

Adiabatic demagnetization refrigeration to millikelvin temperatures with the distorted square lattice magnet NaYbGeO₄

U. Arjun^{1,2,*}, K. M. Ranjith³, A. Jesche², F. Hirschberger², D. D. Sarma¹, and P. Gegenwart^{2,†}

¹*Solid State and Structural Chemistry Unit, Indian Institute of Science, Bengaluru-560012, India*

²*Experimental Physics VI, Center for Electronic Correlations and Magnetism, Institute of Physics, University of Augsburg, 86135 Augsburg, Germany*

³*Laboratoire National des Champs Magnétiques Intenses-EMFL, CNRS, Université Grenoble Alpes, 38042 Grenoble, France*



(Received 28 September 2023; accepted 13 November 2023; published 11 December 2023)

We report the synthesis, characterization, low-temperature magnetic, and thermodynamic measurements of the millikelvin adiabatic demagnetization refrigeration (mK-ADR) candidate material NaYbGeO₄ which exhibits a distorted square lattice arrangement of YbO₆ magnetic units. Magnetization and specific heat indicate weakly interacting effective spin-1/2 moments below 10 K, with a Curie-Weiss temperature of only 15 mK, that can be polarized by magnetic fields of order 1 T. For the ADR performance test, we start the demagnetization from 5 T at a temperature of ~ 2 K and reach a minimum temperature of 150 mK at zero field. The warming curve indicates a sharp magnetic transition in the heat capacity at 210 mK, implying only weak magnetic frustration. The entropy density of $S_{GS} \simeq 101$ mJ K⁻¹cm⁻³ and hold time below 2 K of 220 min are competitive while the minimal temperature is higher compared to frustrated Ytterbium-oxide ADR materials studied under similar conditions.

DOI: [10.1103/PhysRevB.108.224415](https://doi.org/10.1103/PhysRevB.108.224415)

I. INTRODUCTION

Ultralow temperatures below 1 K are often prerequisites for the occurrence of quantum phenomena in condensed matter and, respectively, key for modern quantum technologies. The global helium shortage [1–5] and the rising need for millikelvin (mK) refrigeration lead to a resurrection of adiabatic demagnetization refrigeration (ADR), a long-established helium-free cooling technique [6–8]. ADR cooling has the advantage of having less environmental impact and saving almost one-third of energy [9], and it can be used in various applications such as quantum computation [10], space technologies [11–15], etc. For mK-ADR applications, materials with a significant entropy change (in the temperature range of 20 mK to 5 K) and a strong magnetocaloric effect (MCE) [16] (in a minimal applied magnetic field) are preferred. In ADR, the coolant material is precooled in a magnetic field of a few teslas and then adiabatically demagnetized. Due to the low entropy of the material after precooling in the field, adiabatic demagnetization requires a further temperature reduction to mK. Recent advances in continuous mK-ADR address the ineffectiveness of ADR compared to ³He-⁴He dilution refrigeration for continuous refrigeration [12,17]. Commercial continuous refrigerators based on ADR are already available on the market, suggesting their potential as a significant refrigeration advancement [18].

For cooling down to mK, hydrated paramagnetic salts such as CrK(SO₄)₂ · 12H₂O (CPA), which orders at 30 mK, are

typically used in commercial ADR setups [19]. However, the necessary dilution of magnetic moments in hydrated paramagnetic salts drastically reduces the volumetric cooling power. Conversely, materials with higher concentrations of magnetic ions may exhibit enhanced exchange couplings, leading to magnetic order. The presence of magnetic ordering hinders further adiabatic refrigeration, as it reduces entropy toward zero and sets a temperature limit for ADR [20]. While an ideal refrigerant would be a perfect paramagnet with maximum entropy at zero field around 0 K, actual paramagnetic substances inevitably have weak interactions that affect their refrigeration performance by limiting the minimal ADR temperatures. In addition, hydrated organic paramagnetic salts need vacuum-tight encapsulation due to high water vapor pressure and there is a limitation in properly baking them above 100 °C for UHV uses. Additionally, they have very poor intrinsic thermal conductivity, which requires the elaborate incorporation of metal wires into the encapsulated ADR pills [21].

To overcome the disadvantages of hydrated paramagnetic salts for mK-ADR, other different material classes were explored. These include frustrated [20,22–28], quantum critical [29,30], and molecular magnets [31,32], as well as metallic rare-earth compounds [33,34]. Among them, geometrically frustrated Ytterbium oxides like KBaYb(BO₃)₂ [20] and (Na/K)YbP₂O₇ [28], combine several advantages: minimal ADR temperatures well below 50 mK, in combination with larger volumetric entropy density compared to hydrated paramagnetic salts, and, most importantly, chemical stability. ADR pellets based on these materials can easily be prepared by pressing polycrystals with fine silver powder (to ensure optimal thermal contact at low temperatures) and upscaled to the kilogram range.

*arjunu@iisc.ac.in

†philipp.gegenwart@physik.uni-augsburg.de

As a result of spin orbit coupling and crystal electric field (CEF) splitting of the Yb^{3+} states in an octahedral environment, a Kramers doublet with effective spin $1/2$ moments arises in these materials at low temperatures. The effect of geometrical frustration in triangular rare-earth magnets has recently been investigated in YbMgGaO_4 and AYbX_2 (A =alkali metal, $X = \text{Se, S, O}$) [35–42]. Absence of long-range order together with broad excitation continua was related to the effect of geometrical frustration. In addition, the structural randomness of Mg^{2+} and Ga^{3+} in the former material gives rise to broad CEF splittings and broad distributions of the g factors and exchange interactions. The structural randomness is therefore detrimental to long-range order and could mimic spin liquid behavior [43]. $\text{KBaYb}(\text{BO}_3)_2$, with 40% larger Yb-Yb distance compared to YbMgGaO_4 and no direct Yb-O-Yb links, features similar structural randomness of K^+ and Ba^{2+} atoms, occupying the same position in the crystal lattice. This randomness could, together with frustration, further enhance the ADR performance [20]. For isostructural $\text{KBaGd}(\text{BO}_3)_2$, which orders magnetically at 0.26 K, a minimal temperature of 0.12 K was obtained [27]. Indeed, the phase transition in this material is strongly broadened and of triangular instead of λ -type shape, implying that the entropy release has been shifted by structural randomness toward much lower temperatures. More generally, the previous results motivate the investigation of other than triangular lattices without structural randomness with respect to their mK-ADR performance.

