"Non-Fermi-liquid" phenomena in heavy-fermion CeCu₂Si₂ and CeNi₂Ge₂

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Abstract

We report low-temperature results of specific-heat and resistivity measurements on the heavy-fermion (HF) compounds $CeCu_2Si_2$ and $CeNi_2Ge_2$. "Non-Fermi-liquid" effects are observed which suggest the nearness of an antiferromagnetic quantum critical point (QCP) in either system. The observed deviations from the properties of a Landau Fermi liquid (FL) agree with theoretical predictions and point to an anomalous energy dependence of both the quasiparticle mass and the quasiparticle-quasiparticle scattering cross section. However, the complexity of the B-T phase diagram of $CeCu_2Si_2$ as well as the specific-heat results for $CeNi_2Ge_2$ measured at high pressure (1.7 GPa) indicate that the physics of HF metals is richer than anticipated in the theoretical models.

Keywords: Heavy fermions; CeCu₂Si₂; CeNi₂Ge₂; Non-Fermi liquid; Quantum phase transition

1. Introduction

In a Kondo lattice as approximated by certain Ce intermetallics [1], the formation of a Néel state (with binding energy $k_{\rm B}T_{\rm RKKY} \sim J_{\rm loc}^2/W$) competes with the formation of a local Kondo singlet $(k_{\rm B}T_{\rm K} \sim \exp(W/J_{\rm loc}))$. Here $J_{\rm loc} < 0$ is the local 4f-conduction electron exchange integral and W the conduction bandwidth. For a critical value of $|J_{\rm loc}|$, tuned by a suitable control parameter (pressure or composition), antiferromagnetic (afm) order becomes suppressed, i.e. $T_{\rm N} \rightarrow 0$. Beyond this quantum critical point (QCP), the properties of a

coherent (Landau) Fermi liquid (FL) with strongly renormalized quasiparticles or heavy fermions (HF) is often observed; this heavy FL being characterized by huge coefficients γ and a in the T dependences of the 4f-derived specific heat, $\Delta C = \gamma T$, and the resistivity, $\rho - \rho_0 = \Delta \rho = aT^2$ [2]. Constituent to this Landau FL are short-range and short-lived ("quantum") afm fluctuations [3, 4] mediating the interactions between HF. These fluctuations grow in space and time when approaching the afm phase transition.

A "generalized" FL, with critically enhanced but finite quasiparticle mass m^* and anomalous energy dependences of both m^* and the quasiparticle-quasiparticle scattering cross section ($\sim a = \Delta \rho/T^2$), is predicted by renormalization group [5] as well as SCR spin-fluctuation [6]

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theory: At the QCP one expects the following asymptotic low-T laws: $\gamma = \Delta C/T = \gamma_0 - \alpha T^{1/2}$ and $\Delta \rho = \beta T^{3/2}$. At elevated temperatures, "crossover" behavior is predicted [6], i.e. γ should obey $\gamma'_0 \ln(T_0/T)$ and $\Delta \rho \sim T^{\rm e}$, $\varepsilon \simeq 1$, where T_0 is a characteristic spin-fluctuation temperature. Most published results concerning a QCP in Kondo-lattice systems were obtained with disordered systems. Whereas for $Ce_{1-x}La_{x}Ru_{2}Si_{2}$ ($T_{N} \rightarrow 0$ at $x_{c} = 0.08$) the overall $\gamma(T)$ and $\Delta \rho(T)$ dependences follow well [7] the aforementioned theoretical predictions [5, 6], a largely different criticality has been inferred for $CeCu_{6-x}Au_x$, $x_c = 0.1$, from the observation that within about two decades in T(down to 60 mK), $\gamma \sim \ln(T_0/T)$, $\Delta \rho \sim T$ and $\Delta \chi = \chi - \chi_0 \sim (-T^{1/2})$ [8]. Since in such a system disorder may play a crucial role, we present below a study of "non-Fermi-liquid" (NFL) effects in the two isostructural intermetallics CeCu₂Si₂ and CeNi₂Ge₂. With these compounds, the asymptotic T-dependences for both $\gamma(T)$ and $\Delta \rho(T)$ as predicted by [5, 6] can be verified for the first time in any undoped HF metal. Attempts to "tune" CePd₂Si₂ [9, 10] and Ce₇Ni₃ [11] through a QCP by application of pressure have furnished [9, 11] the aforementioned "crossover" behaviors [6] and, in the case of $CePd_2Si_2$ ($p \ge 2.7$ GPa), an asymptotic $T^{3/2}$ dependence of $\Delta \rho(T)$ [10].

