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# Specific heat and disorder in the mixed state of non-magnetic borocarbides

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**Abstract.** – The temperature and magnetic-field dependence of the specific heat  $c_p(T, H)$  in the superconducting (sc) mixed state as well as the upper critical field  $H_{c2}(T)$  have been measured for polycrystalline  $Y_xLu_{1-x}Ni_2B_2C$  and  $Y(Ni_{1-y}Pt_y)_2B_2C$  samples. The linear-in- $T$  electronic specific-heat contribution  $\gamma(H) \cdot T$  exhibits significant deviations from the usual linear-in- $H$  law resulting in a disorder-dependent negative curvature of  $\gamma(H)$ . The  $H_{c2}(T)$  data point to the quasi-clean limit for (Y, Lu)-substitutions and to a transition to the quasi-dirty limit for (Ni, Pt)-substitutions. The  $\gamma(H)$ -dependence is discussed in the unitary  $d$ -wave as well as in the quasi-clean  $s$ -wave limits. From a consideration of  $\gamma(H)$  data only,  $d$ -wave pairing cannot be ruled out.

*Introduction.* – The rare-earth (R) transition metal (T) borocarbide family  $RCT_2B_2$  (R = Y, Lu; T = Ni, Pd, Pt) contains superconductors with relatively high transition temperatures  $T_c$  up to 23 K [1, 2]. The coexistence of superconductivity and magnetism for members of this family, where R are magnetic rare-earth ions, has stimulated numerous studies of their thermodynamic properties in the sc and in the normal state. At first glance, most of those results support a classification of these materials as intermetallic phonon-mediated superconductors with a moderately strong coupling strength. However, clean  $RNi_2B_2C$  samples exhibit also some features unexpected for ordinary  $s$ -wave superconductors. We emphasize the unusual shape and the strong disorder dependence of the upper critical field  $H_{c2}(T)$  and a nearly  $T^3$ -scaling of the electronic specific heat  $c_{es}(T)$  in the sc state compared with exponential behaviour for ordinary  $s$ -wave superconductors [3].

According to Nohara *et al.* [4] the isoelectronic T-substitution does affect strongly the field dependence of the linear-in- $T$  electronic specific-heat contribution  $\gamma(H) \cdot T$  in the mixed state.

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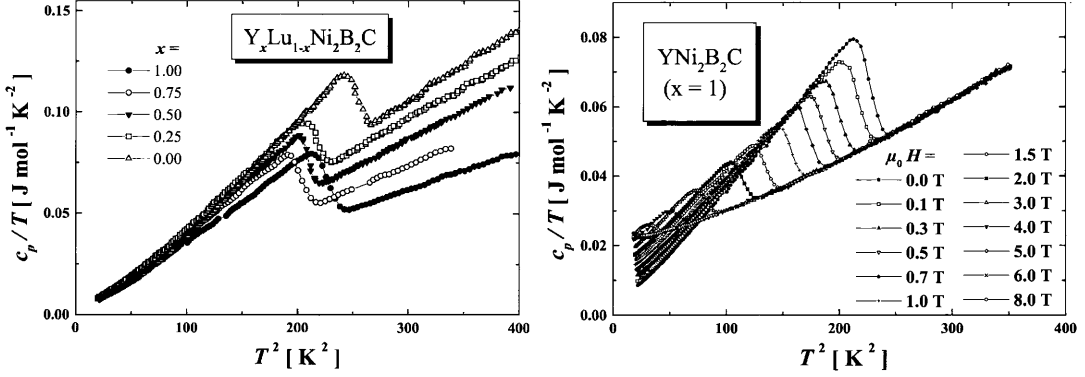


Fig. 1 – Zero-magnetic-field specific heat  $c_p(T)/T$  vs.  $T^2$  of the  $Y_xLu_{1-x}Ni_2B_2C$  series (left panel) and specific heat  $c_p(T, H)/T$  vs.  $T^2$  of  $YNi_2B_2C$  for various magnetic fields (right).

