\text{Au}}$, where $d_{\text{Au}} = 2.88$ Å) in real space which is rotated 30° with respect to the $\bar{1}10$ direction of the substrate. In addition, we observe a second diffraction pattern with a large number of diffraction spots with varying intensity. This diffraction pattern could be modeled by the superstructure matrix

$$\begin{bmatrix} 13 \pm 0.27 & 0 \pm 0.27 \\ 0 \pm 0.27 & 13 \pm 0.27 \end{bmatrix}$$
. Within the experimental uncertainty, this superstructure reveals a close to

commensurate or even a commensurate registry with respect to the surface grid. The corresponding diffraction spots are superimposed onto the experimental diffraction image as red circles and the unit cell in k-space is marked by a green rhombus. This second diffraction pattern with its large ~ 37.44 Å unit cell vector length in real space is assigned to the moiré pattern of the DyAu₂/Au(111). The existence of such a moiré already points to an atomic mismatch between the surface alloys layer and the topmost layer of the Au(111) substrate. More details about the moiré pattern will be discussed in the following section.

4.2. Surface structure of DyAu₂/Au(111)

Next, we studied the DyAu₂ surface alloy structure by STM to understand the local atomic and mesoscopic structure in the real space. The large area in figure 1(b) shows that the herringbone reconstruction of the bare Au substrate is replaced by uniform moiré patterns. This is an indication that the monolayer surface alloy forms successfully, similar to the earlier report for the GdAu₂ surface alloy [25]. Figure 1(b) shows two adjacent terraces with uniformly grown DyAu₂ surface alloy structures. A more detailed view of the structural properties of the DyAu₂ surface alloy can be obtained in the atomically resolved STM image in figure 1(c). We observe periodically ordered bead-like features, which are superimposed on the moiré

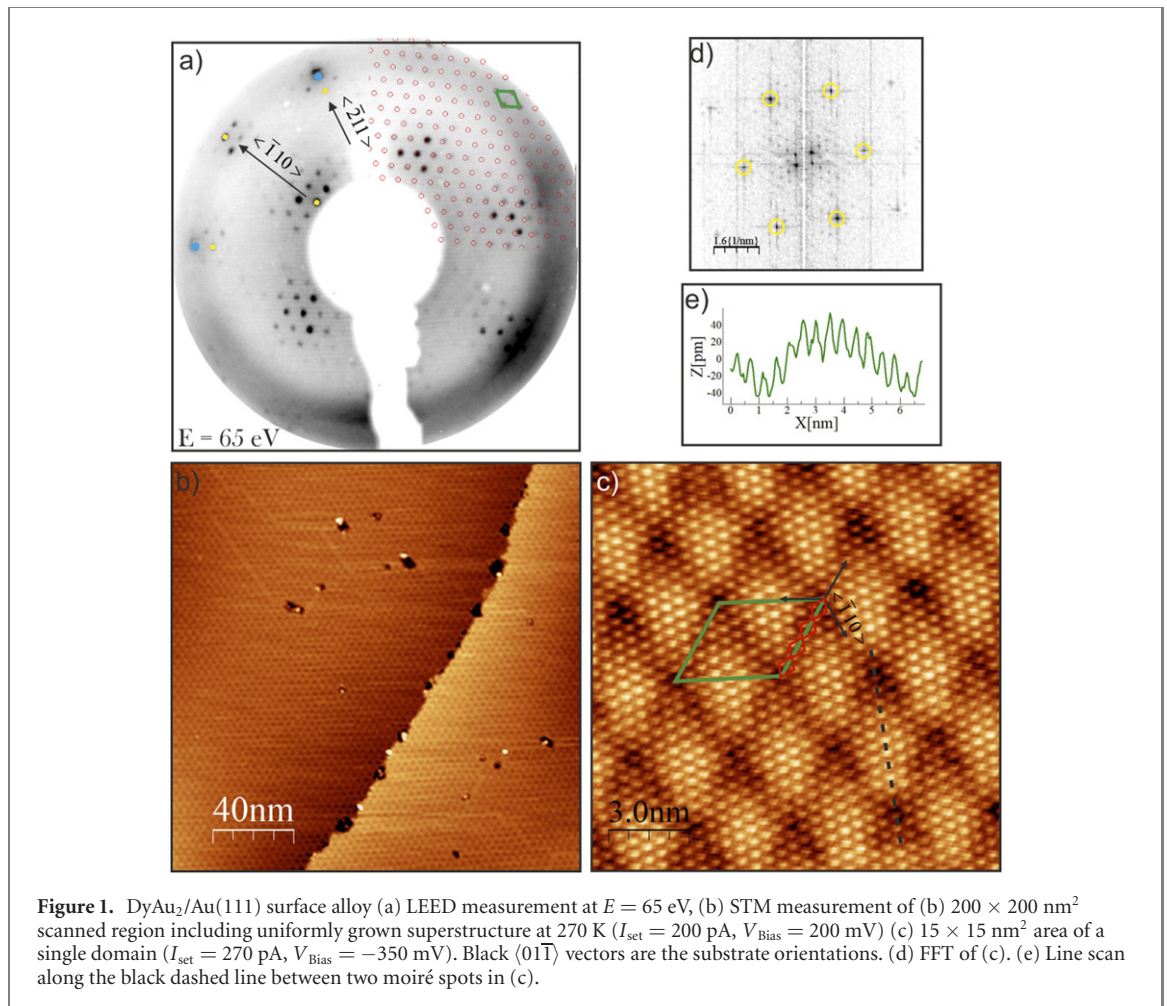


Figure 1. DyAu₂/Au(111) surface alloy (a) LEED measurement at $E = 65$ eV, (b) STM measurement of (b) 200×200 nm² scanned region including uniformly grown superstructure at 270 K ($I_{\text{set}} = 200$ pA, $V_{\text{Bias}} = 200$ mV) (c) 15×15 nm² area of a single domain ($I_{\text{set}} = 270$ pA, $V_{\text{Bias}} = -350$ mV). Black $\langle 01\bar{1} \rangle$ vectors are the substrate orientations. (d) FFT of (c). (e) Line scan along the black dashed line between two moiré spots in (c).

