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Determination of the parameters of semiconducting CdF₂:In with Schottky barriers from radio-frequency measurements

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Physical properties of semiconducting CdF₂ crystals doped with In are determined from measurements of the radio-frequency response of a sample with Schottky barriers at frequencies 10–10⁶ Hz. The dielectric constant, the dc conductivity, the activation energy of the amphoteric impurity, and the total concentration of the active In ions in CdF₂ are found through an equivalent-circuit analysis of the frequency dependencies of the sample complex impedance at temperatures from 20 to 300 K. Kinetic coefficients determining the thermally induced transitions between the deep and the shallow states of the In impurity and the barrier height between these states are obtained from the time-dependent radio-frequency response after illumination of the material. The results on the low-frequency conductivity in CdF₂:In are compared with submillimeter (10¹¹–10¹² Hz) measurements and with room-temperature infrared measurements of undoped CdF₂. The low-frequency impedance measurements of semiconductor samples with Schottky barriers are shown to be a good tool for investigation of the physical properties of semiconductors.

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I. INTRODUCTION

CdF₂ is an ionic dielectric with a wide band gap and only one dipole-active lattice mode centered near 6×10^{12} Hz,¹ which provides lower frequency (static) dielectric constant $\epsilon \cong 8$.^{1,2} CdF₂ crystals doped with In manifest semiconductor properties after additive coloration process, when a part of the interstitial F¹⁻ ions leaves the crystal. At a quite low temperature in CdF₂:In crystals half of the In ions reveals a completely ionized state In³⁺ and the other half exhibits an In¹⁺ state, with two valence electrons.^{3,4} Since, due to the Coulomb interaction, a localization of two electrons at one orbital is energetically not profitable, a compensating local lattice distortion appears around the In¹⁺ ions, the ions being moved along a fourth order axis into a neighboring cell of eight F¹⁻ ions not occupied by a Cd ion.⁵ Consequently, a transition of the In ion from In³⁺ state into the In¹⁺ state requires overcoming a significant potential barrier between these states. Thus, In¹⁺ impurities in CdF₂ form a deep energy level E_{deep} , which is similar to the DX centers in typical semiconductors.^{6,7} A fraction of electrons is captured by In³⁺ ions, forming a hydrogen state (In³⁺ + e_{hydr}), a shallow donor level E_{sh} being the basic reason that the CdF₂:In reveals semiconducting properties. The relative concentrations of the shallow In³⁺ + e_{hydr} and the deep In¹⁺ centers depend on the temperature. Since for a transition from one state to another the electron has to overcome a capture barrier E_{cap} the upper state is metastable. The energy of the states measured from the bottom of the conducting band are $E_{\text{deep}} = 0.25$ eV (Ref. 5) and $E_{\text{sh}} \cong 0.1$ eV.⁸ The electrons of the DX centers can be transferred to the shallow state either by light irradiation or by temperature. The changing of the

DX-center state leads to a change of polarizability and, consequently, to a local change of the refractive index. This fact allows one to use the metastable shallow states to write reversible phase holograms. The efficient writing of such holograms in the semiconducting CdF₂ doped with In or Ga has been demonstrated in Refs. 9 and 10.

Traditionally, investigations of the semiconducting transport properties of doped CdF₂ were carried out using ohmic contacts. The technique to produce such contacts is quite complicated and often is a kind of art. In this paper we report on the radio-frequency investigations of CdF₂:In which were carried out without ohmic contacts. We have determined the dielectric constant, the temperature dependencies of the dc conductivity and of the ion concentration on the donor level, the activation energy of impurities E_a , the total concentration of the active In ions N , the barrier height E_{cap} , and the values of the kinetic coefficients which describe the speed of the thermally induced transfers between the deep and the shallow states of the In ions in the CdF₂ matrix. All these parameters have been defined from low frequency (10–10⁶ Hz) measurements of the complex impedance of thin plane-parallel CdF₂:In samples with metallic electrodes which were either sputtered on their surfaces or just brought into contact with the surfaces. This method is the basis of our previous study.¹¹

II. SAMPLES AND EXPERIMENT

In most of the experiments we used a plane-parallel sample of CdF₂ with an InF₃ concentration in the raw material of 0.02 mole %. This concentration of the In impurities gives the sample a red-brownish color. The absorption coefficient α for light with a wavelength of $\lambda = 488$ nm has been

measured to be of 50 cm^{-1} at room temperature. Control experiments have been also performed for an undoped CdF_2 sample. Both surfaces of the sample have been covered by gold electrodes made by plasma sputtering. The area of each electrode was 20 mm^2 and the electrode thickness was about 10 nm . The light transmittance through this electrode for $\lambda = 488 \text{ nm}$ was about 50%. For the experiments, where we used electrodes isolated from the sample by mica, the same electrodes have been sputtered on two pieces of mica, 35μ thick each. For the experiments with Teflon isolating linings we used polished brass electrodes of 18.5 mm^2 . Finally, additional measurements were also performed for a sample with contacts formed by silver paint.

The sample was placed on a copper cold finger of a helium flow cryostat Helix CTI Cryogenic model 22. The temperature of the finger was monitored and controlled by a Lake Shore 330 temperature controller.