Thus, for an  $Y(Ni_{0.8}Pt_{0.2})_2B_2C$  single crystal,  $\gamma(H) \propto H$  has been found, while a square-root law was observed for a pure  $YNi_2B_2C$  single crystal and for polycrystalline  $LuNi_2B_2C$  [5]:

$$\gamma(H)/\gamma_N \propto \sqrt{H/H_{c2}(0)}, \quad (1)$$

where  $\gamma_N$  is the Sommerfeld constant in the normal state. Although the observed  $\gamma(H) \propto \sqrt{H}$ -law for  $YNi_2B_2C$  and  $LuNi_2B_2C$  was regarded initially as evidence for  $d$ -wave pairing [5, 6], the disorder-related transition from a  $\sqrt{H}$  to a linear-in- $H$  dependence was subsequently used to rule out  $d$ -wave superconductivity in non-magnetic borocarbides [4]. However, to the best of our knowledge, systematic investigations of this problem in a broader concentration range for  $Y(Ni_{1-y}Pt_y)_2B_2C$  are lacking. Since isoelectronic substitutions in the RC charge reservoir are expected to produce much weaker disorder than those in the TB network, we studied also the closely related  $Y_xLu_{1-x}Ni_2B_2C$  system for the sake of comparison [7]. By changing both compositions,  $x$  and  $y$ , deeper insight should be gained on how the disorder does affect the field dependence of the specific heat  $c_p(T, H)$ , the shape, and the magnitude of  $H_{c2}(T)$ , as well as the nature of the pairing state. It has recently been pointed out that possibly an unconventional mechanism is responsible for superconductivity in borocarbides [8].

*Experimental details.* – Polycrystalline  $Y_xLu_{1-x}Ni_2B_2C$  with  $x = 0, 0.25, 0.5, 0.75, 1$ , and  $Y(Ni_{1-y}Pt_y)_2B_2C$  samples with  $y = 0, 0.05, 0.1, 0.15, 0.2, 0.25, 0.5$ , and  $0.75$  were prepared by a standard arc melting technique. Powders of the elements were weighted in the stoichiometric compositions with a surplus of 10 wt.% boron to compensate losses of boron during arc melting. The powder was pressed to pellets which were melted in argon gas on a water-cooled copper plate in an arc furnace. To get homogeneous samples, they were turned over and melted again four times. After the melting procedure the solidified samples were homogenised at  $1100^\circ C$  for ten days. The specific heat was measured between  $4.2 K \leq T \leq 20 K$  increasing the temperature after the samples were cooled down from  $T > T_c$  in applied fields  $\mu_0 H \leq 8 T$  using a quasi-adiabatic step heating technique [9]. The upper critical field  $H_{c2}(T)$  was determined by taking  $T_c(H)$  from the onset of the jump of  $c_p$  in the particular field.

*Results and discussion.* – To illustrate typical specific-heat behaviour, the  $c_p/T$  vs.  $T^2$  data at  $H = 0$  of the  $Y_xLu_{1-x}Ni_2B_2C$  series and the corresponding curves for  $\mu_0 H \leq 8 T$  of the pure Y sample ( $x = 1$ ) are shown in fig. 1. Measurements at 8 T were used to analyse the normal-state specific heat  $c_p = \gamma_N T + \beta_D T^3$ , where  $\beta_D T^3$  is the Debye contribution. The Sommerfeld values  $\gamma_N$  were determined by extrapolating the  $c_p/T$  vs.  $T^2$  curves of the high