pattern-induced contrast variation. These bright protrusions are separated by ~ 5.5 Å. They can be attributed to Dy atoms with enhanced electronic contribution to the tunneling process, similar to earlier works [23–25, 28]. Thus, we assume and assign the small bright protrusions to Dy atoms which hence reflect the atomic periodicity of the DyAu₂ superstructure. Fast Fourier transform (FFT) of this image in figure 1(d) reveals the periodic ordering of these protrusions in reciprocal space (marked by yellow circles), agreeing well with the diffraction pattern found in LEED. The broad dark features, on the other hand, reflect the periodicity of the moiré pattern and are caused by the reduced electron density in the moiré potential modulation. The proposed surface alloy unit cell (red rhombus), the moiré unit cell (green rhombus) as well as the $\langle 01\bar{1} \rangle$ crystal orientations (black vectors) are marked in figure 1(c). The surface alloy lattice vectors have an average length of 5.5 ± 0.3 Å and are oriented along the substrate's high symmetry $\langle 11\bar{2} \rangle$ directions. The average length of the moiré lattice vectors is $\sim 36.0 - 37.0$ Å and they are oriented along the $\langle 01\bar{1} \rangle$ directions of Au(111). These values are in quite good agreement with our LEED analysis. A line scan along the direction connecting two moiré minima (dashed line in figure 1(c)) shown in figure 1(e) reveals a maximum apparent vertical corrugation of ~ 0.55 Å within the moiré unit cell. The lattice constant of both the surface alloy and the moiré are very similar to GdAu₂ surface alloy [28]. In both cases, the observation of the moiré pattern points out to a different density of atoms in the first and second layers of the crystal. Correa *et al* reported the observation of different contrast moiré patterns in GdAu₂ [26]. Their theoretical results reveal the origin of the contrast to be various degrees of vertical relaxation of the alloy layer from the supporting substrate to form lattice-matched periodicity. Further, they assign TOP and FCC/HCP sites to valleys and hills of the moiré pattern contrast. Their theory is further supplemented with experimental dI/dV mapping and spectroscopy data which makes clear support of two types of electronic states, characteristic to each site. It should be noted that the tip/sample distance could also influence the intensity of the observed moiré contrast [40], making it difficult to identify the host metal elements (in this case Au atoms) of the surface alloy. Careful examination reveals that the minima of the moiré pattern in the STM image exhibit different arrangements of Dy atoms. These local variations suggest a non-commensurate registry between the moiré pattern and the substrate grid. This registry can either be classified as incommensurate or as higher order commensurate with a unit cell size larger than the STM

image. This observation suggests a strong variation in the local atomic registry between the alloy layer and the supporting topmost layer of the gold substrate. Considering the size of the moiré lattice from our STM and LEED results we conclude that nearly 12 atoms of the surface layer (four Dy and eight Au atomic units) are spanned along almost 13 Au atoms of the substrate's top layer. This causes an atomic mismatch of almost 7.7% between the layers. The irrational ratio of the atomic mismatch results in continuously altering adsorption sites within the moiré unit cell which ultimately is responsible for the varying STM contrast within the moiré unit cell in figure 1(c). Similar incommensurate moiré patterns were also previously observed for weakly bounded 2D materials on metal surface [41, 42] and hence point to a rather weak coupling between the surface alloy layer and the substrate crystal.