An argon laser beam with $\lambda = 488 \text{ nm}$ was widened by a lens to illuminate the complete sample surface through a window in the cryostat. The laser intensity could be continuously regulated by changing the gas discharge current in the laser tube, and by an external variable attenuator.

The wires from the electrodes through the cryostat terminals were connected with an LCR meter HP4284A. This analyzer covers a frequency range from 20 to 10^6 Hz . Usually an amplitude ac voltage $V_s = 0.1 \text{ V}$ and zero bias have been used. Results of the complex impedance of a sample with electrodes Z were obtained as an equivalent capacitance C_p and an equivalent conductance G_p (i.e., the complex conductance is $1/Z = G_p + i\omega C_p$, where ω is the angular frequency). Additional experiments have been carried out for frequencies extending to 320 MHz. In these experiments an HP4191A analyzer with working range of 1 MHz–1 GHz has been utilized.¹²

III. RESULTS AND DISCUSSION

A. Schottky barriers and a nonhomogenous layered Maxwell-Wagner capacitor model

Typical results of our measurements of the frequency dependencies of C_p , and G_p/ν for the sample with gold electrodes are plotted in Fig. 1 ($\nu = \omega/2\pi$). These measurements were performed with the sample cooled in darkness. They clearly show the signature of a relaxation process for frequencies 20 Hz to 1 MHz, the relaxation frequency ν_p strongly depending on the temperature. When the temperature changes from 110 to 200 K, ν_p rises by a factor of 10 000.

Since in a cubic electronic semiconductor such as $\text{CdF}_2:\text{In}$ it is very difficult to imagine a low frequency microscopic mechanism for this relaxation, we propose that a macroscopic Maxwell-Wagner relaxation process accounts for this behavior. (This statement has been strongly supported by the experiments described below, where isolating layers between sample and electrodes have been used.) The Maxwell-Wagner relaxation is a quite common feature for a nonhomogenous layered capacitor.¹³ The layered structure results from the formation of Schottky barriers in the regions

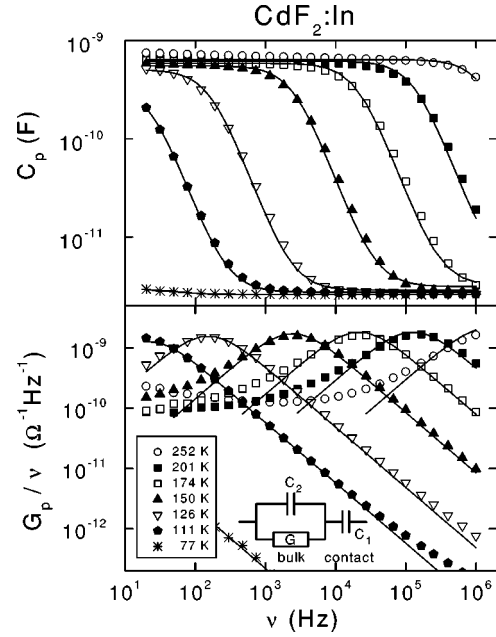


FIG. 1. Frequency dependencies of C_p (upper panel) and G_p/ν (bottom panel) for a sample with gold-sputtered electrodes at various temperatures. The points are experimental data, the solid lines are least square fits by formulas (3) and (4), deduced from the equivalent circuit indicated in the lower panel.

of semiconducting $\text{CdF}_2:\text{In}$ close to the metal electrodes.¹⁴ If the electron work function φ_m in a metal is higher than in an electronic semiconductor φ_s , the electron concentration in the contact region of the semiconductor is suppressed, and a depletion layer appears. Its thickness is equal to

$$d_c = \sqrt{2\varepsilon\varepsilon_0 V_c / en_d}, \quad (1)$$

where e is the electron charge, $V_c = (\varphi_m - \varphi_s)/e$ is the contact potential difference, n_d is the donor concentration (total ionization of donors is supposed), and ε and ε_0 are the dielectric constants of the semiconductor and of the vacuum.

Thus, the sample with two electrodes may be considered as a structure of three condensers in series: two of them are formed by the depletion layers with very small conductivity, and the third (the middle) one represents the bulk material with the real sample conductivity. If the material of both electrodes are the same and both sample surfaces had the same treatment, then the two depletion-layer capacitors with capacity C' may be presented in the equivalent circuit scheme as one capacitor with capacitance $C_1 = C'/2$. The rest of the sample may be considered as a capacity C_2 with a parallel active conductivity G . Overall we arrive at the equivalent circuit indicated in Fig. 1. The impedance of this scheme is

$$Z = \frac{1}{i\omega C_1} + \frac{1}{G + i\omega C_2} \quad (2)$$

and the complex conductance is $1/Z = G_p + i\omega C_p$, where

$$G_p = \frac{C_1^2 \omega^2 G}{\omega^2 (C_1 + C_2)^2 + G^2}, \quad (3)$$

TABLE I. Experimental values of ϵ and σ of the bulk material obtained from the radio-frequency measurements with three different kinds of linings at the electrodes: (1) Teflon linings, (2) mica linings, and (3) without any linings (marked as ‘‘Schottky barrier’’). The values are presented for three temperatures. The experimental accuracy for ϵ is 30% for the Teflon linings, 20% for the mica linings, and 10% for the measurements without linings. The experimental accuracy for σ is 30% for the Teflon linings, 10% for the mica linings, and 4% for the measurements without linings.