In the spin- $1/2$ 2D frustrated square lattice (FSL) model or J_1 - J_2 model, frustration may arise due to competing nearest-neighbor J_1 (along the edge) and next-nearest-neighbor J_2 (along the diagonal) interactions [44–49]. If both J_1 and J_2 are antiferromagnetic (AF), frustration arises, leading to interesting phases. The spin- $1/2$ FSL exhibits a rich theoretical phase diagram with various ground states depending on J_1 and J_2 or the frustration parameter $\alpha = J_1/J_2$ [49,50]. The model exhibits classical ground states characterized by ferromagnetic (FM) order, Néel AF order, and columnar AF order. At the boundary between the latter two, a QSL state has been predicted for $J_2/J_1 \simeq 0.4$ to 0.6. Furthermore, a spin nematic phase is predicted between the FM and columnar AF phase [49,50]. Although there are several spin- $1/2$ FSL candidate systems based on transition metals that fit well within the theoretical phase diagram [49,50], there are yet no good examples of rare-earth-based spin- $1/2$ FSL candidate systems.

In this paper, we report a thorough investigation down to mK temperatures on NaYbGeO_4 , with effective $1/2$ spins on a structurally ordered distorted square lattice. We do not find evidence for magnetic frustration. Instead the material displays a sharp λ -type phase transition in the heat capacity at 0.21 K. Indeed, the minimal ADR temperature after demagnetization to zero field under similar conditions to previous studies on $\text{KBaGd}(\text{BO}_3)_2$ [27] and $(\text{Na/K})\text{YbP}_2\text{O}_7$ [28] is only 0.15 K, while the warm-up time is enhanced compared to that of the two latter systems, as could also be expected from the $\sim 60\%$ higher entropy density. Altogether, the comparison supports the previous conjecture, that magnetic frustration and randomness are beneficial for optimized ADR performance.

II. METHODS

Synthesis: Polycrystalline samples of NaYbGeO_4 were synthesized by solid-state reaction, annealing the stoichiometric mixture of Na_2CO_3 (99.99%), Yb_2O_3 (99.99%), and GeO_2 (99.99%) in an alumina boat at 1000 °C for NaYbGeO_4 for a duration of 48 h with one intermediate grinding and pelletization.

Powder x-ray diffraction: The phase purity of the samples was confirmed by powder x-ray diffraction (XRD, PANalytical powder diffractometer with $\text{Cu } K_\alpha$ radiation, $\lambda_{\text{ave}} = 1.54182 \text{ \AA}$) at room temperature. Rietveld refinement of the observed XRD patterns was performed using the FullProf package [51] (see Fig. 2), taking the initial parameters from [52].

DC magnetization: DC magnetization (M) was measured as a function of temperature T and applied magnetic field H using the SQUID magnetometer with He-3 option [MPMS-3, Quantum Design].

Specific heat: Specific heat [$C_p(T)$], was measured using the heat capacity option of the PPMS (Quantum Design). For the low temperature ($0.4 \text{ K} \leq T \leq 2.2 \text{ K}$) C_p measurements, the ^3He probe (Quantum Design) was utilized in the PPMS. Furthermore, we calculated the heat capacity below 0.4 K from the warming curve in the ADR experiment (see below).

To achieve strong thermal coupling, pellets made with NaYbGeO_4 (grain diameter 10–50 μm) and fine silver powders (grain diameter 1 μm) in a mass ratio of 1 : 1 were used for specific heat measurements. To obtain the specific heat of the sample, the contribution of silver was subtracted from the raw data. The specific heat C_p in a magnetic insulator has significant contributions from phonons (C_{ph}) and the magnetic moments (C_{m}). At high temperatures, $C_p(T)$ is entirely dominated by C_{ph} , while at low temperatures, it is dominated by C_{m} . For estimating the C_{ph} , the zero-field data were fitted by a polynomial function $C_{\text{ph}}(T) = aT^3 + bT^5 + cT^7$ above 10 K, where a , b , and c are appropriate constants [53]. Similar procedures have been adopted earlier and proven to be efficient in cases where heat capacity data of nonmagnetic analog compounds are unavailable [54–57]. The fit was extrapolated down to low temperatures, and C_{m} was obtained by subtracting the fitted data from the experimental C_p data. The magnetic entropy was estimated as $S_{\text{m}}(T) = \int_{0.4 \text{ K}}^T \frac{C_{\text{m}}(T')}{T'} dT'$.

Adiabatic demagnetization refrigeration (ADR): A home-made ADR setup for the PPMS was utilized [20,27,28]. A cylindrical pellet made from equal weights of NaYbGeO_4 (grain diameter 10–50 μm) and silver powder (grain diameter 1 μm) was pressed weighing approximately 3.5 g, with 15 mm diameter and 6 mm thickness. The pellet was mounted on a plastic straw and thermally isolated from the heat bath. A RuO_2 thermometer was attached to the pellet and connected through thin resistive manganin wires to minimize the heat flow. The resistor was measured with a current of 1 nA utilizing a Lake-Shore 372 AC bridge. To minimize the effects of surrounding thermal radiation, a metallic cap was utilized as a shield. The sample was cooled to $T \approx 2 \text{ K}$ at 5 T and then the high-vacuum mode (pressure $< 10^{-4}$ mbar) was applied to achieve thermal decoupling. Subsequently, the magnetic field was swept to zero at a rate of 0.15 T min^{-1} . The pellet reached

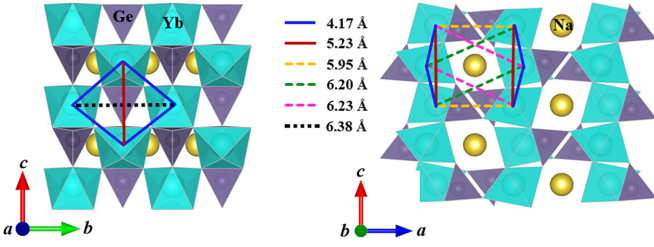


FIG. 1. Crystal structure of NaYbGeO₄. The YbO₆ octahedra are linked via GeO₄ tetrahedra and span a distorted square lattice grid (left panel). Right panel shows the possible connections between the square lattice grids. Different Yb-Yb distances are color coded.

its lowest temperature and then slowly warmed back to 2 K via slow heat flow from the bath.

III. RESULTS

A. Structure

The compound NaYbGeO₄ crystallizes in the orthorhombic crystal structure with space group *Pnma* (No. 62). The crystal structure of NaYbGeO₄ contains a distorted diagonally connected square lattice arrangement of YbO₆ octahedra carrying the magnetic moments connected through GeO₄ tetrahedra along the *bc* plane (see left panel of Fig. 1). The possible interaction pathways between these square lattice layers are shown in the right panel of Fig. 1. From the structure, the nearest neighbor exchange is through corner-shared YbO₆ octahedra, while the second neighbor exchange is through GeO₄ tetrahedra. Both distances are smaller than 5.5 Å, beyond which typically dipolar coupling dominates in other Ytterbium oxides [27].

