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Spin liquid close to a quantum critical point in Na₄Ir₃O₈

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Na₄Ir₃O₈ is a candidate material for a three-dimensional quantum spin liquid on the hyperkagome lattice. We present thermodynamic measurements of heat capacity C and thermal conductivity κ on high-quality polycrystalline samples of Na₄Ir₃O₈ down to T=500 and 75 mK, respectively. Absence of long-range magnetic order down to T=75 mK strongly supports claims of a spin-liquid ground state. The constant magnetic susceptibility χ below $T\approx 25$ K and the presence of a small but finite linear-T term in C(T) suggest the presence of gapless spin excitations. Additionally, the magnetic Grüneisen ratio shows a divergence as $T\to 0$ K and a scaling behavior, which clearly demonstrates that Na₄Ir₃O₈ is situated close to a zero-field QCP.

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In geometrically frustrated materials long range order is prohibited and a liquidlike ground state of spins, the spin-liquid (SL) state, can occur. Since Anderson's proposal of a valence bond state for a triangular lattice, search for such quantum spin liquids (QSL) has been pursued intensely. In the past decade, several new materials have been proposed as SL candidates (see recent reviews, Refs. 2-4). A small spin and quasi-low-dimensionality are considered ingredients that can lead to a SL state. Indeed, most of the proposed QSL candidates are materials with S = 1/2 moments sitting on quasi-lowdimensional structures. These include the two-dimensional (2D) triangular lattice organic compounds κ -(BEDT-TTF)₂Cu₂(CN)₃ (Refs. 5 and 6) and EtMe₃Sb[Pd(dmit)₂]₂,⁷ and the 2D kagome lattice inorganic materials ZnCu₃(OH)₆Cl₂ (Refs. 8 and 9) and BaCu₃V₂O₈(OH)₂. ¹⁰ The QSL states in these and other materials may possess exotic elementary excitations that obey either fermionic or bosonic statistics and can have gapped or gapless energy dispersion.⁴

Whether a QSL can exist in 3D, where quantum effects are reduced and there are more ways in which frustration can be relieved, is still an open question.⁴ In this context, recently, a new 3D material Na₄Ir₃O₈ with effective spins $S = \frac{1}{2}$ on a frustrated hyperkagome lattice has been proposed as a candidate QSL.¹¹ Using thermodynamic measurements at $T \ge 2$ K, it was shown that Na₄Ir₃O₈ does not order in spite of strong antiferromagnetic interactions ($\theta = -650 \text{ K}$). The magnetic specific heat showed a bump around 30 K, a temperature much smaller than θ , and displays a lowtemperature power-law dependence with an exponent close to 2 (Ref. 11) similar to several of the 2D materials listed above. 8,10 Subsequently, using classical and semiclassical spin models of Heisenberg spins on a hyperkagome lattice, the ground state was found to be highly degenerate and either a classical spin nematic order with long-range dipolar spin correlations is chosen at $T \approx 1$ K by an order-by-disorder mechanism¹² or a 120° coplanar magnetically ordered state¹³ were predicted. This coplanar magnetic order was found to give way, through a quantum phase transition, to a gapped topological Z₂ "bosonic" spin-liquid phase (characterized by the absence of long-range dipolar order) when quantum fluctuations are turned on. 13 The elementary excitations of this gapped spin-liquid state were predicted to be chargeless S = 1/2 spinons.¹³ The prediction of a gapped spin liquid is, however, at odds with experiments, which gave a Sommerfeld coefficient $\gamma \approx 2$ mJ/Ir mol K² suggesting gapless spin excitations unless the gap was vanishingly small or had nodes. In a completely different line of approach, a fermionic spin-liquid model was developed. This led naturally to gapless spin liquids as stable phases. These spin liquids had a Fermi surface of chargeless spinons, which at low temperatures was found to be unstable to the formation of paired states with line nodes. This was suggested as a natural explanation of the power law heat capacity at low $T.^{14,15}$ Inclusion of spin-orbit coupling was shown to relieve the frustration in some regions of parameter space and might lead to ordering at low temperatures. The suggesting gap-less spin excitations approach, a completely different line of approach, a fermionic spin-liquid model was developed. This led naturally to gapless spin liquids as stable phases. These spin liquids had a Fermi surface of chargeless spinons, which at low temperatures was found to be unstable to the formation of paired states with line nodes. This was suggested as a natural explanation of the power law heat capacity at low $T.^{14,15}$ Inclusion of spin-orbit coupling was shown to relieve the frustration in some regions of parameter space and might lead to ordering at low temperatures.