T(K)	Teflon			Mica			Schottky barrier		
	109	124	148	109	124	148	110.5	125.3	149.4
ϵ	8.7	9.4	10.9	10.2	10.3	11.0	7.3	7.7	8.3
$\sigma(\Omega^{-1} \text{ cm}^{-1})$	1×10^{-8}	1×10^{-7}	1.8×10^{-6}	1.4×10^{-8}	1.3×10^{-7}	2.2×10^{-6}	1.3×10^{-8}	1.2×10^{-7}	2.2×10^{-6}

$$C_p = \frac{C_1[G^2 + \omega^2(C_1 C_2 + C_2^2)]}{\omega^2(C_1 + C_2)^2 + G^2}. \quad (4)$$

An analysis of Eqs. (3) and (4) shows that at $\omega \rightarrow 0$

$$C_p \rightarrow C_{p0} = C_1, \quad (5)$$

$$G_p \rightarrow G_{p0} = 0, \quad (6)$$

and at $\omega \rightarrow \infty$

$$C_p \rightarrow C_{p\infty} = C_1 C_2 / (C_1 + C_2), \quad (7)$$

$$G_p \rightarrow G_{p\infty} = G C_1^2 / (C_1 + C_2)^2. \quad (8)$$

If $C_1 \gg C_2$ (that usually holds for the Schottky barriers), then

$$C_{p\infty} = C_2, \quad (9)$$

$$G_{p\infty} = G. \quad (10)$$

Thus, the high frequency limit represents the bulk material parameters, while the low frequency one depends strongly on the contact phenomena. In addition, $C_p(\omega_p) = (C_{p\infty} + C_{p0})/2$, where the relaxation frequency is

$$\omega_p = 2\pi\nu_p = G/(C_1 + C_2). \quad (11)$$

The frequency dependencies of C_p , and G_p/ν calculated from formulas (3) and (4) are shown in Fig. 1 as solid lines. The parameters C_1 , C_2 , and G have been fitted with the least square method. As can be seen from Fig. 1, all the characteristic features of the experimental curves are well described by the formulas of the Maxwell-Wagner model. For higher temperatures, at low frequencies deviations of experimental data and fits show up in G_p/ν . They can be ascribed to a small, but nonzero conductivity of the depletion layers, which for very low frequencies would lead to a $1/\nu$ divergence. We note that C_{p0} and $C_{p\infty}$ are almost temperature independent. Consequently, the strong temperature dependence of the relaxation frequency $\nu_p = G/2\pi(C_1 + C_2)$ is due to the temperature dependence of G . Using the temperature dependencies of the fitting parameters $C_2(T)$ and $G(T)$, we have calculated the real part of the dielectric permittivity $\epsilon'(T) = C_2(T)d/(\epsilon_0 S)$ and the conductivity $\sigma(T) = G(T)d/S$ of the bulk material (S is the electrode area and d is the sample thickness).

Since the frequency dependencies of $C_p(\omega)$ and $G_p(\omega)$ [Eqs. (3) and (4)] have the same shape as the frequency dependencies of ϵ' and $\sigma = \epsilon''\epsilon_0\omega$ for the Debye relaxation of homogeneous dielectrics with gain $\epsilon'_{\text{static}} \approx 2000$ (here ϵ' and ϵ'' are real and imaginary parts of ϵ), we have conducted two control experiments for the CdF₂:In sample with electrodes isolated from the sample by 55 μ thick Teflon ($\epsilon_{\text{Teflon}} = 2$) and 35 μ thick mica ($\epsilon_{\text{mica}} = 8$) layers. In these experiments no Schottky barriers are formed, and one can directly calculate the electrode capacitances $C' = 2C_1 \approx 2C_{p0}$ of the Maxwell-Wagner layered system. We have found that the value of C_1 for Teflon is two orders of magnitude smaller and for mica it is one order of magnitude smaller than C_{p0} in the experiments with sputtered gold electrodes (2.5 and 20 pF, respectively), while C_2 remains at 3–4 pF. Accordingly, for a fixed temperature the values of C_{p0} decrease and the characteristic relaxation frequencies increase by 2 (1) orders of magnitude for Teflon (mica) linings. Such a behavior is expected in the case of a Maxwell-Wagner relaxation [see Eq. (11)], while for the Debye relaxation, the characteristic frequency of which does not depend on the electrode capacitances, one would obtain other, more complex, frequency dependencies of C_p and G_p due to a superposition of the Maxwell-Wagner relaxation and the Debye relaxation.

The evaluated values of ϵ' and σ of the bulk material are presented in Table I for three temperatures together with the values determined from the measurements with Schottky barriers. Table I documents that ϵ' and σ determined through the Maxwell-Wagner equivalent circuit analysis coincide with each other within experimental accuracy for all temperatures. This again proves the validity of the Maxwell-Wagner relaxation as a model for the treatment of our results.

