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Tensile and compressive strain tuning of a Kondo lattice

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We present electrical resistivity measurements on the prototypical heavy-fermion metal YbRh₂Si₂ (YRS) under *a*-axis tensile and compressive strain and focus on the evolution of the resistivity maximum near 136 K that arises from the interplay of the Kondo effect and the crystal electric field (CEF) splitting. While compressive strain reduces T_{\max} , similar as previously reported for hydrostatic pressure, T_{\max} is enhanced up to 145 K for 0.13% tensile strain. Model calculations for the strain effect on CEF splitting in YRS reveal a negligible shift of the levels. Instead, the enhancement of the resistivity maximum indicates a 20% increase of the Kondo temperature. This opens the perspective to access the hidden zero-field quantum critical point in pure YRS.

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I. INTRODUCTION

Heavy-fermion metals with partially filled $4f$ or $5f$ shells (typically in Ce, Pr, Yb, or U compounds) are prototype materials for the study of quantum criticality [1,2]. The Doniach diagram [3], shown in Fig. 1, illustrates the competition of the Kondo effect, favoring a paramagnetic heavy-fermion state and the indirect exchange [Ruderman-Kittel-Kasuya-Yosida (RKKY)] coupling, mediating long-range magnetic order. Respective characteristic energies T_K and T_{RKKY} depend exponentially and quadratically on the antiferromagnetic (AFM) exchange coupling J between the f moments and conduction electrons, respectively. The variation of $T_N(J)$ reflects this competition, leading to a quantum critical point (QCP) [4] at a critical J_c , separating the AFM and paramagnetic (PM) ground states. Experimentally, J can be directly modified by pressure or chemical substitution. While pressure suppresses AFM order for Ce systems it acts oppositely for Yb-based HF metals, because it favors the smaller magnetic Yb³⁺ configuration over the mixed valent and nonmagnetic Yb²⁺ cases. Motivated by the invention and commercialization of *in situ* piezoelectric strain tuning tools for low-temperature experiments [5–7], we explore in this paper the possibility to *enhance* the Kondo coupling of AFM Yb-based HF metals by tensile strain.

We focus our attention on the prototype Yb-based HF metal YbRh₂Si₂ (YRS) which shows a weak AFM ground state below $T_N = 70$ mK, providing a platform to study quantum criticality [8]. A small critical magnetic field of 0.06 T (0.66 T) perpendicular (parallel) to the tetragonal c axis is sufficient to suppress the AFM order and induce quantum criticality [9]. Measurements of the Hall effect detected an additional crossover scale at $T^*(B)$ beyond the critical field that has been interpreted as the finite-temperature signature

of a jump of the Fermi surface at the QCP due to a Kondo breakdown [10]. However, this crossover signals a polarization of ferromagnetic fluctuations [11,12], distinct from the AFM QCP at zero field [13]. Since T_N at $B = 0$ is enhanced under hydrostatic pressure, an extrapolated *negative* critical pressure $P_c \approx -0.3$ GPa [14], corresponding to a relative volume expansion of $+1.6 \times 10^{-4}$, is required to access the zero-field AFM QCP. The linear thermal expansion coefficient, which is proportional to the uniaxial pressure derivative of the entropy, is negative both along and perpendicular to the tetragonal c axis in YRS [15]. The negative Grüneisen ratio of thermal expansion to specific heat indeed implies that the characteristic temperature (here, T_K) rises with volume expansion [16]. Since the in-plane thermal expansion exceeds that along the [001] direction by $\sim 80\%$ at low temperature [15] we expect a significant increase of T_K by tensile in-plane strain. YRS single crystals typically grow as thin plates perpendicular to the c axis, thus the material seems well suitable for exploration.

Here, we report on electrical resistance measurements under tensile and compressive piezostain tuning, revealing a significant variation of the Kondo maximum temperature, that can be related to a strain dependence of T_K . Tensile strain significantly enhances T_K , paving the way to reach a zero-field QCP.