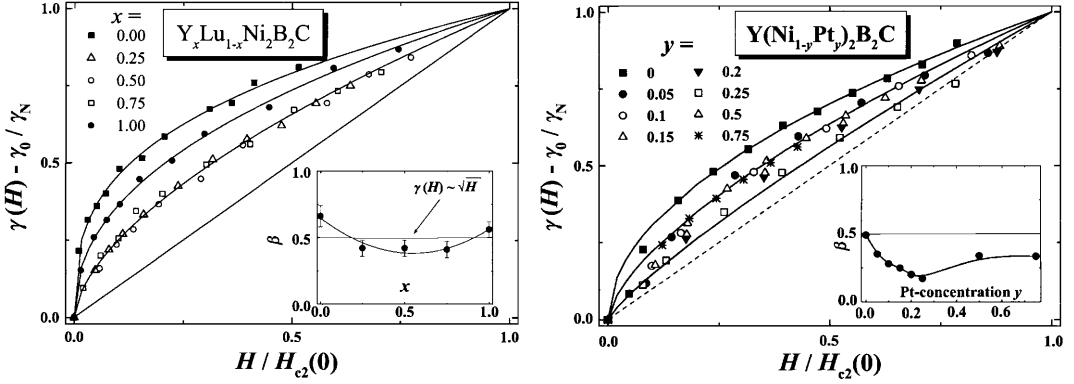


Fig. 2 – Magnetic-field dependence of the specific-heat contribution  $\gamma(H)$  of the vortex core electrons in the mixed state ( $H \leq H_{c2}$ ) normalized by  $\gamma_N$  and  $H_{c2}(0)$  (see fig. 4) for  $Y_xLu_{1-x}Ni_2B_2C$  (left panel) and  $Y(Ni_{1-y}Pt_y)_2B_2C$  (right panel). Residual  $\gamma_0 = \gamma(H = 0)$  values have been subtracted. The lines are fits according to eq. (2) and the straight reference line corresponds to the usual linear-in- $H$  s-wave dirty-limit behaviour. The insets show the curvature parameters  $\beta(x)$  and  $\beta(y)$  as defined in eq. (2).

field data in the normal state to  $T \rightarrow 0$ . By integrating specific-heat differences between the sc and normal state  $(c_s(T, 0 \text{ tesla}) - c_n(T, 8 \text{ tesla}))/T$  from  $T_c$  down to a temperature  $T < T_c$  the entropy conservation was checked resulting in the vanishing entropy difference between sc and normal state  $S_s - S_n$  for  $T \rightarrow 0$  and for  $T \rightarrow T_c$  and in a minimum in between. In this way we obtained  $\gamma_N = 20.4$  ( $x = 0$ ), 19.0 ( $x = 0.25$ ), 18.3 ( $x = 0.5$ ), 18.0 ( $x = 0.75$ ), and 20.2 mJ/mol K<sup>2</sup> ( $x = 1$ ) for our  $Y_xLu_{1-x}Ni_2B_2C$  series in good agreement with the data reported previously by several groups [10–16] and  $\gamma_N = 20.2$  ( $y = 0$ ), 20.2 ( $y = 0.05$ ), 18.4 ( $y = 0.1$ ), 16.4 ( $y = 0.15$ ), 16.2 ( $y = 0.2$ ), 16.9 ( $y = 0.25$ ), 15.3 ( $y = 0.5$ ), and 15.0 mJ/mol K<sup>2</sup> ( $y = 0.75$ ) for the  $Y(Ni_{1-y}Pt_y)_2B_2C$  series. The  $\gamma(H)$ -values obtained in the same way as the Sommerfeld values  $\gamma_N$  are represented in fig. 2. The entropy is conserved in applied fields, too. For all samples  $\gamma(H)$  is a sublinear function of  $H$ . At first generalizing eq. (1), the data were analysed by the expression

