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Nearly itinerant ferromagnetism in CaNi₂ and CaNi₃

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Single crystals of $CaNi_2$ and $CaNi_3$ are successfully grown out of excess Ca. Both compounds manifest a metallic ground state with enhanced, temperature-dependent magnetic susceptibility. The relatively high Stoner factors of Z=0.79 and 0.87 found for $CaNi_2$ and $CaNi_3$, respectively, reveal their close vicinity to ferromagnetic instabilities. The pronounced field dependence of the magnetic susceptibility of $CaNi_3$ at low temperatures (T<25 K) suggests strong ferromagnetic fluctuations. A corresponding contribution to the specific heat with a temperature dependence of $T^3 ln T$ is also observed.

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I. INTRODUCTION

Compounds of electropositive elements (e.g., Ca, Ti, and La) and transition metals (e.g., Ni, Cu, and Cr) have been studied, to a certain extent, to explore their potential for hydrogen-storage applications.^{1,2} Among these, the members of the Ca-Ni family (CaNi₂, CaNi₃, Ca₂Ni₇, and CaNi₅) were investigated by means of x-ray diffraction.³ Cubic CaNi2 and trigonal CaNi3 were found to form CaNi2H3.4 and CaNi₃H_{4.6} under elevated H-vapor pressures without changing the symmetry of the crystal structure.⁴ However, despite these earlier investigations and the simplicity of these binary compounds, no experimental data on physical properties have been reported. The main reason for this lack of information is the challenging synthesis of these compounds caused by the high reactivity of Ca, which is highly air and moisture sensitive and tends to attack several standard crucible materials and manifests elevated vapor pressures of 1 bar at T = 1500 °C (close to the melting point of elemental Ni).

In this paper we present a method for the growth of CaNi₂ and CaNi₃ single crystals from Ca flux. Measurements of temperature-dependent magnetization, electrical resistivity, and specific heat reveal a metallic ground state with an unusually high Stoner factor, indicating strong ferromagnetic correlations in CaNi₂ that are further enhanced in CaNi₃.

II. EXPERIMENT

X-ray powder diffraction (XRPD) was performed on ground single crystals using a Rigaku Miniflex diffractometer (with a Cu- $K\alpha_{1,2}$ wavelength). Lattice parameters were refined by the LeBail method using GSAS (Ref. 5) and EXPGUI.⁶ Laue back-reflection patterns were taken with an MWL-110 camera manufactured by Multiwire Laboratories. Magnetization measurements were performed using a Quantum Design MPMS. Electrical resistivity was measured in four-point geometry using the ac transport option of a Quantum Design PPMS. Silver epoxy was used to make electrical contacts on the samples and then cured at T = 120 °C under air for approximately 20 min. The samples did not visually degrade and XRPD measurements revealed no structural changes as a result of this treatment. Absolute values of the electrical resistivity are approximate due to the poorly defined geometry factor of the samples. Specific heat was measured by a heat-pulse relaxation method using a Quantum Design PPMS.

III. CRYSTAL GROWTH

Starting materials were Ni wire (Alfa Aesar, 99.98% metals basis) and distilled Ca (Ames Laboratory, Metals Developement, 99.98%). Best results were obtained by mixing Ca and pieces of Ni wire in a molar ratio of 67:33 and 46:54 for CaNi₂ and CaNi₃, respectively, motivated by the published phase diagrams^{7,8} (Fig. 1). The mixtures, each with a total mass of roughly 2.5 g, were packed into a three-cap Ta crucible⁹ inside an Ar-filled glove box. A combination of laser welding and arc melting was used to seal the Ta crucibles under inert atmosphere (0.5 bar Ar). In accordance with the results of Ref. 4, we found no indications for an attack of Ta-crucibles by Ni.

A. CaNi₂

The Ca-Ni mixture was heated from room temperature to $T=1000\,^{\circ}\text{C}$ over 5 h, cooled to $T=900\,^{\circ}\text{C}$ within 1 h, slowly cooled to $T=650\,^{\circ}\text{C}$ over 50 h, and finally decanted to separate the CaNi₂ crystals from the excess liquid. Single crystals of octahedral habit with dimensions up to 3 mm and masses of 25 mg could be obtained [Fig. 2(a)]. The facets show a threefold rotation symmetry corresponding to $\{111\}$ planes of the cubic lattice as confirmed by Laue back reflection [Fig. 2(b)]. The triangular hopper morphology seen in the center of some surfaces points to a surface diffusion-limited growth that could be further improved best by stirring the melt or rotating the crucible or, to a lesser extent, by decreasing the cooling rate (see, e.g., Ref. 10).