II. EXPERIMENT

Single crystals of YRS were grown using the In-flux technique [8,17]. Yb ingots (Ames, 99.99%), Rh powder (Heraeus, 99.95%), Si pieces (Alfa Aesar, 99.99%), and In shots (Alfa Aesar, 99.9999%) were put together in a cylindrical Al₂O₃ crucible with 96% mol In and 4% mol YbRh₂Si₂. The Yb was handled and stored in an argon-filled glovebox ($O_2 < 1$ ppm, $H_2O < 1$ ppm). The Al₂O₃ crucible was enclosed inside a Ta tube and sealed using arc welding under 0.5 bars Ar [18]. The growth was carried out in an Ar-filled, vertical tube furnace with the Ta container wrapped in Zr foil in order to prevent oxidation. The elements were heated up to

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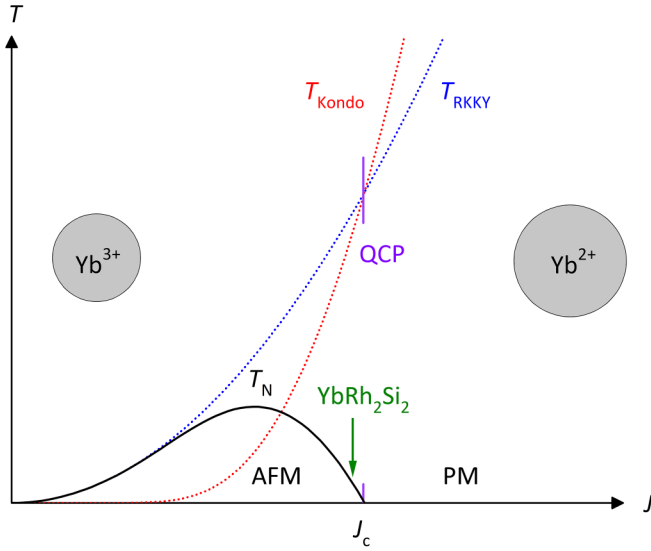


FIG. 1. Doniach diagram [3] illustrating T_{Kondo} , T_{RKKY} , and T_N as a function of the exchange coupling J between f and conduction electrons in heavy-fermion metals. The dashed line at J_c indicates the quantum critical point at $T_N = 0$, separating the antiferromagnetic (AFM) and paramagnetic (PM) ground states. The arrow marks qualitatively the location of YbRh_2Si_2 . The gray spheres illustrate the atomic volume of tri- and divalent Yb.

1480 °C followed by slow cooling to $T = 950$ °C over 5 days. After the growth, the platelike single crystals were extracted by dissolving the In-rich flux in a diluted hydrochloric acid solution. The orientation was determined using Laue back reflection. The plates were sliced to bars along the [100] (a -axis) direction with a length between 1.7 and 2 mm and width in between 100 and 250 μm , using a DIDRAS diamond wire saw cutter and polished to a thickness 40–80 μm . Electrical contacts with Au wires of thickness 25 μm were made using two-component H20 silver epoxy from EPOTEK, cured at 100 °C. The four-probe electrical resistance measurements as a function of temperature and strain were performed in a physical property measurement system (PPMS, Quantum Design) with the strain cell (FC100 from Razorbill) attached to the modified P450 probe (Quantum Design). Thermal anchoring of the cell is achieved by silver foil and wires. As depicted in Fig. 2, the rectangular bar-shaped crystals were mounted onto the clamps of the stress cell using Stycast 2850FT two-component epoxy such that strain on the crystal was along the [100] direction. The horizontal force F applied to the crystal for a given applied voltage on the piezostacks was determined by measuring the change in capacitance of the inbuilt precalibrated capacitive force sensor on the FC100 cell [6]. The uniaxial pressure follows from $P = F/A$ with the sample cross section A . Within the elastic regime and assuming a constant Young's modulus $Y = 189$ GPa for YRS [19] the strain is given by $\epsilon = P/Y$. To minimize strain inhomogeneity between the voltage contacts, it is crucial to mount samples with high length-to-width aspect ratios and place the contacts sufficiently far from the edges, since the strain inhomogeneity decays exponentially towards the center. A comparison with model calculations [5] indicates an inhomogeneity below 5%. The piezovoltage was applied after stabilizing 160 K. Then the