Thus there are predictions of both magnetically ordered or (Bosonic or Fermionic) spin-liquid ground states. As far as low-energy excitations are concerned, proposals for both a gapped or gapless state have been made. Proximity to a quantum critical point (QCP) has also been suggested. The true ground state of Na₄Ir₃O₈ is thus, still an open question.

To clarify the true ground state (ordered or spin-liquid), to address the questions about the nature of the low-energy excitations (gapped or gapless), and to look for proximity to a QCP, we have performed magnetic susceptibility (χ) , heat capacity (C), thermal conductivity (κ), and magnetocaloric effect [MCE = $(dT/dH)_S$)] measurements down to very low temperatures. Our main results are (i) neither C(T) $(T \ge 500 \text{ mK})$ nor $\kappa(T)$ $(T \ge 75 \text{ mK})$ show signature of long-range magnetic order providing fresh evidence for a spin-liquid state, (ii) both χ and C/T tend to finite values as $T \rightarrow 0$ K suggesting presence of gapless excitations although $\kappa/T \to 0$ as $T \to 0$ K, which we argue is most likely due to the polycrystalline nature of the sample, and (iii) the magnetic Grüneisen parameter $[\Gamma_H = \frac{1}{T}(\frac{dT}{dH})_S]$ shows a divergence and the data at various applied magnetic fields show a scaling behavior reminiscent of heavy-fermion materials situated close to a quantum critical point (QCP).¹⁸ All the results above demonstrate that Na₄Ir₃O₈ is a gapless quantum spin-liquid proximate to a zero-field QCP.

Polycrystalline samples of Na₄Ir₃O₈ and Na₄Sn₃O₈ were synthesized using standard solid state reaction at $T=1000\,^{\circ}\mathrm{C}$ and $1300\,^{\circ}\mathrm{C}$, respectively. Measurements down to $T=2\,\mathrm{K}$ were done on a Quantum Design PPMS. The low-temperature C and Γ_H were measured in a dilution refrigerator (DR),¹⁹

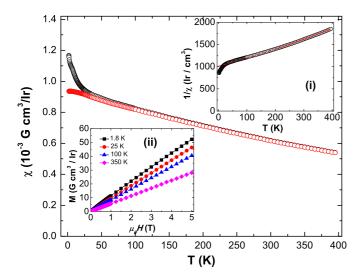


FIG. 1. (Color online) $\chi(T)$ for Na₄Ir₃O₈ between T=1.8 and 400 K before (black/open circles) and after (red/inverted triangles) subtraction of an impurity term (see text for details). Inset (i) shows the $1/\chi(T)$ data. The curve through the data is a fit by $\chi=\chi_0+C/(T-\theta)$. The inset (ii) shows M(H) at various T.

low-temperature κ was measured in a DR, using a standard four-wire steady-state method with two RuO₂ chip thermometers, calibrated in situ against a reference RuO₂ thermometer. Electrical transport (not shown) on sintered pellets showed insulating behavior with an activation gap of ≈ 500 K.

Figure 1 shows χ (open circles) versus T between 1.8 and 400 K. The data below $T \approx 25$ K show a sharp upturn suggesting contribution from a small amount of paramagnetic impurities. A fit to this low-T upturn by a Curie-Weiss behavior $\chi = \frac{C}{T-\theta}$ indicates that the upturn is well accounted for by $\approx 1\%$ S = 1/2 impurities. Subtracting this from the total χ , we obtain the red curve (inverted triangles) in Fig. 1. The corrected χ saturates to a large and T independent value $\chi \approx 9.4 \times 10^{-4}$ G cm³/Ir mol below T = 25 K, as it would in a metal, suggesting gapless excitations in Na₄Ir₃O₈. Inset (i) of Fig. 1 displays the $1/\chi(T)$ data. The data between T=300 and 400 K were fit by the Curie-Weiss expression $\chi = \chi_0 + \frac{C}{T - \theta}$. The fit shown in inset (i) of Fig. 1(a) as the curve through the data gave the values $\chi_o = 6.8(5) \times 10^{-5}$ cm³/mol/Ir, C =0.43(2) cm³ K/mol/Ir, and $\theta = -512(6)$ K. Assuming a gfactor g = 2, the above value of C corresponds to an effective magnetic moment $\mu_{\rm eff} = 1.85(5)\mu_{\rm B}$, which is close to that expected for $S_{\text{eff}} = 1/2$. The inset (ii) in Fig. 1 shows the magnetization M versus magnetic field H data at various T. The M(H) is linear at all T indicating the absence of any ferromagnetic or large amount of paramagnetic impurity in the sample consistent with the less than 1% impurities estimated above.