2. Evidence for a quantum critical point in CeCu₂Si₂

A systematic study [12, 13] of polycrystalline off-stoichiometry $Ce_{1+x}Cu_{2+y}Si_{2+z}$ samples revealed that the different physical groundstates, previously established for high-quality single crystals [14, 15], could be related to different sectors within the narrow homogeneity range of the primary 1-2-2 phase in the chemical Ce-Cu-Si phase diagram: While Cu-rich samples are HF superconductors ("S type") below $T_c = 0.65$ K, in samples with small Ce and/or Cu deficiency a transition into "phase A" is found at $T_A \simeq 0.6-0.8$ K ("A type"). Though up to now not directly confirmed via neutron diffraction, phase A is associated by most researchers with some low-moment, antiferromagnetically ordered state, presumably of finite correlation length [16]. This interpretation is supported by recent investigations on the $CeCu_2(Si_{1-x}Ge_x)_2$ system [17]. In-between the S and A sectors, "AStype" behavior is observed in that upon cooling, the incipient A-phase transition becomes replaced by bulk superconductivity. Owing to the high sensitivity of phase A to control parameters such as sample composition or external pressure, one might be able to "tune" the system through a QCP at which $T_A \rightarrow 0$. Provided that phase A is, in fact, of afm nature clear deviations from the Landau-FL behavior as discussed above are expected. Fig. 1 shows $\gamma = \Delta C/T$ versus T on a logarithmic scale for a polycrystalline sample which exhibits a transition into phase A at $T_A \simeq 0.7$ K [18]. However, if an external pressure of 0.7 GPa is applied the A-phase transition is suppressed and replaced by a bulk superconducting one at $T_c \simeq 0.65$ K. The different natures of the respective p = 0 and 0.7 GPa transitions become evident when we apply a magnetic field B = 2 T, leaving the afm transition almost unchanged but suppressing superconductivity.

In the inset of Fig. 1 our $\Delta C(T)/T$ results taken at B = 2 T and p = 0.7 GPa and are plotted versus $T^{1/2}$. For $T \leq 1.2$ K, the data obey well $\gamma(T) = \gamma_0 - \alpha T^{1/2}$, with $\gamma_0 \simeq 0.99$ J/K² mol and



Fig. 1. $\Delta C/T$ versus T (on a logarithmic scale) for an A-type polycrystalline CeCu₂Si₂ sample measured at p = 0 and 0.7 GPa, B = 0 (open symbols) and 2 T (closed symbols). p = 0 data display A-phase, p = 0.7 GPa (B = 0 T) data superconducting transition. Inset shows p = 0.7 GPa (B = 2 T) data as $\Delta C/T$ versus $T^{1/2}$.

 $\alpha \simeq 0.38 \text{ J/K}^{2.5}$ mol. As inferred from the main part of Fig. 1, for higher T we find the expected [6] crossover law $\gamma(T) = \gamma'_0 \ln(T_0/T)$. These observations lend further support to phase A representing some (itinerant) afm ordered state.