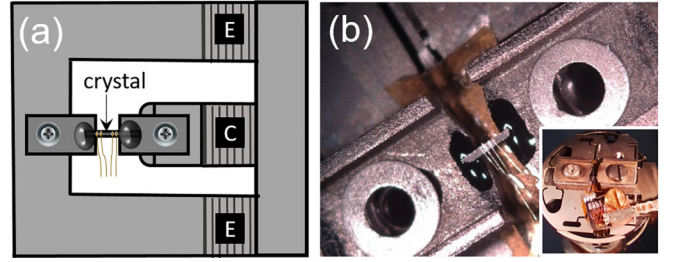


FIG. 2. (a) Schematic depiction of the strain apparatus. **E** represent the extension stacks and **C** the compression stacks. (b) shows a snapshot taken in the process of sample mounting. Depicting a crystal mounted with Stycast on the sample platform of the stress cell for resistance measurement. The inset displays the stress cell after sample mounting, ready for the electrical transport measurements.

sample resistance was detected upon cooling down to 2 K and subsequent warming back to 160 K with a rate of 1 K/min. No thermal hysteresis within the error bar of ± 1 K was detected. The design of the cell compensates the thermal contraction of the setup and ensures a constant force. Three crystals were studied under tensile and one more under compressive strain.

III. RESULTS AND DISCUSSION

Figure 3 shows the temperature dependence of the electrical resistance of four different single crystals at ambient strain down to 1.8 K. After passing a characteristic maximum around $T_{\text{max}} = 136$ K the resistance decreases upon cooling and reaches $\rho_{300\text{K}}/\rho_{1.8\text{K}}$ values in between 8 and 14 similar as reported earlier [9]. The resistivity maximum is characteristic for heavy-fermion metals and arises from incoherent Kondo scattering on the ground state and the excited crystal electric field (CEF) levels (cf. the inset of Fig. 3) of the f electrons [20]. Note that due to the CEF effect the resistivity maximum

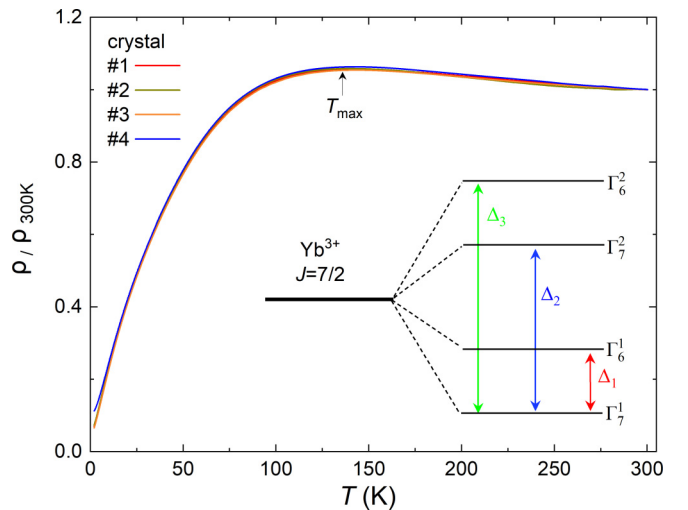


FIG. 3. Normalized electrical resistance of four different single crystals of YbRh_2Si_2 at ambient conditions (no strain). The arrow indicates the position of the maximum temperature T_{max} . The inset depicts schematically the splitting of the $\text{Yb}^{3+} J = 7/2$ multiplet in the tetragonal crystal electric field into four Kramers doublets [22].