B. Powder x-ray diffraction

Figure 2 shows the powder XRD pattern of NaYbGeO₄ at room temperature, along with the Rietveld refinement. The refinement is done using the orthorhombic space group *Pnma* (No. 62), taking initial parameters from Ref. [52]. The goodness of the fit is $\chi^2 = 4.19$. The obtained lattice parameters are $a = 11.2633(5)$ Å, $b = 6.3756(3)$ Å, $c = 5.2344(2)$ Å,

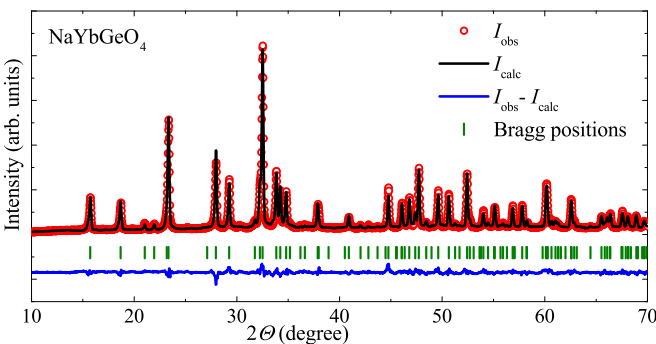


FIG. 2. Powder x-ray diffraction pattern (open red circles) for NaYbGeO₄ at room temperatures. The solid line represents the Rietveld refinement, with the vertical bars showing the expected Bragg peak positions and the lower solid blue line representing the difference between observed and calculated intensities.

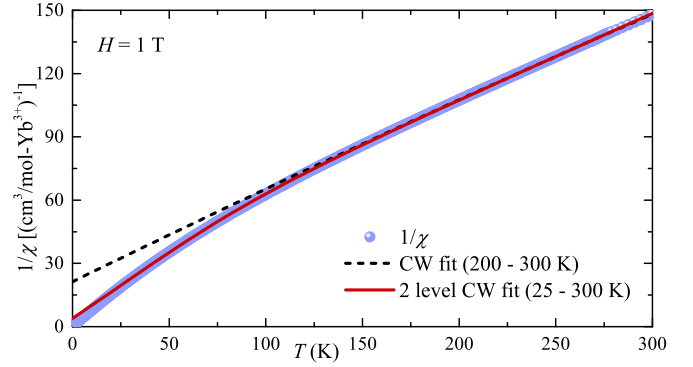


FIG. 3. Inverse magnetic susceptibility $1/\chi$ vs temperature of NaYbGeO₄ at a field of 1 T. Dashed and solid lines represent the fits by Eq. (1) and Eq. (2), respectively.

and $V_{\text{cell}} \simeq 375.89$ Å³. These values are in close agreement with the reported values [52].

C. Magnetization

Figure 3 displays the inverse magnetic susceptibility $\chi(T)^{-1} = H/M$ of NaYbGeO₄ at 1 T field together with an extended Curie-Weiss (CW) fit according to

$$\chi(T) = \chi_0 + \frac{C}{T - \theta_{\text{CW}}}, \quad (1)$$

which describes very well the high- T region between 200 and 300 K. Here, χ_0 is the T -independent contribution consisting of the diamagnetic susceptibility (χ_{core}) of core electron shells and the Van Vleck paramagnetic susceptibility (χ_{VV}) of the open shells of the Yb³⁺ ions. The second term in Eq. (1) is the CW law with the CW temperature θ_{CW} and Curie constant $C = N_A \mu_{\text{eff}}^2 / 3k_B$. Here, N_A is Avogadro's number, $\mu_{\text{eff}} = g\sqrt{J(J+1)}\mu_B$ is the effective magnetic moment, g is the Landé g factor, μ_B is the Bohr magneton, and S is the spin quantum number. The fitting parameters are $\chi_0^{\text{HT}} \simeq 4.34 \times 10^{-4}$ cm³/mol, $C_{\text{HT}} \simeq 2.19$ cm³K/mol, and $\theta_{\text{CW}}^{\text{HT}} \simeq -47.1$ K. From the value of C_{HT} , the effective moment is obtained to $\mu_{\text{eff}}^{\text{HT}} \simeq 4.19\mu_B$, in good agreement with the expected spin-only value of $4.54\mu_B$ for the Yb³⁺ ($J = 7/2$, $g = 8/7$) ion in the $4f^{13}$ configuration. The large value of the CW temperature arises from the CEF splitting. This is evident from the curvature in $\chi^{-1}(T)$ below 200 K leading to a change in slope below 50 K, as excited CEF levels become thermally depopulated. Such behavior is typical for Yb³⁺-based spin systems where CEF splits the $J = 7/2$ multiplet into four Kramers doublets. Our entropy analysis below confirms the presence of a Kramers doublet ground state at temperatures below 10 K. Figure 3 also includes a two-level fit [58] (cf. the red solid line) according to

$$1/\chi(T) = 8(T - \theta_{\text{CW}}) \left(\frac{\mu_{\text{eff},1}^2 + \mu_{\text{eff},2}^2 \cdot e^{(-\Delta/T)}}{1 + e^{(-\Delta/T)}} \right)^{-1}, \quad (2)$$

where $\mu_{\text{eff},1}$ and $\mu_{\text{eff},2}$ correspond to energy levels separated by an energy gap Δ . The fit down to 25 K yields $\Delta \simeq 282$ K, $\mu_{\text{eff},1} \simeq 3.57\mu_B$, $\mu_{\text{eff},2} \simeq 5.11\mu_B$, and $\theta_{\text{CW}} \simeq -6.1$ K. The deviation of the fit from the data below 30 K indicates that the

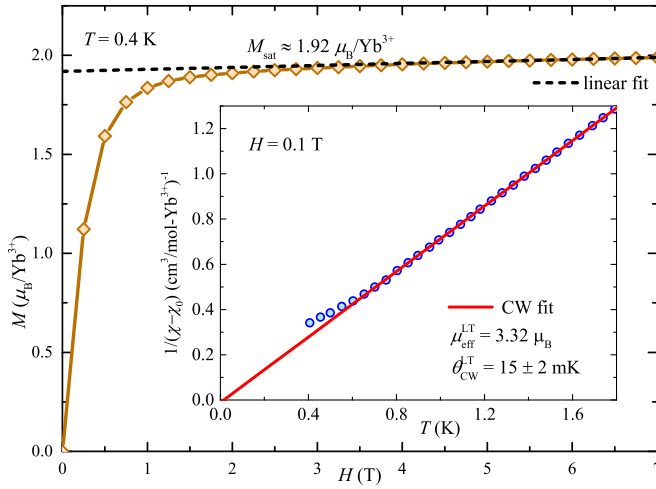


FIG. 4. Isothermal magnetization $M(H)$ of NaYbGeO₄ at a temperature of 0.4 K. Dashed line represents linear contribution (see text). The inset shows the low-temperature inverse magnetic susceptibility after subtracting χ_0 along with the CW fit.

obtained $\mu_{\text{eff},1}$ and θ_{CW} do not represent the lowest Kramers doublet. Using a fitting approach that incorporates four CEF levels and their associated effective moments is challenging due to the excessive number of adjustable parameters. Hence, we analyzed the magnetic susceptibility below 2 K separately using Eq. (1) to determine the properties associated with the Kramers doublet ground state.