According to the weak temperature dependence of $C_{p\infty}$, the capacity C_2 does not depend significantly on temperature: at temperatures between 70 and 300 K $C_2 \approx 3$ pF, and consequently $\epsilon \approx 8$ (at lowest $T = 25$ K, $\epsilon \approx 7$). The same values of ϵ have been determined for an undoped sample. Contactless measurements made in the submillimeter frequency range give the same values for doped and pure CdF₂ as well.²

B. Temperature and frequency dependencies of the conductivity

The temperature dependence of the conductivity obtained by fitting the experimental results $C_p(\omega)$, $G_p(\omega)$ with the Maxwell-Wagner model is shown in Fig. 2. For temperatures

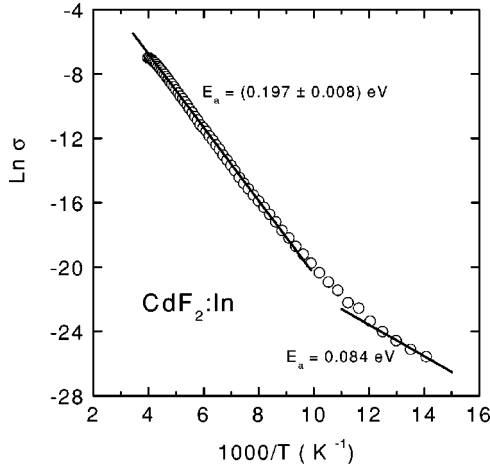


FIG. 2. Arrhenius plot of the temperature dependence of the conductivity obtained by the fitting of the experimental curves $C_p(\nu)$ and $G_p(\nu)$ for different temperatures with the Maxwell-Wagner model, Eqs. (3) and (4).

100–250 K the temperature dependence of the conductivity is well described by a thermally activated behavior

$$\sigma(T) \propto \exp(-E_a/k_B T), \quad (12)$$

with an activation energy $E_a = 0.197 \pm 0.008$ eV. This value, being actually “an weighted-mean activation energy” of the deep E_{deep} and the shallow E_{sh} states of the In ions, takes into account both the electron transfers from the deep and the shallow levels into the conduction band, and the process of transferring electrons between the deep and the shallow levels. As can be seen from Fig. 2, at low temperatures the slope of the $\ln \sigma(1/T)$ curve decreases, corresponding to the decrease in the electron replenishment of shallow levels from the deep ones. The value of E_a , consequently, should approach the activation energy of the shallow state at quite low temperatures. This behavior has been indeed observed in Ref. 15 at temperatures 40–80 K.

Since the electron mobility μ in CdF_2 depends only weakly on temperature [at the temperatures 70–300 K, $\mu \approx 15 \text{ cm}^2 \text{V}^{-1} \text{ s}^{-1}$ (Ref. 16)], we can calculate the electron concentration n_e in the conduction band. For example, for $T = 150$ K one finds $n_e = \sigma/e\mu = 1 \times 10^{12} \text{ cm}^{-3}$. For this value of the electron concentration the total effective concentration of the In ions with the activation energy of $E_a = 0.197$ eV, should be $N = n_e \exp(E_a/k_B T) = 4 \times 10^{18} \text{ cm}^{-3}$, that coincides with $N = (3.5 \pm 0.7) \times 10^{18} \text{ cm}^{-3}$ obtained from our absorption coefficient data $\alpha \approx 50 \text{ cm}^{-1}$ at room temperature for $\lambda = 488$ nm.

Figure 3 compares our results on the low-frequency conductivity in $\text{CdF}_2:\text{In}$ with the measurements in the submillimeter range carried out on a different In-doped sample (possibly with slightly different In content) at 10 and 300 K (Ref. 2) and with room-temperature infrared measurements in undoped CdF_2 .¹ The radio-frequency experimental data shown in Fig. 3, extended up to 1 GHz, were obtained on the same sample as the results of Fig. 1, but with contacts made from silver paint. The dielectric-loss results up to 1 MHz (not shown) are similar to those shown in Fig. 1. In the conduc-

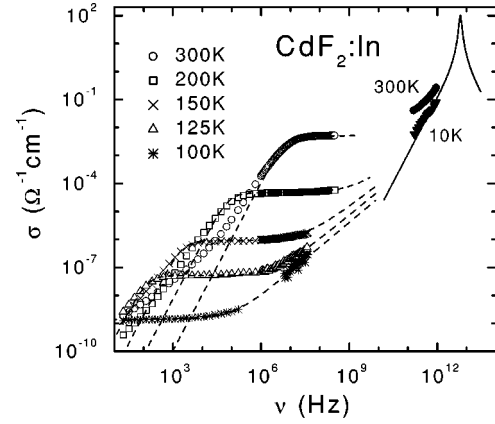


FIG. 3. Panorama spectra of the conductivity of $\text{CdF}_2:\text{In}$ with silver-paint electrodes for various temperatures (note the log-log scale). Open symbols: audio and radio-frequency measurements, solid symbols: submillimeter wave measurements (Ref. 2), solid line: infrared measurements of undoped CdF_2 (Ref. 1). Dashed lines are calculated with the equivalent circuit shown in Fig. 1 with an additional UDR element for the bulk response (Refs. 19,20).