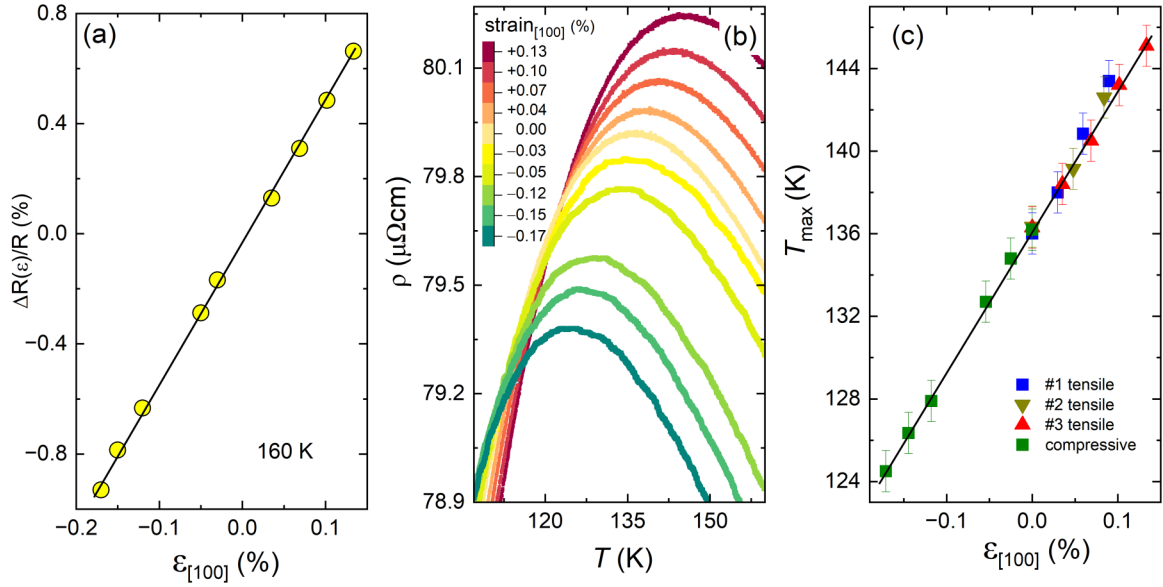


FIG. 4. (a) Linear evolution of the elastoresistance of YbRh_2Si_2 at 160 K as a function of tensile (crystal 3) and compressive strain along the crystallographic [100] direction. (b) Effect of positive (tensile) and negative (compressive) strain (along [100]) on the resistance maximum of YbRh_2Si_2 crystal No. 3. (c) Shift of T_{max} with strain (along [100]) for different YbRh_2Si_2 crystals. Error bars indicate a thermometry accuracy of 1 K.

can appear far above the Kondo temperature of the ground state doublet [21]. Inelastic neutron-scattering experiments on YRS powder have found CEF excitations of the Yb^{3+} ions at approximately 17, 25, and 43 meV [22]. Since the highest level corresponds to temperatures well above room temperature, we consider the Kondo effect on the ground state and the first two excited doublets (with excitations energies Δ_1 and Δ_2 in degrees Kelvin, respectively), yielding, according to Hanzawa *et al.* [23], a “high-Kondo temperature”

$$T_K^h = \sqrt[3]{T_K \Delta_1 \Delta_2}, \quad (3.1)$$

where T_K denotes the Kondo temperature for the ground state doublet, which is around 27 K for YRS [24]. Using this value and splittings of $\Delta_1 = 197$ K and $\Delta_2 = 290$ K yields $T_K^h = 112$ K, which is about 20% lower than the maximum temperature T_{max} of the electrical resistance at ambient strain. However, it should be noted that the exact position of T_{max} is also influenced by the unknown phonon background to $\rho(T)$ and a previous attempt to subtract such a background by the analysis of the $\rho(T)$ data of nonmagnetic LuRh_2Si_2 indeed revealed a lower value of T_{max} , close to the pronounced negative peak in the thermoelectric power at 80–100 K in $\text{Lu}_{1-x}\text{Yb}_x\text{Rh}_2\text{Si}_2$ [25]. Since we follow the *relative* change of energy scales in YRS with strain, we prefer to directly analyze our raw electrical resistance data without any background subtraction and will later use a scaling factor to adjust the strain dependence of the Kondo temperature at zero strain to $T_K = 27$ K. Note that the phonon contribution to the electrical resistance scales with the Debye temperature, whose change under 10^{-3} strain is tiny. Additionally, tetragonal YbRh_2Si_2 is far from any structural phase transitions. Thus, strain-induced changes of $\rho(T)$ result mostly from the $4f$ contribution and not primarily from phonons.