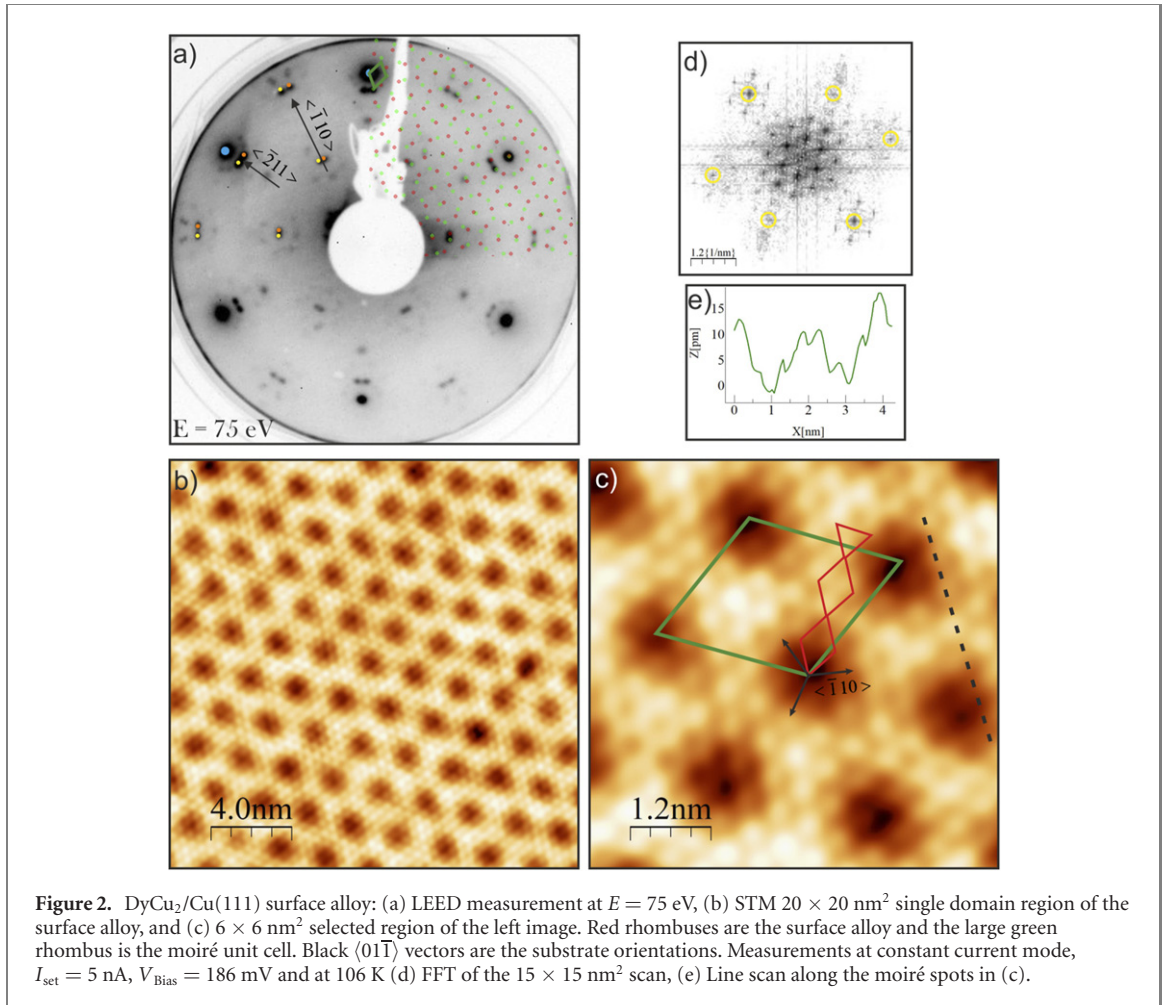
5. DyCu₂/Cu(111)

5.1. Periodic order of the DyCu₂/Cu(111) surface alloy

Figure 2(a) presents the LEED pattern of DyCu₂/Cu(111) surface recorded for an electron energy of 75 eV. The six most intense spots near the edges of the screen (one marked blue) are the first-order spots of Cu(111) substrate. The top left quarter of the image is superimposed with the first three orders of simulated diffraction spots of the alloy superstructure (yellow and orange dots). The pairs of separated spots along the $\langle\bar{1}10\rangle$ direction of the Cu(111) are the first and third-order diffraction spots of the DyCu₂ surface alloy structures. It is clear that the positions of the spots are distributed symmetric along the mirror axis of the copper substrate. Moreover, the distance between each pair of diffraction spots is monotonically increased with increasing distance from the specular reflection, confirming that they are originated from mirror domains. The position of the diffraction spots corresponds to $\pm 28^\circ$ rotation of the superstructure with respect to the $\langle\bar{1}10\rangle$ direction in the real space. The diffraction pattern of the surface alloy unit cell can be represented as a $\begin{bmatrix} 2.26 \pm 0.02 & 1.20 \pm 0.02 \\ -1.20 \pm 0.02 & 1.06 \pm 0.02 \end{bmatrix}$ matrix. According to this matrix, the surface alloy structure in the real space has a lattice constant of $\sim 5.00 \text{ \AA}$ ($\sim 1.96 \times d_{\text{Cu}}$, where $d_{\text{Cu}} = 2.55 \text{ \AA}$) and is rotated $\pm 28^\circ$ with respect to the $\langle\bar{1}10\rangle$ direction of the Cu(111). All additional diffraction spots are assigned to the moiré pattern of the surface alloy, similar to the earlier case of DyAu₂/Au(111). The best agreement between the experimental and simulated moiré diffraction pattern is obtained for the close to commensurate superstructure matrix $\begin{bmatrix} 10 \pm 0.16 & 7 \pm 0.16 \\ -7 \pm 0.16 & 3 \pm 0.16 \end{bmatrix}$. The moiré superstructure has a periodicity of $\sim 22.13 \text{ \AA}$ in real space and is rotated $\pm 13.2^\circ$ with respect to $\langle 11\bar{2} \rangle$ direction of the Cu(111) substrate. This corresponds to an almost $9 \times 9 R30 \pm 13.2^\circ$ reconstruction. The top-right quarter of the image is superimposed with the diffraction pattern of both mirror domains of the moiré superstructures which are indicated by green and red dots.