tivity representation of Fig. 3, the loss peaks are transformed into a steep increase of $\sigma(\omega)$, followed by the approach of a nearly frequency-independent plateau value. The initial increase of $\sigma(\omega)$ can be attributed to the shorting of the high resistance of the depletion layers by its capacitance. Only when the plateau region is reached is the intrinsic bulk response measured. At lower temperatures, following this plateau, $\sigma(\omega)$ starts to increase again. Such a behavior is often observed in amorphous and doped semiconductors and usually ascribed to hopping conductivity of localized charge carriers.¹⁷ It can be parametrized by the so-called “universal dielectric response” (UDR): $\sigma = \sigma_{\text{dc}} + \sigma_0 \omega^s$, $s < 1$.¹⁸ The dashed lines in Fig. 3 have been calculated using the equivalent circuit of Fig. 1, with an additional UDR element (including its contribution to σ'' via the Kramers-Kronig relation¹⁸) connected in parallel to G and C_2 .^{19,20} In this way the general behavior of the experimental spectra can be satisfactorily reproduced. Values of s between 0.8 and 0.88 were obtained, which lies in a reasonable range for hopping conduction.¹⁷ The deviations showing up at low frequencies, again indicate a nonzero conductivity of the depletion layers. Possibly the increase of $\sigma(\omega)$ observed in the submillimeter region can also be taken into account by the UDR. Up to now UDR behavior only rarely has been observed up to such high frequencies (e.g., Ref. 20). It may be noted that in $\text{CdF}_2:\text{In}$ there is no indication for the characteristic decrease of σ with frequency, connected with Drude behavior. The high-frequency conductivity seems to be governed by hopping of localized charge carriers, while Drude-like transport of “free” electrons, excited into the conduction band, dominates at low frequencies and dc only.

The submillimeter-range data for 10 K, where the low-frequency conductivity in the doped sample can be expected to be extremely low, agree well with the infrared data for CdF_2 without impurities (solid line). The latter, showing a peak at around 10^{13} Hz represents a dipolar lattice mode.

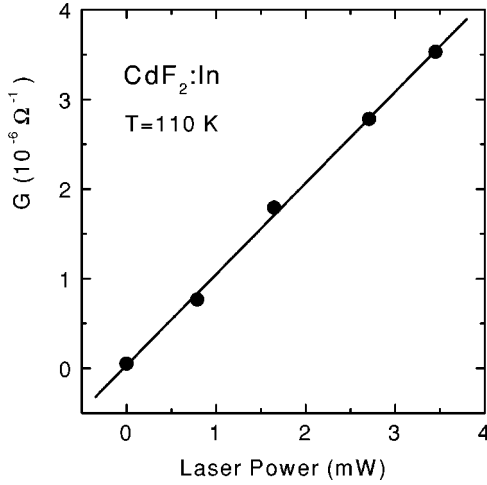


FIG. 4. The CdF₂:In sample conductance G versus the laser power at $T=110$ K [G is obtained from the fitting of $C_p(\nu)$ and $G_p(\nu)$ curves].

C. Light excitation and measurements of the shallow state kinetics

In order to determine the kinetic coefficients which affect the rate of the thermally induced transfers between the deep and shallow states, we have carried out experiments with illumination of the sample by light with a wavelength $\lambda = 488$ nm. This wavelength hits into the wide photoionization absorption band in CdF₂:In centered around 400 nm.³ The sample was cooled to the required temperatures in darkness and illuminated afterwards. We found, that the characteristic relaxation frequency ν_p is proportional to the intensity of the light I_{laser} at all temperatures (50–150 K) at which under illumination ν_p hits into the instrumental frequency window of the HP4284 analyzer. This behavior can be ascribed to the conductivity being proportional to the light intensity (at least for that used in our experiments $I_{\text{laser}} < 6$ mW/cm²), since at $C_1 \cong \text{const}$ and $C_2 \cong \text{const}$ the conductance of the sample is $G = 2\pi\nu_p(C_1 + C_2) \propto I_{\text{laser}}$ [see Eq. (11)]. As an example, Fig. 4 shows the sample conductance versus the laser power for $T=110$ K. The linear dependencies $G(I_{\text{laser}})$ show the absence of any saturation effects for the illumination power used in our experiments.

After switching off the illumination, the frequency ν_p and the conductance G relax with time. The rate of this relaxation is not constant. During first minutes G rapidly drops by 1 or 2 orders of magnitude, but then decreases rather gradually with a characteristic time being from half an hour to several hours (Fig. 5, upper panel) depending on temperature. This process is connected with the capture of a part of the non-equilibrium carriers by the In³⁺ ions into the metastable donor state In³⁺ + e_{hydr} with a subsequent slow transition into the ground state In¹⁺. Heating the sample to room temperature and subsequent recovery cooling in darkness completely restores ν_p and the frequency dependencies of $C_p(\nu)$ and $G_p(\nu)$.