B. CaNi₃

The Ca-Ni mixture was heated from room temperature to $T=1190\,^{\circ}\mathrm{C}$ over 6 h, held at $T=1190\,^{\circ}\mathrm{C}$ for 1/2 h, slowly cooled to $T=910\,^{\circ}\mathrm{C}$ over 32 h, and finally decanted to separate the CaNi₃ crystals from the excess liquid. Platelike single crystals with lateral dimensions of up to 3 mm and a thickness of 0.5 mm could be obtained [Fig. 2(c)]. The threefold crystallographic c axis is oriented perpendicular to the large surface of the plates as confirmed by Laue back reflection [Fig. 2(d)].

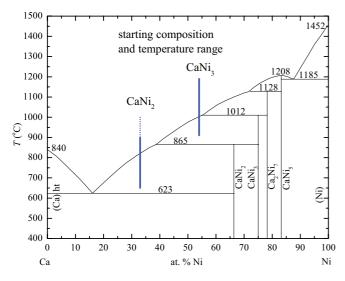
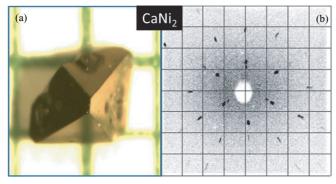


FIG. 1. (Color online) Ca-Ni phase diagram after Notin *et al.* (Ref. 7). Starting compositions and temperature profile for $CaNi_2$ and $CaNi_3$ growths shown with blue lines (the dotted line represents rapid cooling).

IV. STRUCTURAL CHARACTERIZATION

After grinding and mounting the sample in an Ar glove box, the powder was covered with Kapton-foil that was attached to the sample holder using double-faced scotch tape. Once covered in this manner the sample was removed from the Ar



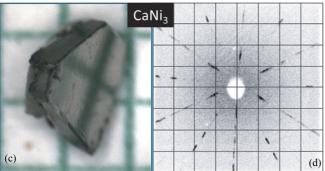


FIG. 2. (Color online) (a) CaNi $_2$ single crystal on a millimeter grid and (b) corresponding x-ray Laue back-reflection pattern. (c) CaNi $_3$ single crystal on a millimeter grid and (d) corresponding x-ray Laue back-reflection pattern. Both diffraction patterns show the threefold rotation symmetry of $\{111\}$ and $\{001\}$ directions of their cubic and hexagonal unit cells, respectively.

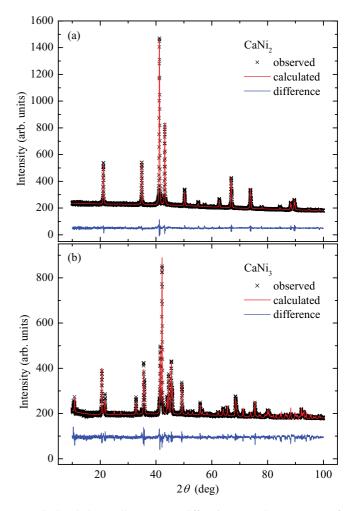


FIG. 3. (Color online) X-ray-diffraction powder patterns of (a) $CaNi_2$ and (b) $CaNi_3$ together with fits based on the published cubic and hexagonal structures, respectively.

glove box. The diffraction pattern taken on covered CaNi₂ and CaNi₃ samples did not change after removing the Kapton foil and exposing the powder to air for one week. Therefore both compounds are significantly less air sensitive than elemental Ca. However, the development of a field dependence in the magnetic susceptibility at room temperature was observed in samples that were stored under air for several weeks, indicating the formation of a small ferromagnetic phase presumably due to the formation of elemental Ni.

Figure 3(a) shows the XRPD pattern measured on ground CaNi₂ single crystals together with the refined pattern based on the published crystal structure [space group $Fd\bar{3}m$ (227)]. The lattice parameter a=7.252(6) Å is in good agreement with the literature data [a=7.251 Å (Ref. 4)].