$$\frac{\gamma(H) - \gamma_0}{\gamma_N} = [H/H_{c2}(0)]^{1-\beta}, \quad (2)$$

where  $\gamma_0 = \gamma(H = 0)$  specifies the linear-in- $T$  contribution observed in the zero field and  $\beta$  measures the sublinearity (*i.e.* a negative curvature) of  $\gamma(H)$ .  $H_{c2}(0)$  is the field where  $\gamma(H)$  reaches  $\gamma_N$ . We obtained  $\beta = 0.66, 0.42, 0.42, 0.41$ , and  $0.56$  ongoing from  $x = 0$  to  $x = 1$  for  $Y_xLu_{1-x}Ni_2B_2C$  and  $\beta = 0.46, 0.35, 0.25, 0.25, 0.21, 0.17, 0.34$ , and  $0.33$  ongoing from  $y = 0$  to  $y = 0.75$  for  $Y(Ni_{1-y}Pt_y)_2B_2C$ , with uncertainties of  $\Delta\beta/\beta \leq 10\%$  due to the small residual  $\gamma_0$  and due to the procedure used to determine  $\gamma(H)$ , as mentioned above. For all our samples but  $Y(Ni_{0.75}Pt_{0.25})_2B_2C$  and  $Y(Ni_{0.5}Pt_{0.5})_2B_2$ , residual values  $\gamma_0 \leq 1.5$  mJ/mol K<sup>2</sup> are observed. For  $y = 0.25$  and  $0.5$  we find  $\gamma_0 = 3.4$  and  $3.3$  mJ/mol K<sup>2</sup>, respectively.

The dependence of  $\beta(x)$  is shown in the inset of fig. 2 and in fig. 4 (left panel).  $\beta$  reaches the largest values for the bordering cases  $x = 0$  and  $1$  and becomes markedly smaller in between. We note that our curvatures for  $LuNi_2B_2C$  and  $YNi_2B_2C$  exceed slightly the value of  $\beta = 0.5$  suggested by eq. (1) and that reported in refs. [4, 5]. To the best of our knowledge, the strong sublinearities for  $\gamma(H)$ , measured by the exponent  $\beta$ , of the borocarbides under consideration are the largest reported so far for any superconductor except for the recently

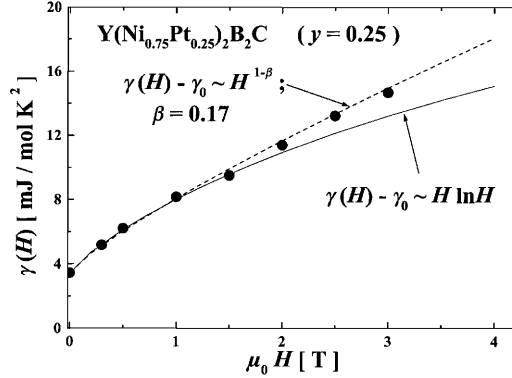


Fig. 3 – Magnetic-field dependence of  $\gamma(H)$  for  $\text{Y}(\text{Ni}_{0.75}\text{Pt}_{0.25})_2\text{B}_2\text{C}$ . The solid line is a fit according to eq. (3). The dashed line is a fit according to eq. (2) with  $\beta = 0.17$ .

discovered  $\text{MgB}_2$  ( $\beta = 0.77$ ) [17]. The  $\beta(y)$  behaviour is depicted in the inset of fig. 2 and in fig. 4 (right panel). The curvature parameter  $\beta$  is significantly reduced with increasing Pt concentrations  $y$  for  $y \leq 0.25$  and  $\beta(y)$  exhibits a *finite* minimum at about  $y = 0.25$  which is at variance with the linear law for an  $\text{Y}(\text{Ni}_{0.8}\text{Pt}_{0.2})_2\text{B}_2\text{C}$  single crystal reported in ref. [4]. We attribute that observation to a stronger disorder compared with our samples. Larger Pt concentrations ( $y > 0.25$ ) reveal even more pronounced  $\beta$  values, *e.g.*  $y = 0.5$ ;  $\beta = 0.34$  and  $\beta$  saturates at this value.

The observed  $\gamma(H) \propto H^{1-\beta}$ -law with  $\beta \approx 0.5$  raises the question whether an unconventional pairing mechanism is responsible for this peculiarity since, according to ref. [18],  $\gamma(H) \propto \sqrt{H}$  is a signature for a nodal order parameter with  $d$ -wave symmetry (a somewhat larger value  $\beta = 0.59$  has been found in ref. [19]) while  $\gamma(H) \propto H$  is usually expected for superconductors with isotropic  $s$ -wave order parameter. According to refs. [20, 21], Volovik's clean-limit  $d$ -wave approach can be generalized to describe also strong impurity scattering. Then at low magnetic fields  $H \ll H_{c2}(0)$  the specific-heat coefficient  $\gamma(H)$  follows an  $H \ln H$ -dependence:

$$\gamma(H) = \gamma_0 + \gamma_N D \left( \frac{H}{H_{c2}(0)} \right) \ln \left[ \frac{\pi}{2a^2} \left( \frac{H_{c2}(0)}{H} \right) \right], \quad (3)$$

where  $a$  and  $D$  are constants. Such a behaviour was observed for various disordered high- $T_c$  cuprates and considered as evidence for  $d$ -wave superconductivity in the unitary scattering limit [22, 23]. At the same time its applicability to non-magnetic borocarbides under consideration was disclaimed [22]. However, some of our data can be described equally well by eq. (3) for  $H/H_{c2}(0) \leq 0.3$  as well as by eq. (2) using intermediate values for  $\beta$  (0.15 to 0.35). This is shown in fig. 3: obviously, the  $H \ln H$  behaviour is not very distinct from the power law at low fields  $\mu_0 H \leq 1.5$  T. At higher fields the  $H \ln H$ -dependence may deviate since it was derived for low fields only [20]. The existence of a non-negligible  $\gamma_0$  is a feature predicted for a  $d$ -wave order parameter in the unitary limit [24] (large  $\gamma_0 \approx 3.3$  mJ/mol K<sup>2</sup> are obtained for  $y = 0.25$  and  $y = 0.5$ ). Hence,  $d$ -wave pairing cannot be ruled out in non-magnetic borocarbides by considering  $\gamma(H)$  data only. While the deviation from the linearity of  $\gamma(H)$  is frequently ascribed to a shrinking of the vortex cores with magnetic field and to vortex core interactions [4, 25, 26], recent investigations support the assumption of delocalized quasiparticle states around the vortex core to be responsible for this feature, in a similar way as in  $d$ -wave superconductors [27]. However, there are several conventional, but anisotropic  $s$ -wave superconductors which also exhibit deviations from the  $\gamma(H) \propto H$  law in the clean