Next, we discuss the change of the electrical resistance of YbRh_2Si_2 with tensile and compressive strain along the [100] direction. As shown in Fig. 4(a) the electrical resistance of YbRh_2Si_2 at 160 K shows a weakly linear dependence on uniaxial tensile and compressive strain, proving a full transmission of the applied strain to the crystal. It is worth mentioning that crystals are prone to crack formation under tensile strain, which currently prevents us from reaching tensile strain values exceeding 0.13%. The temperature dependence of the resistance between 105 and 160 K at these applied strains, in addition to the zero-strain curve, is displayed in Fig. 4(b). T_{max} shows a pronounced shift towards higher values with increasing tensile strain, from 136 to 145 K for $\epsilon = 0.13\%$. A very similar shift is confirmed on two other crystals, as depicted in Fig. 4(c). Note that the linear strain dependence of T_{max} only holds as long as the crystals are not yet cracked. Under compressive strain, T_{max} shifts towards a low temperature from 136 to 124.5 K for $\epsilon = 0.17\%$ and follows the same linear strain dependence in continuation with tensile strain as depicted in Fig. 4(c).

From the above general consideration of Yb-based Kondo metals, such a rapid increase of T_{max} towards a high temperature under tensile strain suggests an expected enhancement of the Kondo interaction. It is also qualitatively consistent with the suppression of T_{max} and T_K in YbRh_2Si_2 with hydrostatic pressure [24,26], as discussed below.

Although the observed tensile and compressive strain dependences suggest that the shift of T_{max} reflects a change of the Kondo temperature, we also need to consider the strain effect on the CEF splitting, since as discussed above, the latter influences the position of the resistance maximum. To estimate the change of the CEF splitting with strain, the elastic deformation of the crystal lattice is considered, following Refs. [27,28]. The strain along the tetragonal [100] direction leads to an orthorhombic distortion. Hence, we evaluate the

following Hamiltonian:

$$H_{\text{total}} = H_{\text{CEF}}^{\text{tetra}} + H_{\text{ME}}^{\text{ortho}}. \quad (3.2)$$

Here,

$$H_{\text{CEF}}^{\text{tetra}} = \alpha(B_2^0 O_2^0) + \beta(B_4^0 O_4^0 + B_4^4 O_4^4) + \gamma(B_6^0 O_6^0 + B_6^4 O_6^4), \quad (3.3)$$

where O_n^m are Stevens operator equivalents, B_n^m are the CEF parameters taken from Kutuzov *et al.* [29], while Stevens multiplicative factors for Yb ions are $\alpha = 2/63$, $\beta = 2/1155$, and $\gamma = 4/27027$. Assuming the magnetoelastic effect $H_{\text{ME}}^{\text{ortho}}$ is small, we only consider first-order perturbation (i.e., to the first order of strain-CEF coupling) as a starting point. We obtain the ground state doublet $|\Psi_{\pm}\rangle$, and the first excited doublet $|\Psi'_{\pm}\rangle$ by diagonalizing Eq. (3.3) which couples $|J, J_z\rangle$ as follows:

$$|\Psi_{\pm}\rangle = a|7/2, \pm 5/2\rangle + b|7/2, \mp 3/2\rangle, \quad (3.4)$$

$$|\Psi'_{\pm}\rangle = a'|7/2, \pm 7/2\rangle + b'|7/2, \mp 1/2\rangle. \quad (3.5)$$