5.2. Surface structure of the DyCu₂/Cu(111) surface alloy

Figure 2(b) presents a medium-size STM scan ($20 \text{ nm} \times 20 \text{ nm}$) of a single domain of the surface alloy which simultaneously reveals signatures of both the atomic as well as of the moiré structure of the surface alloy. In analogy to the DyAu₂ surface alloy, we assign the bright protrusions to the Dy atoms. The larger dark spots mark the minima of the moiré pattern formed by the atomic mismatch between the alloy layer and the substrate. The periodicity of the moiré pattern can be extracted from the FFT of the STM image shown in figure 2(d). The moiré unit cell clearly shows a hexagonal symmetry in the FFT pattern, in good agreement with our LEED analysis as discussed above. The central spots of the FFT and the six outer spots (circled yellow) correspond to the large moiré mesh, and the alloy superstructure respectively. A closer view on the relation between the atomic and moiré superstructure can be obtained in figure 2(c) which presents an enlarged area of the same scan. The hexagonal arrangement of various dark depressions and bright protrusions is clearly visible in this image. The lattice formed by Dy atoms (red rhombus) is rotated by almost 29° from the $\langle 01\bar{1} \rangle$ direction of the Cu(111), marked by black arrows. The in-plane interatomic distance of the Dy atoms is $5.2 \pm 0.3 \text{ \AA}$ indicating that the DyCu₂ alloy layer is successfully formed on Cu(111). This value is close to the 5.00 \AA observed by LEED measurement. Importantly the interatomic distance of the atoms of the alloy superstructure is not in registry with the underlying Cu(111). As a result, nearly every eight atoms of the alloy layer almost matches every nine atoms of the substrate. This means an almost 11.2% mismatch between the topmost alloy layer and the substrate, leading to the formation of a non-commensurate registry with the substrate and the corresponding moiré pattern. The latter is evidenced by the area of dark contrast in figure 2(c). Similar to the DyAu₂ sample, each moiré minimum reveals a slightly different contrast in contrast and are not identical, confirming the non-commensurate nature of the alloy layer. The length of the moiré unit cell is measured to be $21.4\text{--}22.8 \text{ \AA}$ and rotated by 45.2° with respect to the $\langle 01\bar{1} \rangle$ direction of the Cu(111). This periodicity is in very good agreement with the proposed moiré



unit cell calculated in our LEED analysis. An STM image that reveals both mirrored domains, is provided in figure SI.4 (<https://stacks.iop.org/NJP/24/033048/mmedia>).

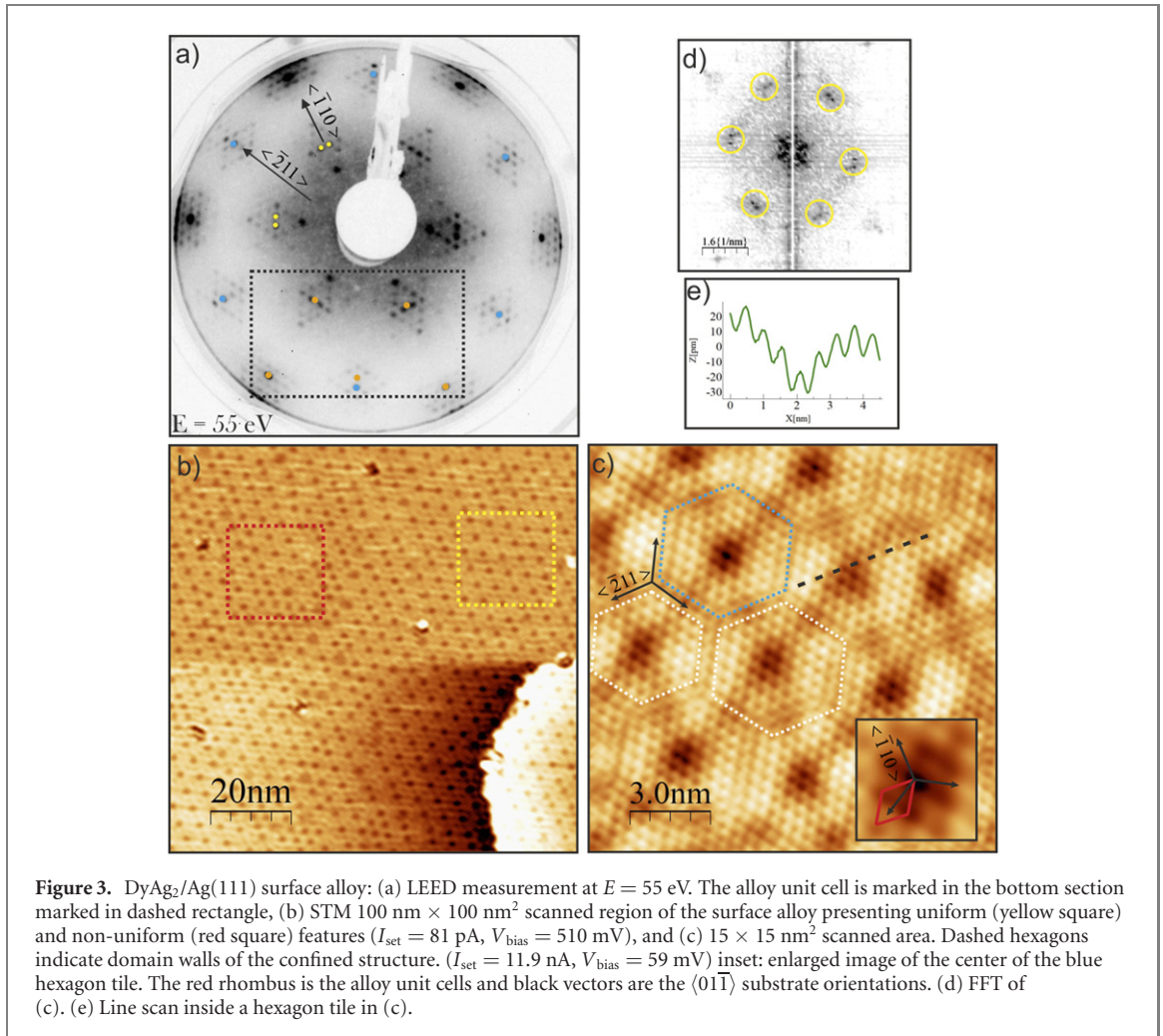
6. DyAg₂/Ag(111)