The XRPD pattern measured on ground CaNi₃ single crystals is plotted in Fig. 3(b) together with the refined pattern based on the published crystal structure [space group $R\bar{3}m$ (hexagonal) (166)]. The lattice parameters of a=5.044(3) Å and c=24.44(9) Å are in good agreement with the literature data [a=5.052 Å and c=24.45 Å (Ref. 2)].

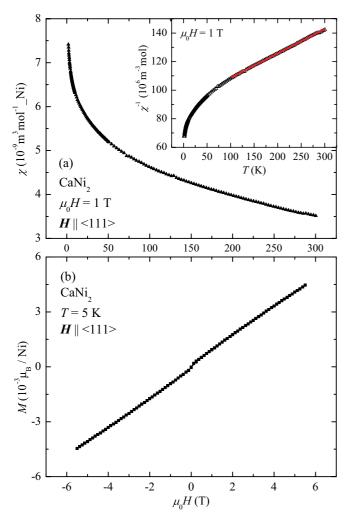


FIG. 4. (Color online) (a) Magnetic susceptibility $\chi = M/H$ per mol Ni of CaNi₂. The moderate increase of $\chi(T)$ under cooling from 300 K to $T \approx 20$ K is followed by a significant increase at lower temperatures. The inset shows the inverse susceptibility. (b) Magnetization M(H) as a function of field.

V. RESULTS

A. Magnetization

The magnetic susceptibility data $\chi(T) = M/H$ per mol Ni are shown in Figs. 4(a) and 5(a) for CaNi₂ and CaNi₃, respectively. In both compounds $\chi(T)$ increases significantly with decreasing T, which is in contrast to the T-independent behavior expected for a simple metal. Between T = 100 and 300 K $\chi(T)$ is proportional to T^{-1} , manifesting what could be interpreted as a Curie-Weiss-like behavior [insets in Figs. 4(a) and 5(a)].

For CaNi₂ the effective moment that can be inferred from this analysis is $\mu_{\rm eff} = 1.4(1)\mu_B$ per Ni and the corresponding Weiss temperature amounts to a large antiferromagnetic (AFM) value of $\Theta_W = -540$ K. Figure 4(b) shows the magnetization as a function of the field M(H) in units of μ_B per Ni. At T = 5 K M(H) increases in an essentially linear fashion with the magnetic field with only a tiny anomaly around $H \approx 0$.

For CaNi₃ the effective moment that can be inferred from this analysis is $\mu_{\rm eff} = 1.95(5)\mu_B$ ($H \parallel c$) and $\mu_{\rm eff} =$

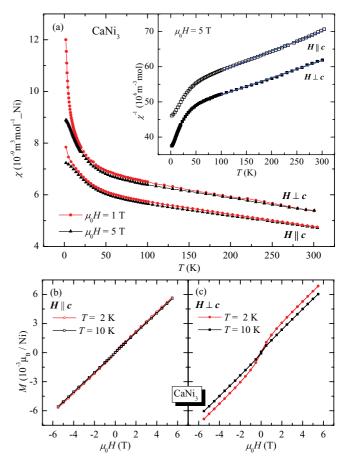


FIG. 5. (Color online) (a) Magnetic susceptibility $\chi = M/H$ of CaNi₃ per mol Ni. The moderate increase of $\chi(T)$ under cooling from 300 K to $T \approx 20$ K is followed by a significant increase at lower temperatures. The inset shows the inverse susceptibility. Magnetization M(H) as a function of field for $H \parallel c$ (b) and $H \perp c$ (c) at T=2 and 10 K.

 $2.08(5)\mu_B$ ($H \perp c$) per Ni. The Weiss temperatures amount to large AFM values of $\Theta_W^{H\parallel c} = -950$ K and $\Theta_W^{H\perp c} = -960$ K. As will be discussed below, such high Weiss temperatures are unphysical for intermetallic compounds that remain paramagnetic and indicate that such a local moment treatment of the data is most likely inappropriate. For $T \geqslant 25$ K CaNi₃ shows nearly no field dependence of $\chi(T)$. In contrast to the high-T behavior, a pronounced field dependence of $\chi(T)$ emerges at T < 25 K (more pronounced for $H \perp c$), indicating strong ferromagnetic (FM) correlations.