Normalization requires $a^2 + b^2 = 1$ and $a'^2 + b'^2 = 1$. Orthorhombic distortion includes $O_2^2, O_4^2, O_6^2, O_6^6$ in addition to the five other terms that are also included in $H_{\text{CEF}}^{\text{tetra}}$. Since the operator O_n^2 (O_n^6) only couples to the state of $\Delta_{J_z} = \pm 2$ (± 6), the matrix elements $\langle \Psi | O_n^2 (O_n^6) | \Psi \rangle$ vanish exactly. In other words, a small orthorhombic distortion does not add more terms to the original CEF environment $H_{\text{CEF}}^{\text{tetra}}$ because of the incompatible symmetry between the CEF doublets and O_n^2, O_n^6 terms, as mentioned above. Therefore, the CEF wave functions retain their structure. Incidentally, the effects from O_n^2 and O_n^6 are no longer negligible for second-order perturbation because the off-diagonal matrix elements between the CEF ground state and the first excited state $\langle \Psi | O_n^2 (O_n^6) | \Psi' \rangle$ have finite values. For first-order perturbation we could write Eq. (3.2) as follows,

$$H_{\text{total}} = H_{\text{CEF}}^{\text{tetra}} + g_{xx}\epsilon_{xx}(O_2^0 + \Delta g_{04}O_4^0 + \Delta g_{44}O_4^4 + \Delta g_{06}O_6^0 + \Delta g_{46}O_6^4), \quad (3.6)$$

where g_{xx} is the magnetoelastic coupling constant, ϵ_{xx} is the applied strain along the [100] direction, and Δg_{mn} is the weight on each Stevens operator equivalents. We further simplify the equation by dropping the higher-order terms O_4^m and O_6^m , since they should contribute much less than the quadrupolar term. For example, in the case of the rare-earth intermetallic compound TmSb, the magnetoelastic coupling with O_4^m is only 16 mK, which is three orders of magnitude smaller than the coupling with the quadrupolar term which is 20 K [30].

Diagonalization of the simplified Hamiltonian

$$H_{\text{CEF}}^{\text{tetra}} + g_{xx}\epsilon_{xx}O_2^0 \quad (3.7)$$

allows then to calculate the approximate strain effect on the energy shifts between the protected Kramers doublets. Upon first-order perturbation, the energy for the ground state doublet is

$$E = E_0 + g_{xx}\epsilon_{xx}\langle \Psi | O_2^0 | \Psi \rangle, \quad (3.8)$$

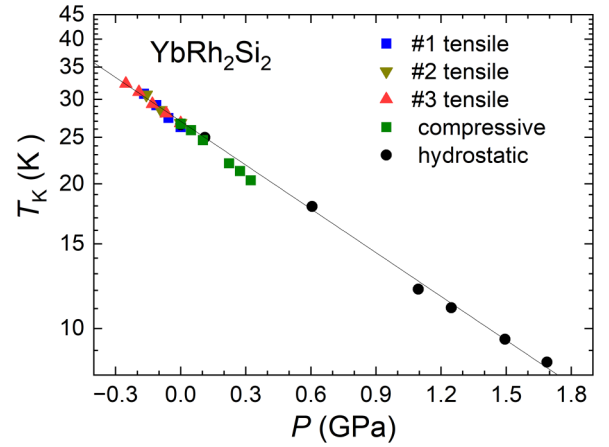


FIG. 5. Hydrostatic pressure dependence of Kondo temperature T_K of YbRh_2Si_2 from Tokiwa *et al.* [24] (solid black circles) compared to T_K under tensile and compressive strain along the [100] direction, as calculated using Eq. (3.1) with a constant adjustment factor to match with $T_K = 27$ K at $P = 0$.

and for the first excited doublet

$$E' = E'_0 + g_{xx}\epsilon_{xx}\langle \Psi' | O_2^0 | \Psi' \rangle. \quad (3.9)$$

We define the energy gap between the ground state and the first excited state as $\Delta_1 = E'_0 - E_0$ where E_0 (E'_0) is the unperturbed energy of the ground state doublet (first excited doublet), and the energy gap after introducing the first-order perturbation as $\Delta_1^{(1)} = E' - E$. The energy gap between the first and the second excited doublet with (without) perturbation $\Delta_2^{(1)}$ (Δ_2) can be defined in a similar manner.