6.1. Periodic order of the DyAg₂/Ag(111) surface alloy

The LEED pattern of the DyAg₂ surface alloy, presented in figure 3(a), is significantly different compared to the above-discussed DyCu₂ and DyAu₂. This severely complicated the unambiguous interpretation of the LEED data. For instance, the first order LEED spots of the DyAg₂/Ag(111) superstructure (marked as yellow points in figure 3(a)) are split mirror symmetrically with respect to the $\langle 01\bar{1} \rangle$ direction of the Ag(111) substrate, similar to the DyCu₂/Cu(111). However, no such splitting is observed for the corresponding (11) superstructure spots along the $\langle 11\bar{2} \rangle$ direction (see the head of the arrow along this direction in figure 3(a)). To resolve this apparent contradiction, we immediately turn to our local STM study to determine the structural parameters of the atomic and mesoscopic superstructure of the DyAg₂/Ag(111) surface alloy.

6.2. Surface structure of the DyAg₂/Ag(111) surface alloy

We start our structural analysis of the DyAg₂ surface alloy with the overview STM scan ($100 \text{ nm} \times 100 \text{ nm}$) in figure 3(b). Similar to the DyAu₂ and DyCu₂ cases, we observe an array of dark features which we assign again to the moiré structure. However, a careful inspection reveals that these dark features cover the surface non-uniformly. In certain regions, we find a nearly uniformly-spaced grid of these features (marked by the yellow square), in others (marked red displays), the dark features are irregularly distributed. This observed non-uniformity within a single terrace is an indication that the DyAg₂ alloy does not grow uniformly over the Ag(111) substrate. Upon close inspection in the atomically resolved 15×15 nm² STM image (figure 3(c)), we realize that the surface consists of neighboring hexagonal tiles with surface areas varying between $15.4\text{--}21.8$ nm² and each tile includes exactly one dark moiré valley feature. Interestingly, after scanning several different regions of the sample, there seems to be no periodic order in the distances between these tiles as well as in the tile size. However, the boundaries of the tiles are all aligned along the



$\langle 11\bar{2} \rangle$ substrate directions. The positions of the Dy atoms appear as dark depressions in this scanned image due to the applied bias voltage. Similar to other surface alloys in the previous sections, the DyAg₂ surface alloy unit cell has a hexagonal lattice with an average unit cell vector length of $5.2 \pm 0.3 \text{ \AA}$ that is rotated almost 30° with respect to the substrate's $\langle 01\bar{1} \rangle$ orientation, creating $\sim 3.8\%$ atomic mismatch between the alloy layer and Ag(111) substrate. At first glance, this unit cell is in contrast to our LEED data, where we observed two sets of first-order diffraction spots (see figure 3(a)). However, the FFT of this atomically resolved STM image (figure 3(d)) clearly reveals double spots as well as additional intensity-modulated spots, very similar to diffraction spots observed in our LEED experiment. This point will be addressed in more detail in the discussion section. Using these structural parameters, we propose that the unit cell of the DyAg₂/Ag(111) surface alloy can be described by the superstructure matrix
$$\begin{bmatrix} 2.08 \pm 0.02 & 1.04 \pm 0.02 \\ -1.04 \pm 0.02 & 1.04 \pm 0.02 \end{bmatrix}.$$
 The corresponding first and second-order diffraction spots are superimposed as orange dots onto the experimental LEED pattern. In addition, we find that the surface alloy structure discommensurates at the edges of the tiles. As a result, the adjacent tiles are anti-phased, i.e. shifted by half an alloy unit cell up or down respectively. Besides, discommensuration generates domain wall boundaries around the tiles that have rectangular lattices and an average width of $4.5\text{--}4.8 \text{ \AA}$ (see supplementary information (SI) 1). This distance is significantly shorter than the measured lattice size of the surface alloy unit cell and implies that the atomic units of these sites are not fully relaxed. Careful examination of the structure within the tiles confirms no additional local superstructure. Moreover, by creating a distance map of this scan, we did not find any significant lattice distance variation within the tiles (details are provided in SI.2).

7. Models and discussion

To have a better understanding of the surface alloy structure as well as the moiré pattern formation, we present hard sphere space filling ball models of all three surface alloys in figure 4, which are constructed based on our LEED and STM findings. We present in table 1 the parameters of the alloy unit cell, and the