The magnetization isotherm $M(H)$ of NaYbGeO₄ measured up to 7 T at $T = 0.4$ K shows a saturation at around 1.5 T (Fig. 4). The saturation value M_{sat} is estimated by fitting the high-field region above 5 T with a straight line reflecting $\chi_0 H$ and extrapolating the line back to zero field. This yields $\chi_0 \simeq 5.58 \times 10^{-3}$ cm³/mol and $M_{\text{sat}} \simeq 1.92 \mu_{\text{B}}$, giving $g_{\text{eff}} \simeq 3.84$ from $\mu_{\text{sat}} = g_{\text{eff}} S_{\text{eff}} \mu_{\text{B}}$.

After subtracting χ_0 , the $\chi(T)$ data below 2 K are fitted by the CW law $\chi(T) = C/(T - \theta_{\text{CW}})$. The fitting yields $\theta_{\text{CW}}^{\text{LT}} \simeq (15 \pm 2)$ mK and $\mu_{\text{eff}}^{\text{LT}} \simeq 3.32 \mu_{\text{B}}$. The obtained effective moment is in good agreement with $\mu_{\text{eff}} = g_{\text{eff}} \sqrt{S_{\text{eff}}(S_{\text{eff}} + 1)} \mu_{\text{B}}$ for a pseudo-spin-1/2 ground state with g_{eff} value of ~ 3.84 , consistent with the value estimated from M_{sat} . The CW temperature depends on the sum of all exchange interactions and thus the balance of AF and FM contributions could result in a very small value of $\theta_{\text{CW}}^{\text{LT}}$. Analysis of ADR curves, detailed later, evidences AF order at 210 mK, which proves that the extremely small value of θ_{CW} must arise from the sum of AF and FM contributions. Note that a combination of nearest neighbor AF and next-nearest neighbor FM interactions on the square lattice excludes significant frustration.

D. Specific heat

Figure 5, upper panel, illustrates the magnetic specific heat for NaYbGeO₄ under various applied fields, suggesting its potential for mK-ADR. The zero-field specific heat data show no indication of magnetic long-range ordering above 0.4 K. A small anomaly at 2.23 K, cf. the difference between the data and the solid blue line, arises from 0.6% Yb₂O₃ impurities [53]. The finite-field data show Schottky anomalies, resulting

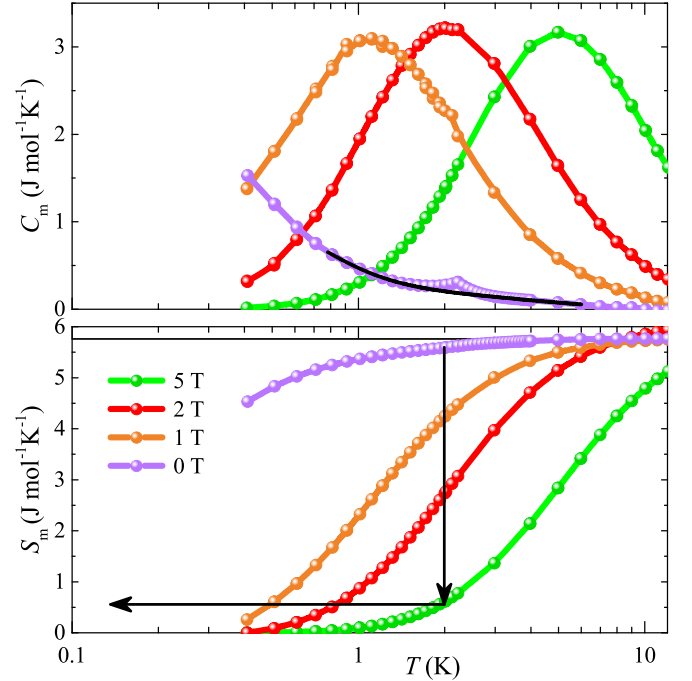


FIG. 5. Low-temperature magnetic specific heat (C_m) of NaYbGeO₄ at several external magnetic fields (upper panel). Phonon contribution was subtracted from the raw data using a polynomial fit [53]. The lower panel displays the magnetic entropy $S_m(T)$ obtained by integrating C_m/T over temperature. For the 0 and 1 T data the integration constant was adjusted such that a value of $R \ln 2$ (thin black line) is reached above 10 K. Two arrows show the ADR process.

from the splitting of the lowest Kramers doublet in field. This is confirmed by the fact that the entropy approaches $R \ln 2$, as displayed in the lower panel. As indicated by the two arrows, starting the ADR at ~ 2 K in a field of 5 T should reveal a minimal temperature well below 0.4 K in zero field.

E. Adiabatic demagnetization refrigeration (ADR)

The cooling performance of NaYbGeO₄ in our PPMS setup described above is shown in Fig. 6. Near 0.1 T the temperature trace passes a minimum at 135 mK. This sign change of the adiabatic magnetocaloric effect indicates the crossing of a magnetic phase boundary. Upon further reducing the field, the temperature increases toward 150 mK in zero field. The subsequent warming results from the finite heat input due to nonperfect adiabatic conditions. The time dependence of the temperature $T(t)$ displays a clear anomaly near 100 minutes. To analyze this trace, we utilize the equation

$$\dot{Q} = C_{\text{ADR}} \cdot \dot{T}, \quad (3)$$

where \dot{Q} represents a (constant) heat input per unit time, C_{ADR} denotes the (magnetic) heat capacity of the ADR pellet, and \dot{T} is the time derivative of temperature during warming. Taking $\dot{Q} = 0.58 \mu\text{W}$, a perfect agreement between the directly measured heat capacity and C_{ADR} is found down to 0.4 K (see Fig. 7). This heat input mainly arises from the residual He gas in our setup and here it was slightly lower than the $0.71 \mu\text{W}$ determined previously for KBaGd(BO₃)₂ [27]. For

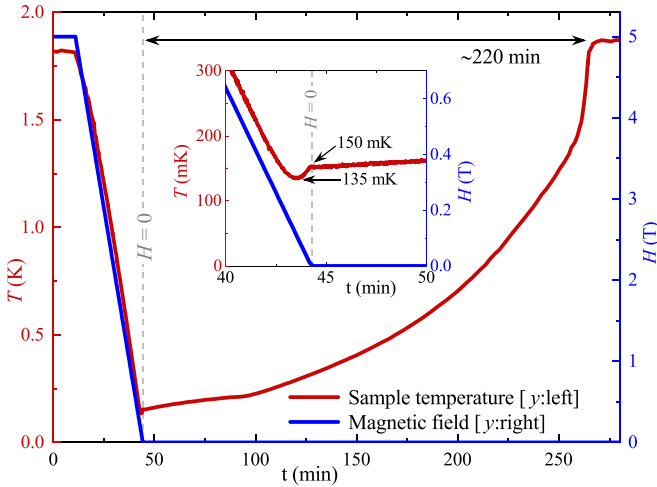


FIG. 6. Cooling of NaYbGeO₄ by ADR. The red and blue lines display the temporal evolution of temperature (left y axis) and magnetic field (right y axis). After precooling in a field of 5 T, the sample space was evacuated and subsequently the magnetic field was swept from 5 to 0 T at a rate of 0.15 T min⁻¹. The inset enlarges the regime close to zero field, where the temperature reaches a minimum of 135 mK at 0.1 T and then saturates at 150 mK in zero field. The warm-up time amounts to 220 min.