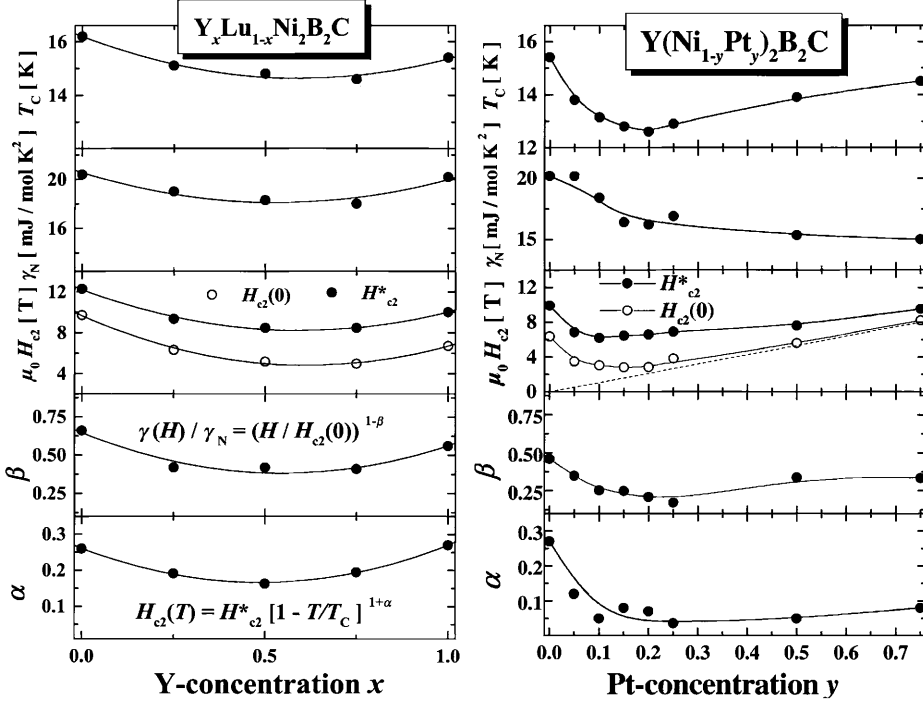


Fig. 4 – Composition dependence of the transition temperature  $T_c$  (upper panels), the Sommerfeld constant  $\gamma_N$  (second-row panels), the upper bound for the upper critical field  $H_{c2}^*$  according to eq. (4) and  $H_{c2}(0)$  according to eq. (2) (third-row panels; see text for more details), the specific-heat curvature exponent  $\beta$  of  $\gamma(H)$  according to eq. (2) (fourth-row panels), and the curvature exponent  $\alpha$  of the upper critical field  $H_{c2}$  according to eq. (4) (lower panels) determined for  $Y_x\text{Lu}_{1-x}\text{Ni}_2\text{B}_2\text{C}$  (left) and for  $Y(\text{Ni}_{1-y}\text{Pt}_y)_2\text{B}_2\text{C}$  (right). The lines are guides to the eye.

limit, *e.g.*  $\text{V}_3\text{Si}$  [28],  $\text{NbSe}_2$  [4] ( $\beta = 0.33$ ), and  $\text{CeRu}_2$  [19, 29]. Remarkably, a sublinear  $\gamma(H)$  behaviour has been reported also for the novel “medium- $T_c$ ” superconductor  $\text{MgB}_2$  [17, 30]. In this general context, recent ultrahigh-resolution photoemission spectroscopy measurements suggest that a highly anisotropic gap might be responsible for the above-mentioned peculiarities in clean Ni borocarbides [31]. By introducing disorder due to Pt substitution ( $y = 0.2$ ), a complete isotropization of the gap was observed. The highly anisotropic gap function is corroborated by magnetic-field-dependent thermal-conductivity data for  $\text{LuNi}_2\text{B}_2\text{C}$  in the mixed state [8]. The gap minimum  $\Delta_{\min}$  was reported to be at least 10 times smaller than the gap maximum  $\Delta_0$ ,  $\Delta_{\min} \leq \Delta_0/10$ , and possibly going to zero at nodes [8]. Calculations of the density of states (DOS) at the Fermi level,  $N(0)$ , in the mixed state with interacting vortices revealed a  $H^{0.67}$  ( $\beta = 0.33$ ) dependence of  $\gamma(H)$  for anisotropic *s*-wave superconductors [19].

Like  $\gamma(H)$ , the upper critical field  $H_{c2}(T)$  can be described also by a simple scaling law [32]:

$$H_{c2}(T) = H_{c2}^*(1 - T/T_c)^{1+\alpha}, \quad \text{valid for } 0.3 \leq T/T_c. \quad (4)$$

Our values of the upper critical field  $H_{c2}(0) \approx 0.9H_{c2}^*$  are reduced due to R-site substitution. A similar behaviour was found for the pronounced positive curvature of  $H_{c2}(T)$  near  $T_c$ , which is measured by the exponent  $\alpha$  in eq. (4), in contrast to the opposite statement of a nearly constant curvature [10]. The unusual positive curvature of  $H_{c2}(T)$  near  $T_c$  observed here can be explained for superconductors in the clean limit by a significant dispersion of the

Fermi velocities using, *e.g.*, an effective two-band model [33].  $T_c$  and  $\gamma_N$  are reduced to a smaller extent, which has been ascribed to a slight reduction of the electron-phonon coupling constant  $\lambda$  at intermediate  $x$  [34, 35]. For  $T_c$  a dip near  $x = 0.7$  is observed, in accordance with refs. [10, 32] ( $T_c \approx 14.6$  K at  $x = 0.75$ ). The dirty-limit region is not reached (which would be represented by vanishing  $\alpha$  and increasing  $H_{c2}(0)$  with increasing disorder [11, 12]).