The above results of $\chi(T)$ indicate the presence of large antiferromagnetic interactions and the absence of long-range magnetic order down to $T=1.8~\rm K$. In addition, $\chi(T)$ is shown to saturate to a T-independent value at low temperature. These results are consistent with what was observed earlier lathough our Weiss temperature $\theta \approx -500~\rm K$ is significantly smaller than the value $-650~\rm K$ estimated in that report. We have used higher temperature ($T \leq 400~\rm K$) $\chi(T)$ data to estimate θ , which is probably more reliable given the large value of θ .

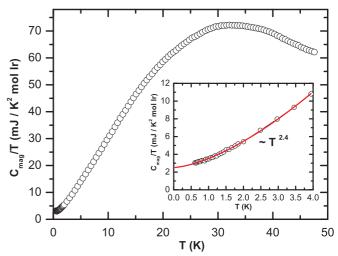


FIG. 2. (Color online) $C_{\rm mag}/T$ vs T between T=0.5 and 50 K, (inset) data below T=4 K. The solid curve through the data is a fit by $C=\gamma T+\beta T^n$ (see text for details).

In Fig. 2, we show the magnetic heat capacity divided by temperature C_{mag}/T versus T for Na₄Ir₃O₈ between T = 0.5and 50 K. C_{mag} was obtained by subtracting the C(T) data of Na₄Sn₃O₈ from the data of Na₄Ir₃O₈. C_{mag}/T shows a broad anomaly peaked at $T \approx 30$ K consistent with what was observed earlier. 11 We did not find any signature of long range magnetic order down to T = 0.5 K in our heat capacity data. An entropy of $R \ln 2$ expected for S = 1/2moments is recovered at $T \approx 50 \, \text{K}$, a temperature a little above the anomaly in C_{mag} . This suggests that the broad anomaly in C_{mag} could be the onset of short-ranged magnetic order. However, it could also be an indication of something more exotic like a crossover to a correlated spin-liquid-like state from a thermally disordered high temperature state dominated by nearest-neighbor interactions. A similar anomaly has been observed at T = 6 K in the organic spin-liquid candidate κ -(BEDT-TTF)₂Cu₂(CN)₃.⁵ In the case of the latter compound, NMR and μ SR measurements below this temperature did not detect signature of internal fields indicating that magnetic order was not causing the anomaly.

 $C_{\rm mag}$ below T=4 K is shown in the inset of Fig. 2. These data were fit by the expression $C=\gamma T+\beta T^n$. We were able to obtain an excellent fit, shown as the solid curve through the data in the inset of Fig. 2, with the values $\gamma=2.5(2)$ mJ/K² mol Ir, $\beta=3.0(1)$ mJ/mol K⁴, and n=2.41(2). An exponent n between 2 and 3 was also observed earlier for data measured down to T=2 K. 11 One of the mechanisms leading to this power-law behavior in C could be the predicted line-nodes in a spinon Fermi surface. 14,15 The most important conclusion from our low temperature C data is the presence of a small but finite linear-T term. In this insulating material where charge excitations are gapped, the linear term is expected to arise due to gapless spin excitations. We did not observe any signature of a Schottky anomaly associated with free paramagnetic impurities.

Figure 3 shows the thermal conductivity (κ) data for Na₄Ir₃O₈. Figure 3(a) shows the zero field κ/T versus T^2 data between T=2 and 47 K. The temperature dependence of κ is

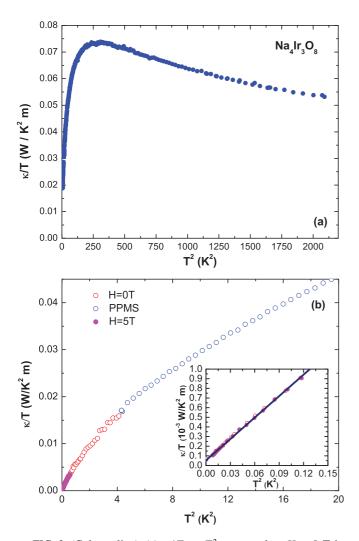


FIG. 3. (Color online) (a) κ/T vs T^2 measured at H=0 T in a PPMS. (b) κ/T vs T^2 at H=0 T and H=5 T measured in a dilution fridge. (Inset) κ/T vs T^2 data for $T\leqslant 0.4$ K to highlight the absence of a significant linear-T term.