KBaGd(BO₃)₂ we also confirmed that the calculated heat capacity exactly equals the measured heat capacity signature of the AF transition. This provides us strong confidence that the sharp transition in C_{ADR} for NaYbGeO₄ distinctly signifies sharp AF order at $T_N \simeq 210$ mK. Note, that the sign change of the magnetocaloric effect in the field of 0.1 T at 130 mK is compatible with the suppression of the AF order in field.

The warm-up time of ~ 220 min (3 hr 40 min) is approximately 4–6 times longer than that of KYbP₂O₇ (~ 35 min),

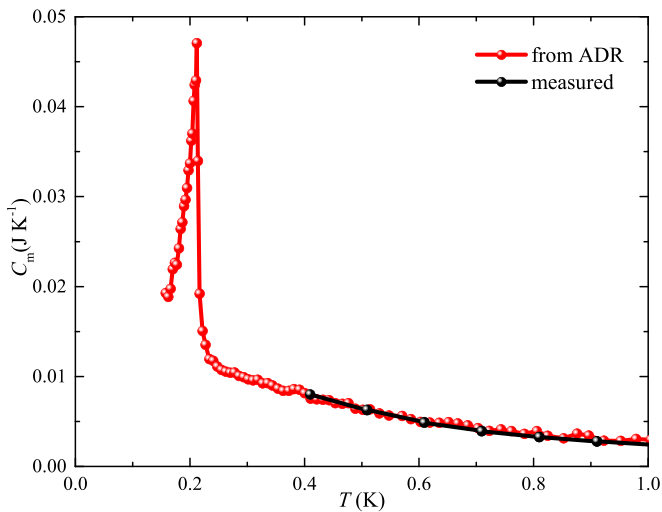


FIG. 7. Temperature dependence of the total (magnetic) heat capacity of the NaYbGeO₄-based ADR pellet determined from the warming curve shown in Fig. 6 by calculating $C_{\text{ADR}} = \dot{Q}/\dot{T}$ (red points). The constant heat input $\dot{Q} = 0.58 \mu\text{W}$ was used to obtain agreement with the measured heat capacity (black points) above 0.4 K.

NaYbP₂O₇ (~ 55 min), and KBaYb(BO₃)₂ (~ 40 min) [28] though much less than ~ 8 hr for KBaGd(BO₃)₂ [27]. This reflects that the entropy density 101 mJ/(K cm³) of NaYbGeO₄ is roughly 60% larger than that of the former materials but only half of that in KBaGd(BO₃)₂. The latter material reaches a similar (even slightly lower) ADR end temperature of 122 mK [27] compared to 135 mK in NaYbGeO₄ and is therefore even better suitable for applications in this target range.

IV. DISCUSSION

The sharp AF phase transition at 210 mK indicates that NaYbGeO₄ with a distorted square-lattice arrangement of Yb³⁺ moments is much weaker magnetically frustrated compared to the triangular-lattices KBaYb(BO₃)₂ [20] and NaYbP₂O₇ [28], as well as the distorted hyperhoneycomb-lattice KYbP₂O₇ [28], which all show no magnetic order above 35 mK ($T_N = 8$ mK in KBaYb(BO₃)₂ has been deduced by comparison with KBaGd(BO₃)₂ [27]). The fact that the CW temperature in NaYbGeO₄ is much smaller compared to the ordering temperature could be attributed to AF nearest neighbor and FM second neighbor exchange couplings. In this configuration, no frustration arises, as both first and second neighbor interactions are consistently satisfied simultaneously. If any frustration exists, it would likely arise from interactions perpendicular to the plane.

A comparison of the ADR performance of NaYbGeO₄ with that of other ADR materials, in particular geometrically frustrated Ytterbium borates and diphosphates is therefore interesting, as this may allow to draw conclusions on the importance of magnetic frustration in this respect. The crucial parameters that determine the efficiency of the various known ADR materials are compared in Table I. The full entropy of

TABLE I. Comparison of important parameters of different mK ADR materials: T_N is the magnetic ordering temperature, T_{min} is the minimum temperature attained, S_{GS} is the entropy of the ground-state multiplet, and R is the universal gas constant. The abbreviations are MAS = Mn(NH₄)₂(SO₄)₂ · 6H₂O (manganese ammonium sulfate), FAA = NH₄Fe(SO₄) · 12H₂O (ferric ammonium alum), CPA = KCr(SO₄) · 12H₂O (chromium potassium alum), and CMN = Mg₃Ce₂(NO₃)₁₂ · 24H₂O (cerium magnesium nitrate).

ADR materials				
Material	T_N (mK)	T_{min} (mK)	S_{GS}	$S_{\text{GS}}/\text{vol.}$ [mJ/(K cm ³)]
MAS [59]	170	<300	$R \ln 6$	70
FAA [59]	30	<100	$R \ln 6$	53
CPA [19]	10	<100	$R \ln 4$	42
CMN [60]	2	<40	$R \ln 2$	16
KBaGd(BO ₃) ₂ [27]	263	122	$R \ln 8$	192
YbPt ₂ Sn ₁₂ [34]	250	<200	$R \ln 2$	124
Yb ₃ Ga ₅ O ₁₂ [24]	54	<200	$R \ln 2$	124
NaYbGeO₄ (this study)	210	135	$R \ln 2$	101
KBaYb(BO ₃) ₂ [20]	8	<20	$R \ln 2$	64
NaYbP ₂ O ₇ [28]	<45	<45	$R \ln 2$	64
KYbP ₂ O ₇ [28]	<37	<37	$R \ln 2$	57

the ground state is described as $S_{GS} = R \ln(2J + 1)$, and the entropy density $S_{GS}/\text{vol.}$ is calculated by dividing S_{GS} by the unit cell volume. A large value of S_{GS} is always beneficial because the magnetic entropy changes (ΔS_m) of magnetic refrigerants act as the driving force of ADR. However, it is worth noting that for practical purposes it is not the molar entropy but the volumetric entropy density S_{GS} of the material that is relevant.

As can be seen from Table I, materials with high entropy density such as YbPt_2Sn or $\text{Yb}_3\text{Ga}_5\text{O}_{12}$ exhibit magnetic orderings at 250 mK and 54 mK, respectively, which limit their lowest attainable temperatures as the entropy drops below the ordering temperatures. The high spin hydrated paramagnetic salts, such as MAS and FAA, which have a larger magnetic entropy $R \ln 6$ are also affected by their much higher magnetic ordering temperatures. On the other hand, low transition temperature materials such as CPA and CMN have low magnetic moment density and hence low entropy density. A high entropy density usually contradicts a low magnetic ordering temperature.