Since we expect the A-phase transition temperature T_A to vanish within the "S" sector of the homogeneity range, we address below the (p = 0)n-state properties of an S-type CeCu₂Si₂ single crystal, identical to that studied in Ref. [14]. In Fig. 2(a), we show the *T*-dependence of its resistivity which, down to the lowest temperature of 20 mK, obeys well $\rho = \rho_0 + \beta T^{3/2}$ ($\rho_0 = 36 \,\mu\Omega \,\text{cm}$, $\beta = 14.9 \,\mu\Omega \,\text{cm} \,\text{K}^{-1.5}$ for $B = 4 \,\text{T}$). This *T*-dependence holds for $T < 1.7 \,\text{K}$ and $B \leq 5 \,\text{T}$; see Fig. 2(b).

For B > 6 T, the low-temperature resistivity turns into $\Delta \rho = aT^2$, characterized by a huge almost field-independent coefficient, and $a \simeq 10 \ \mu\Omega \ \mathrm{cm} \ \mathrm{K}^{-2}$. The apparent change from "NFL" behavior at $B \leq 5$ T to "FL" behavior at B > 6 T is substantiated by magnetoresistivity results: In an isothermal field sweep at T = 20 mK, $\Delta \rho(B)$ changes sign from an anomalous $\Delta \rho(B) < 0$ for $B_{c2}(T = 20 \text{ mK}) < B \leq 5 \text{ T}$ to $\Delta \rho(B) > 0$ (as commonly found in a coherent FL) for B > 6 T. For $8 T \le B \le 15.5 T$, the highest field accessible, the T² dependence of $\Delta \rho(T)$ precedes the transition into the (as yet unidentified) high-field "phase B"

(Fig. 2(b)), first discovered for an AS-type single crystal [15]. The B-phase transition manifests itself in an increase of the resistivity for $T \leq T_{\rm B}$.

Compared to the resistivity behavior, the temperature and field dependences of the specific heat as determined for the same single crystal [19] are more complex [20]. This observation highlights a more realistic theoretical treatment of an afm QCP in CeCu₂Si₂, a HF compound with an anisotropic, multi-component quasiparticle system [21].

3. "Non-Fermi-liquid" effects in CeNi₂Ge₂

In order to investigate a "simple" reference compound isostructural to CeCu₂Si₂, recent activities have been devoted to non-afm ordered CeNi₂Ge₂, with $\gamma_0 \simeq 350 \text{ mJ/K}^2 \text{ mol}$ [22] ($\simeq \gamma_0/2$ of CeCu₂Si₂). Though a peak near $T \simeq 30 \text{ K}$ [23] in $\chi_c(T)$, the susceptibility measured along the easy *c* direction, points to some short-range afm fluctuations, a low-*T* anomaly in $\chi_c(T)$ [23] suggests "NFL" behavior. The latter may be related to an afm QCP in Ce(Ni_{1-x}Cu_x)₂Ge₂ with low critical Cu concentration, $x_c < 0.2$ [13, 20].

In Fig. 3 we show new specific-heat results on a polycrystalline $CeNi_2Ge_2$ sample. While, at



Fig. 2. (a) Resistivity of S-type CeCu₂Si₂ single crystal at B = 4 T, applied parallel to the a axis. (b): B-T diagram displaying superconducting (sc) and B phase as well as ranges in which the resistivity shows "FL" ($\Delta \rho \sim T^2$) and "NFL" ($\Delta \rho \sim T^{3/2}$) behavior, respectively.



Fig. 3. Field dependence of $\Delta C/T$ versus T (on a logarithmic scale) for polycrystalline CeNi₂Ge₂ sample. Arrows mark onset of low-T "FL" regime for B = 4, 6 and 8 T, respectively (from Fig. 4(a)). Inset: B = 0 data on a linear temperature scale. Solid line represents $\Delta C/T = \gamma_0 - \alpha T^{1/2}$, see text.