In the case of Pt substitutions in the investigated range  $0 < y < 0.75$ , the values of  $T_c$ ,  $\beta$ , and  $H_{c2}(0)$  are reduced, too. As for R-substitutions, those sc properties exhibit minima at intermediate composition while the Sommerfeld constant  $\gamma_N$  and the curvature parameter  $\alpha$  of  $H_{c2}(T)$  depend monotonously on  $y$ . For  $y < 0.2$  a strong decrease of  $\alpha$  with increasing  $y$  is observed, but for  $y > 0.2$  an increase of  $\alpha$  does not occur (see fig. 4). This behaviour of  $H_{c2}$  suggests that the quasi-dirty limit has been reached at about  $y \approx 0.2$  since  $H_{c2}(0)$  increases linearly with  $y$  above  $y \approx 0.2$ , while the curvature of  $H_{c2}(T)$  measured by  $\alpha$  remains strongly reduced. In the dirty-limit case  $H_{c2}(0)$  is expected to increase linearly with the degree of disorder [11]. The results obtained for  $\text{Y}(\text{Ni}_{1-y}\text{Pt}_y)_2\text{B}_2\text{C}$  show that the deviations from the linearity of  $\gamma(H)$  measured by  $\beta$  are not correlated with the field exponent  $\alpha$ . While  $\alpha$  almost vanishes,  $\beta$  does increase for  $y > 0.25$ . Thus, here the behaviour of the specific heat in the vortex state even in the quasi-dirty limit remains rather complex.

To summarize, the deviations from the linear  $\gamma(H)$  behaviour we observe for the pure specimens of  $\text{Y}_x\text{Lu}_{1-x}\text{Ni}_2\text{B}_2\text{C}$  ( $x = 0; 1$ ) are only exceeded for the recently discovered  $\text{MgB}_2$  superconductor. Weak disorder effects caused by isoelectronic substitutions of Lu by Y yield a reduction of the  $\gamma(H)$ -nonlinearity without reaching the standard linear behaviour. Similar moderate suppressions of characteristic features which are typical for the quasi-clean limit have been found for the upper critical field  $H_{c2}(0)$ , the curvature exponent  $\alpha$ ,  $\gamma_N$ , and  $T_c$ . Stronger disorder effects are caused by isoelectronic substitutions of Ni by Pt. From the behaviour of  $H_{c2}(T)$  we deduce a transition from clean to quasi-dirty limit caused by isoelectronic substitutions at the T-site. The quasi-dirty limit is concluded from the nearly vanishing curvature of  $H_{c2}(T)$  and from the approximately linear increase of  $H_{c2}(0)$  with  $y$  for  $y \geq 0.2$ . At the same time there the sublinearity of  $\gamma(H)$  remains and does even increase. Hence, a simple monotonous relationship between  $\alpha$  and  $\beta$ , as one might expect by considering the results on  $\text{Y}_x\text{Lu}_{1-x}\text{Ni}_2\text{B}_2\text{C}$  only, does not hold in the quasi-dirty limit. In the case of intermediate deviations from the linearity of  $\gamma(H)$  ( $\beta = 0.15\text{--}0.35$ ), our results on specific heat at low magnetic fields are discussed in the context of a dirty *d*-wave model on the one hand and within the framework of the conventional *s*-wave picture in the quasi-clean limit on the other hand. At low fields the  $H \ln H$ -dependence of  $\gamma(H)$  predicted for *d*-wave pairing in the dirty (unitary) limit is not very distinct from the  $H^{1-\beta}$  behaviour which favours *s*-wave superconductivity in the quasi-clean limit. Thus, considering results on  $\gamma(H)$  a possible unconventional pairing mechanism in borocarbide superconductors cannot be ruled out.

*Additional Remark.* – Recently, the sublinear  $H$ -dependence of  $\gamma(H)$  has been addressed theoretically for a clean *s*-wave two-band superconductor [36]. It was found that  $\beta$  depends sensitively on the ratio of the two gaps of the strongly and weakly coupled bands. That appealing picture proposed for  $\text{MgB}_2$  might be transferred also to borocarbides under consideration. Then the two-band character manifests itself by two unusual curvature exponents  $\alpha$  and  $\beta$ .

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