In this context, it has been reported that the frustrated Yb-based quantum magnets AYbP_2O_7 , $\text{KBaYb}(\text{BO}_3)_2$, exhibit these two mutually exclusive criteria, such as a high volumetric entropy density combined with a very low ordering [20,28], allowing ADR to well below 50 mK. In $\text{KBaYb}(\text{BO}_3)_2$, both magnetic frustration and structural randomness contribute to suppress magnetic ordering. These oxides have been shown to be excellent anhydrous ADR refrigerants and under the same experimental conditions in PPMS, out of these three compounds, KYbP_2O_7 is attaining the lowest temperature of 37 mK [28]. Utilizing a better adiabatic setup in the ^3He - ^4He dilution refrigerator with feedback control of the bath temperature following the sample temperature, these materials can reach even lower temperatures well below 20 mK, which has been experimentally demonstrated for $\text{KBaYb}(\text{BO}_3)_2$ [20].

NaYbGeO_4 has a large magnetic ion density ($\sim 10.6 \text{ nm}^{-3}$) and volumetric entropy density [$\sim 101 \text{ mJ}/(\text{K cm}^3)$]. These values are higher than that of AYbP_2O_7 and $\text{KBaYb}(\text{BO}_3)_2$, and this is reflected in the significantly longer warm up time under comparable conditions. However, the end temperature of 135 mK is much higher compared to the case of the frustrated materials, indicating the importance of frustration for obtaining low end temperatures.

Compared to conventional mK ADR coolants based on hydrated paramagnetic salts, NaYbGeO_4 is stable at high

vacuum and can be heated up to 1000°C making it easy to handle and suitable for UHV applications. For our studies we prepared ADR pellets by mixing powder samples with silver powder in a 1 : 1 ratio for getting excellent thermal contact. The NaYbGeO_4 pellets, sintered at 1000°C , are mechanically stronger compared to the diphosphate pellets which we sintered only at 600°C [28]. Thus, mechanically stable NaYbGeO_4 ADR pills could also be made with much less or even without silver powder.

V. CONCLUSION

We synthesized and studied NaYbGeO_4 with effective spin-1/2 moments on a distorted square lattice with respect to its performance in millikelvin (mK) adiabatic demagnetization refrigeration (ADR). While the Curie-Weiss temperature of 15 mK would suggest the absence of significant magnetic interactions, the heat capacity, derived from the warming curve after ADR, shows a sharp AF phase transition at $T_N \simeq 210 \text{ mK}$. This suggests AF nearest neighbor and FM second neighbor exchange couplings and a nonfrustrated magnetic state. Compared to geometrically frustrated Ytterbium borates and diphosphates, the minimal ADR temperature of NaYbGeO_4 is significantly larger. This supports the conjecture that magnetic frustration is beneficial for mK-ADR.

Even though NaYbGeO_4 has a limitation in the lowest attainable temperature ($\sim 135 \text{ mK}$) due to the presence of sharp AF ordering, it has a comparably high entropy density and respectively shows a much longer warm-up time than Ytterbium borates and diphosphates. Chemical stability upon heating up to 1000°C , UHV compatibility, and the easy production of mechanically stable sintered pellets make this material an interesting alternative to hydrated paramagnetic salts for ADR applications above 200 mK.

ACKNOWLEDGMENTS

We thank Marvin Klinger and Yoshi Tokiwa for useful discussions. U.A. would like to acknowledge the Department of Science and Technology (DST), Government of India, for the financial support received through the DST Inspire Faculty Fellowship with reference number DST/INSPIRE/04/2019/001664. This work was supported by the German Research Foundation through Project 514162746 (GE 1640/11-1). D.D.S. thanks SERB, DST, and CSIR, Government of India, for financial support.

-
- [1] L. M. Kelley, Challenging ‘‘helium scarcity’’, *Chem. Eng.* **110**, 8 (2003).
- [2] A. H. Olafsdottir and H. U. Sverdrup, Assessing the past and future sustainability of global Helium resources, extraction, supply and use, using the integrated assessment model WORLD7, *Biophys. Econ. Sustainability* **5**, 6 (2020).
- [3] R. T. Kouzes and J. H. Ely, Status summary of ^3He and neutron detection alternatives for homeland security, US Department of Energy, Pacific Northwest National Laboratory, PNNL-19360 (2010), https://www.pnnl.gov/main/publications/external/technical_reports/PNNL-19360.pdf.
- [4] D. A. Shea and D. Morgan, *The Helium-3 Shortage: Supply, Demand, and Options for Congress* (Congressional Research Service, Washington DC, 2011).
- [5] A. Cho, Helium-3 shortage could put freeze on low-temperature research, *Science* **326**, 778 (2009).
- [6] P. Debye, Einige bemerkungen zur magnetisierung bei tiefer temperatur, *Ann. der Phys.* **386**, 1154 (1926).
- [7] W. Giauque and D. MacDougall, Attainment of temperatures below 1° absolute by demagnetization of $\text{Gd}_2(\text{SO}_4)_3 \cdot 8\text{H}_2\text{O}$, *Phys. Rev.* **43**, 768 (1933).