typical of insulators with a dominant lattice contribution. The dilution fridge data between T=75 mK and 2 K is plotted along with the PPMS data in Fig. 3(b). Both sets of data match quite well. A signature of long-range magnetic ordering (spin-glass freezing) would be an abrupt (gradual) increase in κ due to freezing out of the spin disorder scattering below the ordering (freezing) temperature. The $\kappa(T)$ data in Fig. 3 do not show any signature of magnetic ordering or spin freezing down to 75 mK providing fresh evidence to support claims of a spin-liquid state in Na₄Ir₃O₈.

The data below $T \approx 0.4$ K are shown in Fig. 3(b) inset. The data extrapolate to $\kappa(0)/T = 6.3(9) \times 10^{-2}$ mW K²/m at T = 0 K. This is independent of magnetic field as can be seen from the H = 5 T data plotted along with the H = 0 T data in Fig. 3(b). The extrapolated T = 0 K value of $\kappa(0)/T$ is tiny and within errors is indistinguishable from zero. The fact that our samples are polycrystalline leads to two issues. At low temperatures when the phonon mean-free path becomes large, scattering from grain boundaries becomes important and phonon contribution to κ deviates from the diffuse scattering limit T^3 behavior. Thus there is no clear way of estimating

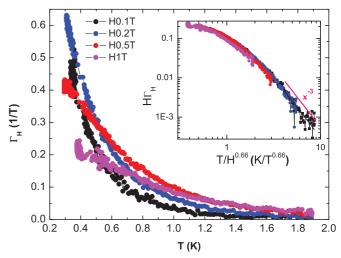


FIG. 4. (Color online) Magnetic Grüneisen parameter Γ_H vs T, (inset) scaling plot, $H\Gamma_H$ vs $T/H^{\nu z}$ with $\nu z=2/3$. At large $x=T/H^{\nu z}$, we observe a x^{-3} divergence.

and subtracting the phonon contribution to κ and getting out a magnetic or itinerant contribution. For the same reason, C and κ , which would otherwise be related, can not be compared in this case. Additionally, in our samples, the measured thermal conductivity, specially at low temperatures, will be lowered from its intrinsic value due to thermal resistance coming from grain boundary scattering. So $\kappa(0)/T=6.3(9)\times 10^{-2}$ mW K^2/m can be considered a lower limit.

We next present evidence for the proximity of $Na_4Ir_3O_8$ to a zero-field quantum critical point (QCP). Figure 4 shows the magnetic Grüneisen ratio Γ_H versus T data between T=0.3 and 2 K at various magnetic fields. A clear divergence of the Γ_H is observed at low fields. The divergence of the magnetic Grüneisen parameter is a typical signature of proximity to a field tuned QCP. Similar divergences have been observed at the field-induced QCP in the heavy fermion material YbRh₂Si₂. The divergence of Γ_H is suppressed at higher fields indicating that at these fields the system is being tuned away from the QCP.

Assuming that only a single diverging time scale governs the critical phenomena, the critical free energy, F_{cr} with magnetic field as control parameter can be expressed by $F_{cr} = aT^{(d+z)/z}\phi(bh/T^{1/\nu z})$, where $h=H-H_c$ (Refs. 22–24) and a and b are nonuniversal constants. Thus thermodynamic quantities that are derivative(s) of free energy are expected to collapse as a function of $T/h^{\nu z}$. Here, we present in Fig. 4 inset an excellent collapse of our data, when they are rescaled in a form $H\Gamma_H$ versus $T/H^{0.67}$, indicating $H_c=0$ and implying $\nu z=2/3$. These data demonstrate that Na₄Ir₃O₈ is situated at or close to a zero-field QCP.

By expanding the dimensionless argument $y=(bh)/T^{1/vz}$ in ϕ for high temperatures, $y\ll 1$, we obtain $\phi(y)\approx \phi(0)+1/2\phi''(0)y^2$, where the y-linear term (*H*-linear term) vanishes, because it would correspond to a spontaneous magnetization. Now, $\Gamma_H=[\partial^2 F_{cr}/(\partial T\partial H)]/[T\partial^2 F_{cr}/\partial T^2]$, yielding $\Gamma_H H\sim [b'T^{2/vz}/H^2+1]^{-1}$. Here b' is another nonuniversal constant. From this, we expect $\Gamma_H H\sim (T/H^{vz})^{-2/vz}$ at high T. The high T exponent, -3=-2/vz (solid line in Fig. 4 inset), is in perfect agreement with

vz = 0.67, obtained from the argument of scaling function, $\phi_T(T/H^{vz})$.