The Magnetization M(H) of CaNi₃ shows an almost perfectly linear field dependence for $T \ge 10$ K [for both $H \parallel c$ and $H \perp c$, black squares in Figs. 5(b) and 5(c)]. At lower temperatures (T=2 K) a small deviation from the linear behavior in M(H) is found for $H \parallel c$, whereas a clear curvature forms in M(H) for $H \perp c$ [red circles in Figs. 5(b) and 5(c)] in accordance with the field dependence of $\chi(T)$ at low temperatures.

B. Electrical resistivity

Figure 6 shows the electrical resistivity of (a) CaNi₂ and (b) CaNi₃ measured with current flow along $\langle 1\bar{1}0 \rangle$ and along the

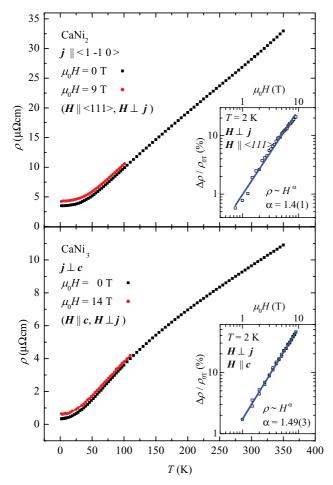


FIG. 6. (Color online) Electrical resistivity of (a) CaNi₂ and (b) CaNi₃. CaNi₂ shows metallic behavior with a linear T dependence over a wide temperature range and a crossover to T^2 dependence at low T. An additional change of slope is observed for CaNi₃ in the region around $T\approx 150$ K. (Absolute values are approximate due to the poorly defined geometry factor of the samples.) Insets: The magnetoresistance $\Delta\rho/\rho_0=(\rho_H-\rho_0)/\rho_0$ plotted on a double-logarithmic scale at T=2 K is positive and approaches values of 22% and 46% at $\mu_0H=9$ T for CaNi₂ and CaNi₃, respectively.

basal plane, respectively. The metallic behavior observed for CaNi₂, demonstrated by the linear T dependence for T > 50 K and an approximately quadratic T dependence at low T, is modified for CaNi₃ by an additional change of slope over a wide T range between T = 100 and 200 K. Residual resistivity ratios of RRR = $\rho_{300 \, \text{K}}/\rho_0 = 8$ and 29 for CaNi₂ and CaNi₃, respectively, are consistent with good-quality single crystals.

A positive magnetoresistance $\Delta \rho = \rho_H - \rho_0$ is observed for both compounds with increasing values towards low T (solid red circles and insets in Fig. 6, $H \perp j$). The field dependence of $\Delta \rho$ at T=2 K follows a power-law dependence of $\Delta \rho(H) \sim H^{\alpha}$ with $\alpha \approx 1.5$ [1.4(1) and 1.49(3) for CaNi₂ and CaNi₃, respectively], which differs significantly from the expected value of $\alpha=2$ for a simple metal. The values of $\Delta \rho/\rho=22\%$ and 46% at $\mu_0H=9$ T for CaNi₂ and CaNi₃, respectively, can be regarded as rather high, taking into account the comparatively low RRR values when compared to simple metals in the picture of a Kohler plot (see, e.g., Ref. 11),

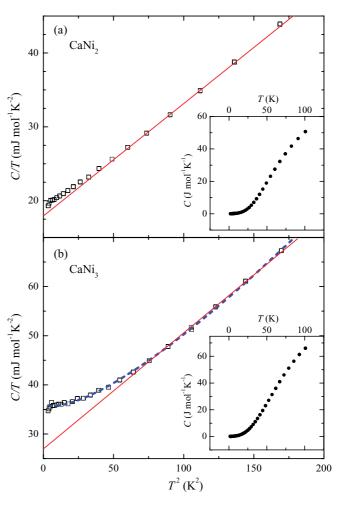


FIG. 7. (Color online) Specific heat plotted as C/T vs T^2 for (a) $CaNi_2$ and (b) $CaNi_3$. Additional contributions to the specific heat of an ordinary metal $(C/T = \gamma + \beta T^2)$, indicated by the red lines) are observed below $T \approx 10$ K. Assuming a contribution of spin fluctuations of the form $C_{mag} = AT^3 \ln(T/T_{SF})$ leads to a T dependence shown by the dashed blue line. Insets: specific heat as a function of temperature.

and are comparable to YAgSb₂, ¹² but are significantly smaller than the large values of $\Delta \rho/\rho = 5 \times 10^5\%$ found in PtSn₄ (Ref. 13) (RRR ~ 1000).