- [8] F. Pobell, *Matter and Methods at Low Temperatures*, 3rd ed. (Springer, Berlin, Heidelberg, New York, 2007).
- [9] A. Alahmer, M. Al-Amayreh, A. O. Mostafa, M. Al-Dabbas, and H. Rezk, Magnetic refrigeration design technologies: State of the art and general perspectives, *Energies* **14**, 4662 (2021).
- [10] A. E. Jahromi, P. J. Shirron, and M. J. DiPirro, *Subkelvin cooling systems for quantum computers*, in *Proceedings of the 2019 Cryogenic Engineering Conference and International Cryogenic Materials Conference (CEC/ICMC)*, GSFC-E-DAA-TN70637 (NASA NTRS, Hartford, CT, 2019).
- [11] P. J. Shirron, Applications of the magnetocaloric effect in single-stage, multi-stage and continuous adiabatic demagnetization refrigerators, *Cryogenics* **62**, 130 (2014).
- [12] P. Shirron, E. Canavan, M. DiPirro, J. Francis, M. Jackson, J. Tuttle, T. King, and M. Grabowski, Development of a cryogen-free continuous ADR for the constellation-X mission, *Cryogenics* **44**, 581 (2004).
- [13] P. J. Shirron, Cooling capabilities of adiabatic demagnetization refrigerators, *J. Low Temp. Phys.* **148**, 915 (2007).
- [14] N. Luchier, J. Duval, L. Duband, P. Camus, G. Donnier-Valentin, and M. Linder, 50 mK cooling solution with an ADR precooled by a sorption cooler, *Cryogenics* **50**, 591 (2010).
- [15] C. Hagmann and P. Richards, Adiabatic demagnetization refrigerators for small laboratory experiments and space astronomy, *Cryogenics* **35**, 303 (1995).
- [16] P. Weiss and A. Piccard, Le phénomène magnétocalorique, *J. Phys. Theor. Appl.* **7**, 103 (1917).
- [17] J. Bartlett, G. Hardy, I. Hepburn, C. Brockley-Blatt, P. Coker, E. Crofts, B. Winter, S. Milward, R. Stafford-Allen, M. Brownhill *et al.*, Improved performance of an engineering model cryogen free double adiabatic demagnetization refrigerator, *Cryogenics* **50**, 582 (2010).
- [18] Kiutra, See e.g. Cooling Technology: Solid-state cryogen-free cooling, <https://kiutra.com/technology/>.
- [19] J. Daniels and N. Kurti, The thermal and magnetic properties of chromium potassium alum below 0.1 K, *Proc. R. Soc. A* **221**, 243 (1954).
- [20] Y. Tokiwa, S. Bachus, K. Kavita, A. Jesche, A. A. Tsirlin, and P. Gegenwart, Frustrated magnet for adiabatic demagnetization cooling to millikelvin temperatures, *Commun. Mater.* **2**, 42 (2021).
- [21] P. Wikus, E. Canavan, S. T. Heine, K. Matsumoto, and T. Numazawa, Magnetocaloric materials and the optimization of cooling power density, *Cryogenics* **62**, 150 (2014).
- [22] M. E. Zhitomirsky, Enhanced magnetocaloric effect in frustrated magnets, *Phys. Rev. B* **67**, 104421 (2003).
- [23] Y. Hu and A. Du, Magnetization behavior and magnetic entropy change of frustrated Ising antiferromagnets on two- and three-dimensional lattices, *J. Phys.: Condens. Matter* **20**, 125225 (2008).
- [24] D. A. P. Brasiliano, J.-M. Duval, C. Marin, E. Bichaud, J.-P. Brison, M. Zhitomirsky, and N. Luchier, YbGG material for adiabatic demagnetization in the 100 mK–3 K range, *Cryogenics* **105**, 103002 (2020).
- [25] X.-Y. Liu, Y. Gao, H. Li, W. Jin, J. Xiang, H. Jin, Z. Chen, W. Li, and G. Su, Quantum spin liquid candidate as superior refrigerant in cascade demagnetization cooling, *Commun. Phys.* **5**, 1 (2022).
- [26] M. Kleinhans, K. Eibensteiner, J. C. Leiner, C. Resch, L. Worch, M. A. Wilde, J. Spallek, A. Regnat, and C. Pfleiderer, Magnetocaloric properties of $R_3Ga_5O_{12}$ ($R = Tb, Gd, Nd, Dy$), *Phys. Rev. Appl.* **19**, 014038 (2023).
- [27] A. Jesche, N. Winterhalter-Stocker, F. Hirschberger, A. Bellon, S. Bachus, Y. Tokiwa, A. A. Tsirlin, and P. Gegenwart, Adiabatic demagnetization cooling well below the magnetic ordering temperature in the triangular antiferromagnet $KBaGd(BO_3)_2$, *Phys. Rev. B* **107**, 104402 (2023).
- [28] U. Arjun, K. M. Ranjith, A. Jesche, F. Hirschberger, D. D. Sarma, and P. Gegenwart, Efficient adiabatic demagnetization refrigeration to below 50 mK with ultrahigh-vacuum-compatible ytterbium diphosphates $AYbP_2O_7$ ($A = Na, K$), *Phys. Rev. Appl.* **20**, 014013 (2023).
- [29] B. Wolf, Y. Tsui, D. Jaiswal-Nagar, U. Tutsch, A. Honecker, K. Remović-Langer, G. Hofmann, A. Prokofiev, W. Assmus, G. Donath, and M. Lang, Magnetocaloric effect and magnetic cooling near a field-induced quantum-critical point, *Proc. Natl. Acad. Sci. USA* **108**, 6862 (2011).
- [30] B. Wolf, U. Tutsch, S. Dörschug, C. Krellner, F. Ritter, W. Assmus, and M. Lang, Magnetic cooling close to a quantum phase transition—the case of $Er_2Ti_2O_7$, *J. Appl. Phys.* **120**, 142112 (2016).
- [31] M. Evangelisti, O. Roubeau, E. Palacios, A. Camón, T. N. Hooper, E. K. Brechin, and J. J. Alonso, Cryogenic magnetocaloric effect in a ferromagnetic molecular dimer, *Angew. Chem. Int. Ed.* **50**, 6606 (2011).
- [32] A. Baniodeh, N. Magnani, Y. Lan, G. Buth, C. E. Anson, J. Richter, M. Affronte, J. Schnack, and A. K. Powell, High spin cycles: Topping the spin record for a single molecule verging on quantum criticality, *npj Quantum Mater.* **3**, 10 (2018).
- [33] Y. Tokiwa, B. Piening, H. S. Jeevan, S. L. Bud'ko, P. C. Canfield, and P. Gegenwart, Super-heavy electron material as metallic refrigerant for adiabatic demagnetization cooling, *Sci. Adv.* **2**, e1600835 (2016).
- [34] D. Jang, T. Gruner, A. Steppke, K. Mitsumoto, C. Geibel, and M. Brando, Large magnetocaloric effect and adiabatic demagnetization refrigeration with $YbPt_2Sn$, *Nat. Commun.* **6**, 8680 (2015).
- [35] I. Kimchi, A. Nahum, and T. Senthil, Valence bonds in random quantum magnets: Theory and application to $YbMgGaO_4$, *Phys. Rev. X* **8**, 031028 (2018).
- [36] Y. Li, D. Adroja, P. K. Biswas, P. J. Baker, Q. Zhang, J. Liu, A. A. Tsirlin, P. Gegenwart, Q. Zhang *et al.*, Muon spin relaxation evidence for the $u(1)$ quantum spin-liquid ground state in the triangular antiferromagnet $YbMgGaO_4$, *Phys. Rev. Lett.* **117**, 097201 (2016).
- [37] J. A. Paddison, M. Daum, Z. Dun, G. Ehlers, Y. Liu, M. B. Stone, H. Zhou, M. Mourigal *et al.*, Continuous excitations of the triangular-lattice quantum spin liquid $YbMgGaO_4$, *Nat. Phys.* **13**, 117 (2017).
- [38] M. M. Bordelon, E. Kenney, C. Liu, T. Hogan, L. Posthuma, M. Kavand, Y. Lyu, M. Sherwin, N. P. Butch, C. Brown *et al.*, Field-tunable quantum disordered ground state in the triangular-lattice antiferromagnet $NaYbO_2$, *Nat. Phys.* **15**, 1058 (2019).
- [39] K. M. Ranjith, S. Luther, T. Reimann, B. Schmidt, P. Schlender, J. Sichelschmidt, H. Yasuoka, A. M. Strydom, Y. Skourski, J. Wosnitzer, H. Kühne, T. Doert, and M. Baenitz, Anisotropic field-induced ordering in the triangular-lattice quantum spin liquid $NaYbSe_2$, *Phys. Rev. B* **100**, 224417 (2019).