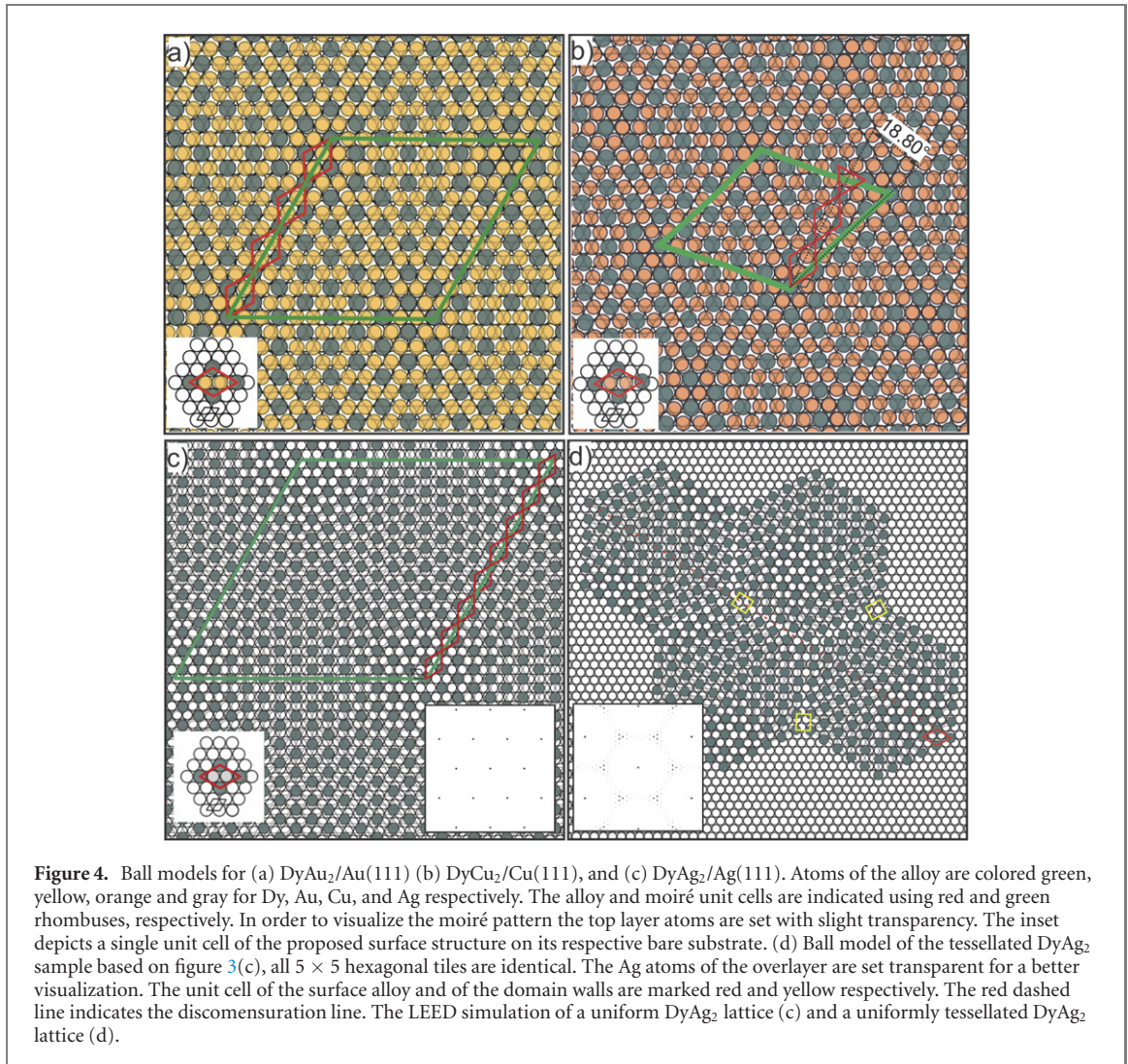


Figure 4. Ball models for (a) DyAu₂/Au(111) (b) DyCu₂/Cu(111), and (c) DyAg₂/Ag(111). Atoms of the alloy are colored green, yellow, orange and gray for Dy, Au, Cu, and Ag respectively. The alloy and moiré unit cells are indicated using red and green rhombuses, respectively. In order to visualize the moiré pattern the top layer atoms are set with slight transparency. The inset depicts a single unit cell of the proposed surface structure on its respective bare substrate. (d) Ball model of the tessellated DyAg₂ sample based on figure 3(c), all 5 × 5 hexagonal tiles are identical. The Ag atoms of the overlayer are set transparent for a better visualization. The unit cell of the surface alloy and of the domain walls are marked red and yellow respectively. The red dashed line indicates the discommensuration line. The LEED simulation of a uniform DyAg₂ lattice (c) and a uniformly tessellated DyAg₂ lattice (d).

Table 1. Realspace lattice parameters of surface alloy superstructures, moiré unit cells, and the calculated moiré unit cell parameters using the Hermann model. For Hermann model, the mean experimental values of surface alloy parameters obtained from LEED (values outside brackets) were used. Angles α and γ are with respect to the substrate's $\langle 11\bar{2} \rangle$ and $\langle 01\bar{1} \rangle$ orientations respectively. The lattice parameters inside the brackets are obtained from a spot profile analysis of the experimental LEED data.

Sample	Substrate	LEED				STM		Hermann model	
		Surface alloy		Moiré		Moiré		Moiré	
	a_{sub} (Å)	a_{alloy} (Å)	$\pm\alpha$ (°)	$a_{\text{moiré}}$ (Å)	$\pm\gamma$ (°)	$a_{\text{moiré}}$ (Å)	$\pm\gamma$ (°)	$a_{\text{moiré}}$ (Å)	$\pm\gamma$ (°)
DyAu ₂	2.88	5.41(5.47 ± 0.08)	0(0 ± 0.8)	37.57(31 ± 5)	0(0 ± 9)	36.0–37.0	0	37.03	0
DyCu ₂	2.55	5.00(4.95 ± 0.05)	2(1.8 ± 0.6)	22.13(25 ± 2)	16.8(16 ± 4)	21.4–22.8	16.8	21.04	16.74
DyAg ₂	2.89	5.22(5.26 ± 0.04)	0(0 ± 0.5)	NA	NA	NA	NA	70.37	0

moiré unit cell for each sample which are extracted from the superstructure matrixes determined experimentally. In addition, we have included calculated values for the structural parameters of the moiré unit cell based on a mathematical method for two mismatched hexagonal lattices provided by Hermann [43].