It is shown in Ref. 3, that during illumination of CdF₂:In by light with a wavelength inside of the photoionization absorption band, the following photochemical reaction takes place:

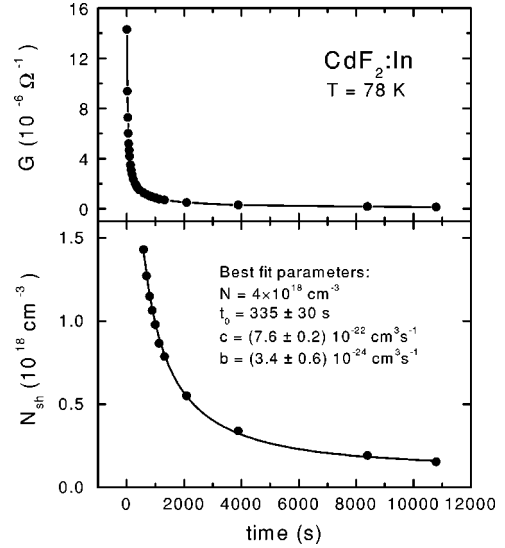
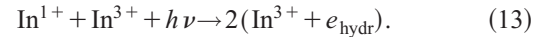
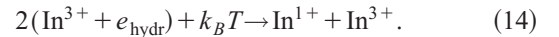


FIG. 5. Time dependencies of the conductance G (upper panel) and of the shallow donor concentration N_{sh} (bottom panel) of CdF₂:In after its irradiation with 488 nm laser light at $T=78$ K. Upper panel: points are the experimental data, line is guided for eye. Bottom panel: points are calculated from Eq. (20) using $n_e(t) = G(t)d/Se\mu$, and line is the best fit by Eq. (16) [only those $G(t)$ data points have been used here, for which the calculated N_{sh} is much less than the total concentration of active impurity $N = 4 \times 10^{18}$ cm⁻³].



This reaction brings the In ions into the hydrogenlike state with an energy E_{sh} . The reverse process of the thermal decay of the shallow centers with capture of the released electrons by other shallow centers occurs in accordance with the bimolecular reaction



The thermal decay of the shallow states after the light illumination is described by the kinetic equation³

$$dN_{\text{sh}}/dt = -cN_{\text{sh}}^2 + b(N - N_{\text{sh}})^2/4, \quad (15)$$

where N_{sh} is the concentration of the shallow centers, c and b are the kinetic coefficients of the decay and the creation of the shallow center, correspondingly. It is assumed here, that (i) the concentration N^{1+} of the deep centers is approximately equal to the concentration N^{3+} of the completely ionized In³⁺ centers, (ii) $N^{1+} + N^{3+} + N_{\text{sh}} = N$ and, consequently, $N^{1+} \approx N^{3+} \approx (N - N_{\text{sh}})/2$, (iii) and the free electron concentration is negligible. The solution of Eq. (15) yields the following time dependence for N_{sh} :

$$N_{\text{sh}}(t) = \frac{n_1 \exp[N\sqrt{cb}(t+t_0)] - n_2}{\exp[N\sqrt{cb}(t+t_0)] - 1}, \quad (16)$$

$n_1 = N/(1 + 2\sqrt{cb})$, $n_2 = N/(1 - 2\sqrt{cb})$, t_0 is a constant of integration.

In order to compare our results for $G(t)$ with Eq. (16) we have calculated the electron concentration $n_e(t) = G(t)d/(Se\mu)$, and then obtained $N_{\text{sh}}(n_e)$, using the procedure described below.

Since in the $\text{CdF}_2:\text{In}$ crystals, after the additive coloration process, the In^{3+} ions play a role of donors, and the In^{1+} ions, capturing an additional electron, play a role of acceptors, and since the effective concentration of donors n_d in a compensated donor semiconductor is equal to the difference between the concentrations of donors and acceptors,²¹ we obtain n_d equal to the concentration of the shallow hydrogenlike centers N_{sh} , formed via capture of electrons to a hydrogenlike orbit by a little part of the In^{3+} ions. We assume thermal equilibrium between the conduction electrons and the shallow states. We also assume that all the conduction electrons are formed through ionization of the shallow states and that the direct electron transitions between the deep levels and the conduction band are negligible. The conducting electron concentration in a semiconductor with donor and acceptor impurities with concentrations of N_d and N_a , correspondingly, is²¹

$$N_e = \frac{N_d - N_a}{2N_a} N_c \exp(-E_d/k_B T), \quad (17)$$

where E_d is the energy of the donor level, $N_c = 2(2\pi m^* k_B T)^{3/2}/h^3$ is the density of states in the conduction band, and m^* is the effective electron mass. Equation (17) is valid for low enough temperatures, when

$$E_d/k_B T \gg 1. \quad (18)$$

In our case $N_d \equiv N^{3+}$, $N_a \equiv N^{1+}$ and $N_d - N_a = N_{\text{sh}}$, $N^{3+} \approx N^{1+} \approx N/2$, $E_d \equiv E_{\text{sh}} = 0.1$ eV and the condition of Eq. (18) is always satisfied. Consequently, the electron concentration is given by