- [40] M. Baenitz, P. Schlender, J. Sichelschmidt, Y. A. Onykieenko, Z. Zangeneh, K. M. Ranjith, R. Sarkar, L. Hozoi, H. C. Walker, J.-C. Orain, H. Yasuoka, J. van den Brink, H. H. Klauss, D. S. Inosov, and T. Doert, NaYbS₂: A planar spin-1/2 triangular-lattice magnet and putative spin liquid, *Phys. Rev. B* **98**, 220409(R) (2018).
- [41] B. Schmidt, J. Sichelschmidt, K. M. Ranjith, T. Doert, and M. Baenitz, Yb delafossites: Unique exchange frustration of $4f$ spin- $\frac{1}{2}$ moments on a perfect triangular lattice, *Phys. Rev. B* **103**, 214445 (2021).
- [42] K. M. Ranjith, D. Dmytriieva, S. Khim, J. Sichelschmidt, S. Luther, D. Ehlers, H. Yasuoka, J. Wosnitza, A. A. Tsirlin, H. Kühne, and M. Baenitz, Field-induced instability of the quantum spin liquid ground state in the $J_{\text{eff}} = \frac{1}{2}$ triangular-lattice compound NaYbO₂, *Phys. Rev. B* **99**, 180401(R) (2019).
- [43] Z. Zhu, P. A. Maksimov, S. R. White, and A. L. Chernyshev, Disorder-induced mimicry of a spin liquid in YbMgGaO₄, *Phys. Rev. Lett.* **119**, 157201 (2017).
- [44] E. Dagotto and A. Moreo, Phase diagram of the frustrated spin-1/2 heisenberg antiferromagnet in 2 dimensions, *Phys. Rev. Lett.* **63**, 2148 (1989).
- [45] R. Darradi, O. Derzhko, R. Zinke, J. Schulenburg, S. E. Krüger, and J. Richter, Ground state phases of the spin-1/2 $J_1 - J_2$ heisenberg antiferromagnet on the square lattice: A high-order coupled cluster treatment, *Phys. Rev. B* **78**, 214415 (2008).
- [46] H.-C. Jiang, H. Yao, and L. Balents, Spin liquid ground state of the spin- $\frac{1}{2}$ square $J_1 - J_2$ heisenberg model, *Phys. Rev. B* **86**, 024424 (2012).
- [47] L. Wang and A. W. Sandvik, Critical level crossings and gapless spin liquid in the square-lattice spin-1/2 $J_1 - J_2$ heisenberg antiferromagnet, *Phys. Rev. Lett.* **121**, 107202 (2018).
- [48] N. Shannon, T. Momoi, and P. Sindzingre, Nematic order in square lattice frustrated ferromagnets, *Phys. Rev. Lett.* **96**, 027213 (2006).
- [49] N. Shannon, B. Schmidt, K. Penc, and P. Thalmeier, Finite temperature properties and frustrated ferromagnetism in a square lattice heisenberg model, *Eur. Phys. J. B* **38**, 599 (2004).
- [50] O. Mustonen, S. Vasala, K. P. Schmidt, E. Sadrollahi, H. C. Walker, I. Terasaki, F. J. Litterst, E. Baggio-Saitovitch, and M. Karppinen, Tuning the $s = 1/2$ square-lattice antiferromagnet Sr₂Cu(Te_{1-x}W_x)O₆ from Néel order to quantum disorder to columnar order, *Phys. Rev. B* **98**, 064411 (2018).
- [51] J. Rodríguez-Carvajal, Recent advances in magnetic structure determination by neutron powder diffraction, *Phys. B: Condens. Matter* **192**, 55 (1993).
- [52] M. Emirdag-Eanes, M. Krawiec, and J. W. Kolis, Hydrothermal synthesis and structural characterization of NaLnGeO₄ (Ln = Ho, Er, Tb, Tm, Yb, Lu) family of lanthanide germanates, *J. Chem. Crystallogr.* **31**, 281 (2001).
- [53] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevB.108.224415> for additional information on the specific heat data analysis.
- [54] S. Guchhait, U. Arjun, P. K. Anjana, M. Sahoo, A. Thirumurugan, A. Medhi, Y. Skourski, B. Koo, J. Sichelschmidt, B. Schmidt, M. Baenitz, and R. Nath, Case study of bilayered spin-1/2 square lattice compound VO(HCOO)₂ · (H₂O), *Phys. Rev. Mater.* **3**, 104409 (2019).
- [55] R. Nath, M. Padmanabhan, S. Baby, A. Thirumurugan, D. Ehlers, M. Hemmida, H.-A. Krug von Nidda, and A. A. Tsirlin, Quasi-two-dimensional $S = 1/2$ magnetism of Cu[C₆H₂(COO)₄][C₂H₅NH₃]₂, *Phys. Rev. B* **91**, 054409 (2015).
- [56] T. Matsumoto, Y. Miyazaki, A. S. Albrecht, C. P. Landee, M. M. Turnbull, and M. Sorai, Heat capacities of the $S = 1/2$ two-dimensional Heisenberg antiferromagnet bis(2-amino-5-chloropyridinium) tetrabromocuprate(ii) [(5CAP)₂CuBr₄] and its diamagnetic analogue [(5CAP)₂ZnBr₄], *J. Phys. Chem. B* **104**, 9993 (2000).
- [57] T. Lancaster, S. J. Blundell, M. L. Brooks, P. J. Baker, F. L. Pratt, J. L. Manson, M. M. Conner, F. Xiao, C. P. Landee, F. A. Chaves, S. Soriano, M. A. Novak, T. P. Papageorgiou, A. D. Bianchi, T. Herrmannsdörfer, J. Wosnitza, and J. A. Schlueter, Magnetic order in the $s = 1/2$ two-dimensional molecular antiferromagnet copper pyrazine perchlorate Cu(Pz)₂(ClO₄)₂, *Phys. Rev. B* **75**, 094421 (2007).
- [58] S. Mugiraneza and A. M. Hallas, Tutorial: a beginner's guide to interpreting magnetic susceptibility data with the Curie-Weiss law, *Commun. Phys.* **5**, 95 (2022).
- [59] O. E. Vilches and J. C. Wheatley, Measurements of the specific heats of three magnetic salts at low temperatures, *Phys. Rev.* **148**, 509 (1966).
- [60] R. A. Fisher, E. W. Hornung, G. E. Brodale, and W. F. Giauque, Magnetothermodynamics of Ce₂Mg₃(NO₃)₁₂ · 24H₂O. II. The evaluation of absolute temperature and other thermodynamic properties of CMN to 0.6 mK, *J. Chem. Phys.* **58**, 5584 (1973).