C. Specific heat

Figure 7 shows the specific heat of (a) CaNi₂ and (b) CaNi₃ plotted as C/T vs T^2 . Electron and phonon contributions are described by $C = \gamma T + \beta T^3$ and are indicated by red lines in Fig. 7. A similar Sommerfeld coefficient of $\gamma = 9.0$ mJ mol $_{\rm Ni}^{-1}$ K $^{-2}$ was found for both compounds (when expressed of in terms per mole nickel). Additional contributions to the specific heat are observed for T < 10 K. Whereas the deviations are small for CaNi₂, there is a significant enhancement of C/T for CaNi₃ toward low T most likely associated with FM fluctuations observed in the $\chi(T)$ measurements. These magnetic fluctuations contribute to the specific heat by $C_{\rm mag} = AT^3 \ln(T/T_{\rm SF})$. The coefficients obtained by fitting the experimental data to the resulting

equation

$$C/T = \gamma_{\text{mag}} + \beta T^2 + AT^2 \ln(T/T_{\text{SF}})$$

are $\gamma_{\rm mag}=12.1(2)$ mJ mol $_{\rm Ni}^{-1}$ K $^{-2}$, $\beta=0.080(5)$ mJ mol $_{\rm Ni}^{-1}$ K $^{-4}$, A=0.056(3) mJ mol $_{\rm Ni}^{-1}$ K $^{-4}$, and $T_{\rm SF}=18(2)$ K. The corresponding fit is plotted as a dashed blue line in Fig. 7(b). Note that the contribution of spin fluctuations to the specific heat is negative for $T< T_{\rm SF}$, corresponding to a shift of entropy to higher T around $T_{\rm SF}$. This is compensated for by assuming a higher electron contribution to C at low T ($\gamma_{\rm mag}=12.1$ mJ mol $_{\rm Ni}^{-1}$ K $^{-2}$ compared to $\gamma=9.0$ mJ mol $_{\rm Ni}^{-1}$ K $^{-2}$). Since the deviation of the measured specific heat of CaNi $_2$ from the expected lattice and electron contribution are small, a quantitative estimate of A and $T_{\rm SF}$ is not reliable. The specific heat data between T=2 and 100 K are plotted in the insets of Fig. 7, showing the expected decrease of slope in the upper T range toward approaching the Dulong-Petit limits (75 and 100 J mol $^{-1}$ K $^{-1}$, respectively).

VI. DISCUSSION

Our results on CaNi₂ are in contrast to the findings of Tsvyashchenko *et al.* claiming weak ferromagnetism for CaNi₂ at room temperature.¹⁵ However, no measured experimental data are presented in Ref. 15. Therefore, we are not sure whether the discrepancy is due a modification of the structure caused by the high-pressure synthesis used by Tsvyashchenko *et al.* or simply the result of FM nickel impurities (or other second phases) that might be present in their polycrystalline samples.

We now discuss the possibility of local magnetic moments indicated by the Curie-Weiss behavior of the magnetic susceptibility $\chi(T)$. In this scenario a large AFM exchange interaction has to be inferred from the observed Weiss temperatures of $\Theta_W \approx -500$ and -900 K, for CaNi₂ and CaNi₃, respectively. Effective moments greater than $1\mu_B$ (as obtained for these compounds) coupled by such strong interactions are expected to order antiferromagnetically above 100 K. However, there is no indication for an AFM ordering in the whole T range investigated. Therefore, the experimental results are incompatible with a local moment scenario unless the system is assumed to be extremely frustrated (which is highly unlikely in both of these such different structures). Taking into account that Ni is not known to carry a local moment together with the FM correlations inferred from the low-T upturn in $\chi(T)$ [Fig. 5(a)] makes this assumption unlikely.

A more plausible explanation for the increase in $\chi(T)$ toward low T is given by an enhancement of the normally only weakly T-dependent terms of the paramagnetic susceptibility of a metal. A similar temperature dependence of $\chi(T)$ was observed for elemental Pd (Ref. 16) and more recently for YFe₂Zn₂₀ and LuFe₂Zn₂₀ (Refs. 17 and 18) and can be understood in terms of proximity to the Stoner limit. Thereby, the theoretical description is based on the temperature dependence of the Fermi-Dirac distribution function (within the framework of Stoner theory) and leads to a qualitative agreement with the experimental data (see, e.g., Ref. 19).