We start with the simplest structure, i.e., the one of the DyAu₂ surface alloy presented in figure 4(a). The inset provides a structural model of the atomic unit cell of the surface alloy (red rhombus) placed on top of the Au(111) substrate (empty circles). The unit cell includes one Dy atom (green) and two Au atoms (yellow) which are placed equidistantly on the long diagonal of the rhombohedral unit cell. This stoichiometric configuration is common for all RE/NM surface alloys reported so far [23–25].

The unit cell of the DyAu₂ surface alloys is rotated by 30°, which is the identical orientation with respect to the substrate lattice as observed for a $\sqrt{3} \times \sqrt{3}R30$ superstructure. This structure is frequently observed for heavy metal/NM surface alloys on NM fcc(111) substrates. The only striking difference is that the

interatomic distances in the DyAu₂ surface alloy are almost 1.08 times larger than the lattice constant of Au(111). The lattice expansion was estimated from the superstructure parameters of the superstructure analysis of our LEED data, see table 1. This ultimately leads to the formation of a non-commensurate $\sim 1.08\sqrt{3} \times 1.08\sqrt{3}R30^\circ$ superstructure of the DyAu₂ surface alloy on the Au(111) surface. Importantly, this mismatch between the atoms in the alloy layer and the substrate layer is responsible for local variation of the Dy positions within the moiré minima in STM. Similarly, continuous change in the FCC/HCP-like adsorption site within the moiré unit cell generates the contrast variation that we observe inside the moiré unit cell. In terms of alloy unit cell and moiré periodicity, DyAu₂ surface alloy is identical to the incommensurate NaAu₂ surface alloy [7, 8]. In terms of alloy unit cell and moiré periodicity, DyAu₂ surface alloy is identical to the NaAu₂ and GdAu₂ surface alloy [7, 8, 26]. This is rather surprising since the valence electronic structure of both elements are significantly different. However, at the same time, the atomic radii of Na, Gd, and Dy are rather similar [44]. Hence, further studies of the electronic states of different classes of surface alloys are essential to disentangle the different roles of electronic and steric effects for their structure formation of surface alloys. The ball model provides a clear visualization of the lattice mismatch between the alloy and the substrate. The moiré unit cell (figure 4(a) green rhombus) is illustrated according to the Hermann model, based on the nearest neighbor distance of the alloy layer, and denotes its non-coinciding character. The size of this unit cell is in good agreement with our experimental result.

Next, we turn to the DyCu₂ surface alloy. Our LEED analysis indicates the existence of two superstructure domains mirrored along the substrate high symmetry directions, marking the DyCu₂ surface alloy as the only RE/NM surface alloy with 1:2 (RE:NM) stoichiometry, that is not oriented along its substrate's $\langle 11\bar{2} \rangle$ direction. Figure 4(b) shows the corresponding atomic model structure of a single mirror domain of the DyCu₂ surface alloy. According to the LEED superstructure matrix analysis, the interatomic distance of the alloy layer is 2.88 Å, which is 1.13 times larger than d_{Cu} . The corresponding lattice expansion of the first layer is hence significantly larger for the DyCu₂ surface alloy compared to the DyAu₂ surface alloy. This distinct difference is attributed to the different atomic sizes of the Cu and Au substrate atoms, which is reflected in its lattice constant as well, refer table 1. The mesoscopic moiré unit cell of the DyCu₂ alloy is rotated by 18.8° with respect to the surface alloy lattice vector (marked in figure 4(b)), which agrees both with the STM results and the calculated Hermann model. This large angle is the direct result of the $\pm 28^\circ$ rotation of the alloy layer with respect to the substrate $\langle \bar{1}10 \rangle$ orientation, which we observe in our experimental data. As a result, the moiré features have a shorter periodicity compared to the DyAu₂ case. Angle mismatches between the surface alloy lattice vector and moiré lattice vectors have previously been observed for RE/NM surface alloys such as LaAu₂/Au(111), where a smooth variation of the azimuthal $\pm 4^\circ$ misalignment of the moiré and the alloy lattice is measured and is explained as the mismatch between the alloy layer and its substrate (7.6%) [24]. However, this angle is substantially larger for the DyCu₂ case and is not merely a misalignment. The clear observation both in LEED and STM point out a different atomic structure of this surface alloy, compared to its related alloy family. It is possible that in addition to rotation the alloy layer minimizes its excessive energy by straining its lattice locally so that the corner Dy atoms of the moiré unit cell match the substrate lattice in the ball model. However, using only the STM result, it is not possible to directly confirm this argument.