Magnetoelastic coupling constants can be determined by measurements of the ultrasound velocity. For YRS such data are missing, likely because the available thin crystal plates are not suitable for such experiments. As a reference, we discuss values of other Yb-based Kondo lattices. For YbPtBi , it is estimated to be around 10 K [27], while for $\text{YbCo}_2\text{Zn}_{20}$ and $\text{YbRh}_2\text{Zn}_{20}$, the fitting of ultrasound data yielded 1 K [31] and 131 K [32] for the largest modes, respectively. Obviously, the magnetoelastic coupling can vary substantially even for materials with the same crystal structure and similar magnetic ions. We thus used a value of 131 K to minimize the risk of underestimating magnetoelastic coupling to the best of our ability. The result of the model calculation indicates that both $\Delta_1^{(1)}$ and $\Delta_2^{(1)}$ are only shifted around 1% with respect to the unperturbed Δ_1 and Δ_2 , respectively, for strain ϵ_{xx} up to $\pm 0.2\%$. The small shift of the CEF energy justifies our approximation based on first-order perturbation. For YRS, such a minute variation of the excitation energies cannot explain the significant shift of the maximum temperature of the electrical resistance, which thus can indeed be related to the strain-induced change of the Kondo temperature.

Using Eq. (3.1), T_K can be calculated from the experimentally determined values of T_{max} and the uniaxial pressure dependence of Δ_1 and Δ_2 from the above calculation. Calculated values of T_K with a constant prefactor adjusted to match 27 K at ambient conditions [24] is shown in Fig. 5. Tensile

strain, corresponding to negative hydrostatic pressure, clearly enhances the Kondo temperature T_K up to 32 K. According to the previous study of T_N under hydrostatic pressure, the extrapolated AFM QCP in YRS is located around -0.3 GPa [14]. Furthermore, the extrapolation of the hydrostatic pressure dependence of T_K [24] to -0.3 GPa yields a T_K of 33 K, which is very close to the maximal value we have obtained under tensile strain. This suggests that the nature of the AFM QCP in pure YRS *at zero field* can be studied in future tensile strain experiments. It requires to overcome demanding challenges of reaching millikelvin temperatures due to the large mass and poor thermal conductance of the piezostain apparatus. A study of the temperature dependence of the electrical resistance, yielding the phase boundary $T_N(\epsilon)$, the crossover to Landau-Fermi-liquid behavior $T_{FL}(\epsilon)$, as well as the strain dependence of the quasiparticle scattering cross section is very interesting, since distinct behavior compared to the case of field tuning, which polarizes the AFM ordered moments could be expected, as discussed in the Introduction. The effect of *compressive* uniaxial as well as biaxial strain, enhancing T_N , has been successfully determined earlier by electrical resistance measurements on thin

microstructured YRS meanders, glued with epoxy to a silver holder [33].

In summary, we have successfully realized tensile piezostain tuning of the prototypical heavy-fermion system YbRh_2Si_2 . The characteristic maximum in the temperature dependence of the electrical resistance has been significantly enhanced for 0.13% tensile strain. Our CEF calculations reveal that the change of T_{\max} is primarily caused by the change of the Kondo temperature. The significant enhancement of T_K with tensile strain allows to tune clean undoped YRS across its zero-field QCP in future millikelvin experiments. While compressive piezostain has recently been used for enhancing the Kondo interaction in a Ce-based heavy-fermion metal [34] our work provides the path to explore hidden regimes in heavy fermions by tensile strain.

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