The Stoner factor Z, defined by $\chi = \frac{\chi_{\text{para}}}{1-Z}$, can be used to quantify the strength of FM correlations (where χ is the

renormalized Pauli susceptibility of a metal χ_{para}) and can be calculated from the experimental data of $\chi(T \to 0)$ and γ by

$$Z = 1 - \frac{3\mu_B}{(\pi k_B)^2} \frac{\gamma}{\chi(T \to 0)}$$

(assuming density of states and magnetic susceptibility of the free electron gas). We find Z=0.79 (CaNi₂) and Z=0.87 (CaNi₃, $\mu_0 H=1$ T, $H\perp c$).

For the archetypical Stoner enhanced metal, elemental Pd, the calculation yields Z=0.83 [$\gamma=9.45$ mJ mol $^{-1}$ K $^{-2}$ (Ref. 20) and $\chi(T\to 0)=9.29\times 10^{-9}$ m 3 mol $^{-1}$ (Ref. 16) of Pd are both similar to the values obtained for CaNi $_2$ and CaNi $_3$]. Therefore, at least CaNi $_3$ is even closer to a FM ordered ground state than Pd and approaches the high values of Z=0.88 found in YFe $_2$ Zn $_{20}$ and LuFe $_2$ Zn $_{20}$. 18 Taking into account the field dependence of $\chi(T\to 0)$ of CaNi $_3$ [steeper increase of M(H) for $\mu_0H<1$ T; see Fig. 5(c)], even higher Stoner factors are obtained, e.g. Z=0.89 for $\mu_0H=0.5$ T. Using the higher $\gamma_{\rm mag}=12.1$ mJ mol $_{\rm Ni}^{-1}$ K $^{-2}$ for CaNi $_3$ and in doing so assuming a larger electron contribution to the specific heat and accordingly a higher density of states at the Fermi level still leads to Z=0.85.

A major difference between CaNi₂ and CaNi₃ and other Stoner enhanced metals such as elemental Pd, YFe₂Zn₂₀, and LuFe₂Zn₂₀ is the absence of a maximum in $\chi(T)$ at low T. As shown by Yamada, ²¹ this maximum is correlated with a possible itinerant electron metamagnetic transition within Ginzburg-Landau theory and occurs when the Landau expansion coefficients (A, B, and C) of the magnetic part of the free energy $\Delta F(M) = \frac{1}{2}AM^2 + \frac{1}{4}BM^4 + \frac{1}{6}CM^6$ fulfill the condition $\frac{AC}{B^2} > \frac{5}{28}$. This is not the case for CaNi₂ and CaNi₃ (in the temperature range investigated) and accordingly no indications for a metamagnetic transition were observed in M(H) measurements.

Consistent with FM spin fluctuations inferred from the field dependence of $\chi(T)$, we observed an upturn in the low-temperature specific heat of CaNi₃ [Fig. 7(b)]. Similar behavior has been observed in other FM, but close to paramagnetic [Ni_{0.63}Rh_{0.37} (Ref. 22)], or nearly FM itinerant electron systems [TiBe₂ (Ref. 23)]. It remains an open question why this upturn is absent or significantly less pronounced in the nearly FM itinerant electron systems such as Pd, YFe₂Zn₂₀, and LuFe₂Zn₂₀.

Since CaNi₃ was found to be very close to a FM ordered ground state and the iso-structural compound YNi₃ is a FM system with $T_C = 30 \text{ K}$, we tried to tune the system by gradually substituting Y for Ca. However, initial attempts to synthesize the alloy Ca_{1-x}Y_xNi₃ failed due to the formation of (Y,Ca)Ni₅ and (Y,Ca)₂Ni₇.

VII. SUMMARY

Single crystals of CaNi₂ and CaNi₃ have been grown and characterized by x-ray diffraction and temperature-dependent electrical resistivity, magnetization, and specific-heat measurements. Both compounds manifest behavior consistent with Stoner enhanced, nearly ferromagnetic Fermi liquids with CaNi₂ and CaNi₃ having Stoner enhancement factors *Z* of 0.79 and 0.87, respectively. The low-temperature specific

heat of CaNi₃ shows signatures of ferromagnetic fluctuations consistent with this Stoner enhanced state.

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