Finally, we consider the most complex case, the DyAg₂ surface alloy. Considering the results of our LEED superstructure matrix analysis, the expansion of the DyAg₂/Ag(111) alloy layer with respect to its substrate is only 3.8% which is significantly smaller than of the DyAu₂/Au(111). Figure 4(c) presents the model which is constructed based on the LEED matrix for the DyAg₂ surface alloy. The large green rhombus is the moiré unit cell that is based on the predicted Hermann model. Nonetheless, our STM data reveal that the DyAg₂ surface alloy does not follow this simple model. Instead, the structure tessellates in the form of large hexagonal tiles, which are shifted with respect to each other by half an alloy unit cell, creating anti-phase domains and boundary walls (figures 3(c) and 4(d)). Based on our experimental findings, we have simulated LEED models by calculating the structure factors of uniform (figure 4(c)) and tessellated (figure 4(d)) DyAg₂ superstructures. The tessellated superstructure reveals spot splitting as well as additional intensity-modulated spots (inset of figures 4(d) and SI.3), which indicates that the co-existence of multiple anti-phase domains caused by the surface tessellation is the genuine reason for the spot-splitting in our LEED pattern (see figure 3(a)) [45]. Moreover, this can at least partially explain the intensity modulation that we observe in the LEED result as well. Spot-splitting has been previously reported for similar anti-phase domain wall systems [46–50]. The reason for observing the splitting in LEED is the presence of a large number of anti-phase domains within the incident electron beam spot size on the sample which leads to the interference between the scattering vectors of the overlayer domains [45, 50]. For example, in a kinematical calculation study, Zeppenfeld *et al* show that in any domain wall system of a $\sqrt{3} \times \sqrt{3}R30^\circ$ superstructure, the first and second-order spots along the $\bar{1}\bar{M}$ direction splits and the amount of atomic relaxation within the walls only influences the intensity of the spots [46]. Similarly, we

observe the splitting of the first order alloy spots along $\langle 01\bar{1} \rangle$ both in our LEED data as well as our simulation, while the spots of the alloy superstructure along the $\langle 11\bar{2} \rangle$ direction shows no sign of any spot splitting. The splitting of the second-order spots along the $\langle 01\bar{1} \rangle$ is not easy to observe because of the high contrast at this point, which could be due to the additional moiré modulations. Also due to the tessellation, we were not able to resolve a complete moiré cell in the STM Data. The average experimental lattice size of the alloy superstructure discussed in the result section is very close to the one measured for the bulk tetragonal crystal of the DyAg₂ alloy (~ 5.23 Å), using x-ray and neutron diffraction methods [51]. This is not the case for the GdAu₂, which has nearly a similar bulk alloy lattice constant [51]. Considering the almost identical lattice constants of silver and gold crystals, we see different expansion ratios of the alloy layer. Thus, we can argue that the DyAu₂ alloy possibly reduces its surface energy by uniformly relaxing its in-plane lattice stress, i.e., by increasing the interatomic distance within the alloy layer. In contrast, the DyAg₂ structure reduces its surface free energy not only by a marginal increase of the interatomic distance of the periodic structure within the hexagonal tiles but by tessellation and the formation of domain walls between the hexagonal tiles [52]. This behavior points out to a possibly stronger interaction between the DyAg₂ surface alloy layer and the Ag(111) substrate. Despite the lack of uniform long-range atomic ordering, each hexagonal tile enclosed by stacking-fault domains walls (marked by rectangular yellow cells in figure 4(d)) reveals a locally identical ordered structure. A similar study on GdAg₂ surface alloy identifies local variation of the unit cell size (1% strain) and change of orientation for each relative moiré pattern. This study identifies similar local formation of strained hexagonal tessellation at low alloy formation temperature [27]. Varying the temperature of the substrate during sample preparation does not affect our results (see SI.6), which suggests that this structure is perhaps the only stable result that can be achieved for the DyAg₂ surface alloy on Ag(111). The surface alloy formation is hence governed by a delicate balance between the in-plane interatomic forces of the alloy layer and the electronic interaction i.e. bonding between the substrate and the top layer atoms. In other words, the atoms of the alloy layer favor settling on their energetically preferred adsorption sites to maintain a locally near-commensurate registry despite the resulting in-plane strain of the alloy layer. In the case of DyAu₂, interatomic bonds of the alloy layer endure this strain, so that a uniform structure with minimum ruptures is maintained. The DyCu₂/Cu(111) can be considered an intermediate case, where the interaction of the substrate with the alloy overlayer is more pronounced and in this particular case results in mirrored domains. In the case of the DyAg₂, the structure grows in its preferred configuration (within the tiles) until the accumulated strain is released by the formation of a domain wall. A more comprehensive understanding of the interplay between these forces in structure formation requires *ab initio* calculation schemes that can identify the most stable structure(s) with the lowest cohesive energy.

8. Conclusion

In conclusion, we investigated the atomic and mesoscopic structure of three Dy-based surface alloys formed on the fcc(111) NMs Au, Cu, and Ag. The structure of each system is characterized using STM and LEED. We find a non-commensurate relation between the alloy and its respective substrate for all three samples. Each system exhibits a different kind of mesoscopic moiré structure, suggesting a different behavior for the substrate/overlayer interaction. Both DyAu₂/Au(111) and DyCu₂/Cu(111) surface alloy systems show homogeneous moiré structures with non-identical valley contrasts in STM, but only the one of the former is aligned with the surface alloy unit cell, while for the latter it deviates substantially from the surface alloy orientation. In the case of the DyAg₂, we find a complex tessellation of the alloy overlayer consisting of anti-phase domains in form of hexagonal tiles that are surrounded by boundary walls, which locally break the general translation symmetry of the surface alloy layer. Crucially, the formation of anti-phase domains in this sample is the consequence of the in-plane strain within the DyAg₂ surface.

Overall, our study has demonstrated that the local atomic, as well as the mesoscopic structure of RE–NM surface alloys, are governed by a complex interplay between the intra-plane and inter-plane interactions of alloy and substrate due to lattice constant variation, mediated by strain. Lattice strain is justified by the significantly different atomic sizes of RE and NM atoms. Achieving active control of these competing processes offers great potential to design moiré patterns with complex spin-dependent band structures and hence to template nanostructures for site-specific absorption of (organic) adsorbate, or the formation of heteromolecular nanostructures [53].

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Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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