$$n_e = \frac{N_{\text{sh}}}{N} N_c \exp(-E_{\text{sh}}/k_B T) \quad (19)$$

and

$$N_{\text{sh}}(t) = [n_e(t)N/N_c] \exp(E_{\text{sh}}/k_B T). \quad (20)$$

Substituting to Eq. (20) the data for N and $n_e(T)$, defined in our experiments [$N = 4 \times 10^{18} \text{ cm}^{-3}$, $n_e(T) = \sigma(T)/e\mu$], and the values of $m^* = 0.45m_e$ (Ref. 16) and $E_{\text{sh}} = 0.1$ eV, we obtain $N_{\text{sh}}/n_e = 1.15 \times 10^7$ at $T = 78$ K and $N_{\text{sh}}/n_e = 9.07 \times 10^4$ at $T = 110$ K. In accordance with assumed thermal equilibrium between the conduction electrons and the shallow states we use these ratios for calculating $N_{\text{sh}}(t)$ through the experimentally found time-dependent electron density $n_e(t) = G(t)d/Se\mu$. The strong identity of the time dependencies of the infrared absorption [$\propto N_{\text{sh}}(t)$] and of the conductivity [$\propto n_e(t)$] after an optical excitation has been experimentally shown in Ref. 15. Since Eq. (15) implies that $N_{\text{sh}} \ll N$, we used only those experimental $G(t)$ data points, for which the calculated N_{sh} is much less than $4 \times 10^{18} \text{ cm}^{-3}$.

The results for $N_{\text{sh}}(t)$ and the calculated fit curve Eq. (16) are shown in Fig. 5 (bottom part) for $T = 78$ with the best fit

parameters ($N = 4 \times 10^{18} \text{ cm}^{-3}$, $t_0 = 335$ s, $c = 7.6 \times 10^{-22} \text{ cm}^3 \text{ s}^{-1}$, and $b = 3.4 \times 10^{-24} \text{ cm}^3 \text{ s}^{-1}$). For the thermal decay curve at $T = 110$ K the best fit parameters are $N = 4 \times 10^{18} \text{ cm}^{-3}$, $t_0 = 2875$ s, $c = 1.17 \times 10^{-19} \text{ cm}^3 \text{ s}^{-1}$, and $b = 3.7 \times 10^{-25} \text{ cm}^3 \text{ s}^{-1}$. Using these values of c and b , we compare the shallow center decay and creation processes for $T = 78$ K and $T = 110$ K. At $t = 1000$ s and $T = 78$ K, the first term of Eq. (15) is two orders of magnitude larger than the second one, i.e., the thermal decay of the shallow states is dominating. At $T = 110$ K and $t = 1000$ s these terms are nearly equal, i.e., the thermal decay begins to be compensated by the thermal activation. It is interesting, that $c(110 \text{ K})$ is two orders of magnitude larger than $c(78 \text{ K})$, while $b(110 \text{ K})$ is one order of magnitude smaller than $b(78 \text{ K})$.

Assuming that the temperature dependence of the kinetic coefficient c can be described by activated behavior, $c(T) = A \exp(-E_{\text{ac}}/k_B T)$, from $c(78 \text{ K})$ and $c(110 \text{ K})$ we found $E_{\text{ac}} = 0.12$ eV. This value coincides with E_{ac} obtained in Ref. 3 by the kinetic measurements of the shallow state infrared absorption. The kinetic coefficient c may be presented as $c(T) = \text{const } p_1 p_2$, where $p_1 = \nu_1 \exp(-E_{\text{sh}}/k_B T)$ is the rate of the electron releasing out the first shallow center to the conduction band, and $p_2 = \nu_2 \exp(-E_{\text{cap}}/k_B T)$ is the rate of the thermally activated electron hopping over the barrier E_{cap} and simultaneous capture of a conduction electron by the second shallow center.³ Here ν_1 and ν_2 are the attempt frequencies: ν_1 is the impurity vibration frequency and ν_2 is the ‘‘configuration phonon mode’’ frequency of the impurity. Thus, for the activation energy of the kinetic coefficient c one has $E_{\text{ac}} = E_{\text{sh}} + E_{\text{cap}}$, and the capture barrier is equal to $E_{\text{cap}} = E_{\text{ac}} - E_{\text{sh}} = 0.12 - 0.1$ eV = 0.02 eV.

For a higher temperature ($T = 150$ K) the shallow state decay curve is not fitted exactly by Eq. (16). The change of the decay kinetics type on increasing temperature may be explained by formation of a shallow states impurity band in $\text{CdF}_2:\text{In}$. The levels of the hydrogenlike states $\text{In}^{3+} + e_{\text{hydr}}$ may form such a band due to Coulomb interaction with statistically distributed F^{1-} , In^{3+} , and In^{1+} ions.¹⁵ For increasing temperature, the higher levels of this band become populated, leading to an effective decrease of E_{cap} . At $T = 150$ K the levels up to $k_B T = 0.013$ eV $\approx E_{\text{cap}}$ are populated and the barrier is eliminated.