We note that Γ_H for H=0.2 T is larger than that for H=0.1 T in Fig. 4, which is counter-intuitive to expectation for a zero-field QCP. A crossing between two curves of Γ_H at different H is expected as a function of T for $H>H_c$. This is due to a crossover between high-temperature H-linear [since $\Gamma_H H \sim (T/H^{2/3})^{-3}$] and low-temperature 1/H regimes. For example, the curve for H=0.1 T crosses with that for H=1 T at 0.55 K and the curve for H=0.5 T at T=0.4 K. The crossing temperature decreases with decreasing field. From the scaling plot, the Γ_H curves for H=0.1 and 0.2 T are expected to cross below 0.3 K, which is the lowest temperature in our experiment.

In summary, we have shown that Na₄Ir₃O₈ is a fascinating material with several novel properties. We have presented three main results here. (i) The absence of long-range magnetic (or other) order down to T = 75 mK strongly supporting a spinliquid ground state. (ii) A suggestion of gapless excitations from finite terms in χ and C in the limit $T \to 0$: even though Na₄Ir₃O₈ is shown to be a Mott insulator from transport and magnetism, the χ becomes T-independent below $T \approx 25$ K and the heat capacity shows a small but finite linear-Tterm at the lowest temperatures. Since the charge excitations are gapped, the above implies the presence of gapless spin excitations in Na₄Ir₃O₈. The thermal conductivity, however, extrapolates to a tiny value $\kappa/T \approx 6.5 \times 10^{-2} \text{ mW/K}^2 \text{ m}$. The values of the linear-T terms in C and κ are both small. If we compare with the two-dimensional organic spin-liquid candidates ET-dmit ($\kappa/T \approx 180 \text{ mW/K}^2 \text{ m}, \gamma \approx 20 \text{ mJ/mol K}^2$) and κ -(BEDT-TTF)₂Cu₂(CN)₃ ($\kappa/T \rightarrow 0$,⁶ $\gamma \approx 20$ mJ/mol K²),⁵ we find that the case of Na₄Ir₃O₈ seems similar to the latter material where a relatively large γ is found but is not consistent with the vanishing linear-T term in thermal conductivity, both of which were obtained from measurements on single crystals.

Recent zero-field μ SR measurements on kappa-(BEDT-TTF)₂Cu₂(CN)₃ reveal a microscopic phase separation below about 3 K into gapless paramagnetic nanoislands embedded in a sea of a gapped singlet phase.²⁵ This was proposed as

a resolution to the conflicting results of C and κ because the heat capacity will measure both contributions (giving a net gapless result), whereas the thermal conduction between gapless islands will be cutoff by the gapped sea around the islands.²⁵ The absence of a significant $\kappa(0)/T$ for Na₄Ir₃O₈ could thus be a result of something exotic. Future microscopic measurements like NMR or μ SR would be useful in this regard. We would nevertheless like to stick our necks out and state that the evidence from C and χ at low T strongly suggest gapless excitations. These could arise, e.g., from a Fermi surface of spinons and in analogy with metals the small values of γ and $\kappa(0)/T$ might therefore suggest a small spinon density of states. This would be consistent with theoretical predictions of three small spinon Fermi surface pockets for Na₄Ir₃O₈. ¹⁴ These are, however, still speculations at this stage and direct evidence of the existence of a spinon FS in Na₄Ir₃O₈ is hardly established. (iii) The third main result of our work is proximity to a QCP: The divergence of Γ_H points to quantum criticality. The quantum criticality must be associated with an instability of the system to some nearby (possibly magnetic) ordered state. Note that Γ_H of fluctuating paramagnetic moments is independent of T. Therefore the observed scaling cannot be explained by an impurity contribution and provides strong evidence for quantum critical behavior in Na₄Ir₃O₈.

Note added in proof. A recent muSR measurement²⁶ on powder Na₄Ir₃O₈ samples prepared by Y.S. has shown the absence of long-range magnetic ordering or spin freezing at 5 K strongly supporting a SL ground state at least down to this temperature.

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