B = 0, γ(T) = ΔC(T)/T ~ ln(T₀/T) for 1 K ≤ T ≤ 4 K, at lower T it follows γ(T) = γ₀ − αT^{1/2} (γ₀ ≃ 0.42 J/K² mol; α ≃ 0.1 J/K^{2.5} mol); see inset of Fig. 3. These observations are corroborated by our resistivity results on several (poly- and single crystalline) CeNi₂Ge₂ samples, showing residual resistivities between 1.5 and 2.5 μΩ cm: For 2.5 K < T < 10 K (B = 0) we find Δρ ~ T^ε, ε ≃ 1.2, but for T < 2.5 K (B = 1 T), again Δρ = βT^{3/2} (β = 0.22 μΩ cm K^{-1.5}) holds down to 20 mK.

The isothermal magnetoresistivity indicates a change, at $B = B_{\ell}$, from a negative to a positive field coefficient, i.e. from anomalous scattering off long-range, long-lived afm fluctuations at low fields to scattering off some short-range, short-lived fluctuations, typical for a coherent FL, at higher fields (see Fig. 4(a)). In fact, as can be seen in Fig. 4(b), for B > 2 T, $\Delta \rho(T)$ is found to be $\sim T^2$ below some limiting temperature T_{ℓ} . As inferred from Fig. 4(a), a nearly quadratic relationship exists between B_{ℓ} and T_{ℓ} . The arrows in Fig. 3 indicate that the regime, in which $\Delta \rho \sim T^2$ holds, satisfactorily coincides with the one in which γ becomes almost independent.

However, this field-induced "FL" state shows scaling properties strongly different from that of a canonical heavy FL [2]: In the latter,



Fig. 4. B-T phase diagram for CeNi₂Ge₂ as derived from resistivity measurements (a), including change from negative (low B) to positive (high B) magnetoresistivity as well as ranges in which the resistivity shows "NFL" ($\Delta \rho \simeq T^{3/2}$) and "FL" ($\Delta \rho \sim T^2$) behavior. Their limits are indicated by dashed lines, the latter being described by $B_{\ell} = AT_{\ell}^2$, see text. T_{ℓ} values for fixed values of B_{ℓ} are read off ρ versus T^2 plots in (b) (arrows).

 $\gamma \simeq 0.3 \text{ J/K}^2$ mol would relate to a $T_{\rm K}$ of the order of several tens of K, while in Fig. 3 broad humps near T = 1 K occur in $\Delta C/T$ versus T (for B = 6and 8 T). In addition, for B = 8 T the coefficient a of the low-T $\Delta \rho = aT^2$ law is found to be too small by one order of magnitude when compared to the a value expected from the "universal" $a \sim \gamma^2$ relation for HF compounds [2].

If an external pressure of p = 1.3 GPa is applied to CeNi₂Ge₂, the "NFL" effects are found to be completely suppressed. Rather, one observes a constant $\gamma \simeq 150$ mJ/K² mol for $T \le 5$ K, typical of a moderately heavy Landau FL: At p = 1.7 GPa, $\gamma \simeq 130$ mJ/K² mol is even somewhat smaller. Fully unexpectedly, a non-superconducting second-order phase transition at $T_1 = 1$ K was recently discovered [20] at this pressure.

4. Outlook

For both CeCu₂Si₂ and isostructural CeNi₂Ge₂ distinct low-temperature anomalies have been found in the T dependences of $\gamma = \Delta C/T$ and $\Delta \rho$: $\gamma(T) = \gamma_0 - \alpha T^{1/2}$ and $\Delta \rho = \beta T^{3/2}$ suggest the nearness of an afm QCP in either system, i.e. (in space and time) slowly varying fluctuations of an afm order parameter [5, 6]. In the case of CeNi₂Ge₂, this holds for relatively low values of external magnetic field and hydrostatic pressure. The near degeneracy of two collective states in CeCu₂Si₂, i.e. HF superconductivity and phase A, as well as the occurrence of the additional (highfield) phase B display a more complex behavior of this canonical HF compound. Inconsistencies found between the $\gamma(T, B)$ [19] and $\Delta \rho(T, B)$ results for an S-type single crystal highlight a theoretical treatment of the QCP in CeCu₂Si₂, by taking into account its strongly anisotropic, multi-component quasiparticle system [21].

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