The knowledge of the key parameters $E_{\text{cap}} = 0.02$ eV, $E_{\text{sh}} = 0.1$ eV,⁸ $E_{\text{deep}} = 0.25$ eV,^{5,8} $E_{\text{opt}} = 1.9$ eV (Ref. 8) (the optical ionization energy of the deep state), and $Q_0 - Q_1 = 1.84$ Å (Ref. 5) (the difference of ion In configuration coordinates in the deep Q_0 and in the shallow Q_1 states) allows one to define concretely the configuration energy diagram,⁸ assuming $Q_1 = 0$ and a quadratic Q dependence of the levels

$$E_{\text{cond}}(Q) = a_1 Q^2,$$

$$E_{\text{sh}}(Q) = a_1 Q^2 - E_{\text{sh}}, \quad (21)$$

$$E_{\text{deep}}(Q) = a_0 (Q - Q_0)^2 - E_{\text{deep}}.$$

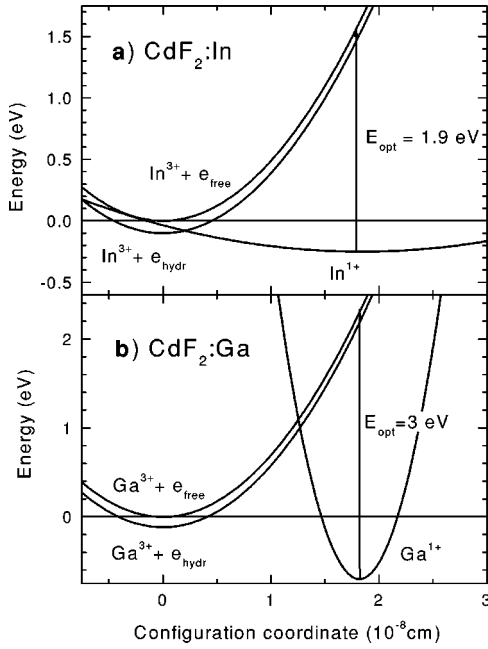


FIG. 6. Specified energy levels diagrams for the deep and the shallow states of the bistable In (a) and Ga (b) center in CdF_2 , as function of the configuration coordinate Q of the impurity ion nucleus.

Here the energies are measured in eV and the coordinates are in \AA . Then for a_1 , a_0 and the barrier peak coordinate Q_{cap} one has

$$\begin{aligned} a_1 &= \frac{E_{\text{opt}} - E_{\text{deep}}}{Q_0^2}, \\ a_0 &= \frac{E_{\text{deep}} - E_{\text{sh}} + E_{\text{cap}}}{(Q_{\text{cap}} - Q_0)^2}, \\ Q_{\text{cap}} &= \sqrt{\frac{E_{\text{cap}}}{a_1}}, \end{aligned} \quad (22)$$

consequently, $a_1 = 0.487 \text{ eV/\AA}^2$, $a_0 = 0.063 \text{ eV/\AA}^2$, and $Q_{\text{cap}} = 0.20 \text{ \AA}$. The corresponding diagram is given in Fig. 6(a), which shows that the walls of the potential well of the shallow states are much steeper than those of the deep state. Therefore, according to the values of a_1 and a_0 , the “return

force” $F = -dE/dQ$ is 8 times larger for the shallow state. In addition, the barrier position Q_{cap} is very close to the potential well minimum of the shallow state.

Similar calculation made for CdF_2 doped with Ga [$E_{\text{sh}} = 0.116 \text{ eV}$,²² $E_{\text{opt}} = 3 \text{ eV}$, $E_{\text{cap}} = 1.12 \text{ eV}$,²³ $E_{\text{deep}} = 0.7 \text{ eV}$, and $Q_0 - Q_1 = 1.82 \text{ \AA}$ (Ref. 5)] gives the opposite picture of the potential curves [Fig. 6(b)]. Now $a_1 = 0.694 \text{ eV/\AA}^2$, $a_0 = 5.63 \text{ eV/\AA}^2$, $Q_{\text{cap}} = 1.27 \text{ \AA}$, i.e., the “return force” for the shallow state is 8 times weaker than one for the deep state, and the barrier position Q_{cap} is far away from the shallow state potential well minimum. In addition, while the “return forces” for the shallow states of In and Ga in CdF_2 are close to each other, the “return force” for the deep state of Ga is 90 times larger than one for In.

Now one can also calculate the impurity “configuration phonon mode” frequencies of the deep $\nu_{\text{deep}} = (1/2\pi)\sqrt{2a_0/M}$, and of the shallow $\nu_{\text{sh}} = (1/2\pi)\sqrt{2a_1/M}$, states. Here M is the reduced mass of the impurity ion and of the surrounding ions, involved in the “configuration phonon modes.” As the first approximation we have taken the values of the impurity ion masses for M and obtained for the In impurity $\nu_{\text{deep}} = 5.18 \times 10^{11} \text{ Hz}$, $\nu_{\text{sh}} = 1.44 \times 10^{12} \text{ Hz}$, and for the Ga impurity $\nu_{\text{deep}} = 6.28 \times 10^{12} \text{ Hz}$, $\nu_{\text{sh}} = 2.2 \times 10^{12} \text{ Hz}$.

IV. CONCLUSIONS

In this paper we report on the low frequency conductivity measurements of semiconducting $\text{CdF}_2:\text{In}$ crystals with metal-coating electrodes, producing Schottky barriers at the sample surface. The results allow to determine a whole lot of the material characteristics: the dielectric constant, the temperature dependence of the dc conductivity, the activation energy of the impurity E_a , the total concentration of the active In ions N , the shallow donor concentration N_{sh} , the height of the capture barrier E_{cap} , and the values of the kinetic coefficients determining the rate of the thermally induced transitions between the deep and the shallow states of In in the CdF_2 matrix. These measurements do not require ohmic contacts, preparation of which is necessary for standard dc measurements and often is quite complicated and not always realizable task.

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