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# Quantifying the Precision of Single-Molecule Torque and Twist Measurements Using Allan Variance

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**ABSTRACT** Single-molecule manipulation techniques have provided unprecedented insights into the structure, function, interactions, and mechanical properties of biological macromolecules. Recently, the single-molecule toolbox has been expanded by techniques that enable measurements of rotation and torque, such as the optical torque wrench (OTW) and several different implementations of magnetic (torque) tweezers. Although systematic analyses of the position and force precision of single-molecule techniques have attracted considerable attention, their angle and torque precision have been treated in much less detail. Here, we propose Allan deviation as a tool to systematically quantitate angle and torque precision in single-molecule measurements. We apply the Allan variance method to experimental data from our implementations of (electro)magnetic torque tweezers and an OTW and find that both approaches can achieve a torque precision better than  $1 \text{ pN} \cdot \text{nm}$ . The OTW, capable of measuring torque on (sub)millisecond timescales, provides the best torque precision for measurement times  $\leq 10 \text{ s}$ , after which drift becomes a limiting factor. For longer measurement times, magnetic torque tweezers with their superior stability provide the best torque precision. Use of the Allan deviation enables critical assessments of the torque precision as a function of measurement time across different measurement modalities and provides a tool to optimize measurement protocols for a given instrument and application.

## INTRODUCTION

Techniques to manipulate single-molecule have enabled studies of the structure, function, interactions, and mechanical properties of biological macromolecules at unprecedented detail (1–7). Many single-molecule manipulation techniques, notably optical tweezers and atomic force microscopy, naturally operate in the space of (linear) extension and force. However, biological macromolecules are frequently subject to torsional strain, and the molecular motors that translocate along them must be able to progress amid accumulated twist and torque. To quantify these phenomena, a number of techniques that enable measurements

of rotation angle and torque (8,9) have been developed recently. Examples of such techniques (reviewed in (9)) include the rotor-bead-tracking assay (10–15), optical torque tweezers (16–28), and various extensions of magnetic tweezers comprising magnetic torque tweezers (29–32), freely orbiting magnetic tweezers (33,34), and electromagnetic torque tweezers (35). Similar to the field of force spectroscopy that has benefited from systematic analyses of the position and force precision of single-molecule techniques (36–44), torque- and twist-measuring techniques would be enriched by a better understanding of the achievable precision in angular detection and the determination of torque.

Here, we propose Allan deviation (AD) (38–49) as a criterion to systematically quantitate the angle and torque precision in single-molecule measurements. The AD allows us to critically assess the torque precision as a function of measurement time across different measurement modalities (e.g., magnetic versus optical torque tweezers) that rely on distinct physical principles. Being a real space quantity and having the same units as the observable of interest, it provides an intuitive and direct way to quantify and interpret precision (38–44). In addition to enabling direct quantitative comparisons of

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different torque and twist measurement strategies, use of the AD in a systematic way provides an experimental user with a very convenient tool with which to optimize the measurement protocol for a given instrument and system. Here, we investigate the AD method using simulated traces and demonstrate its application to various implementations of magnetic torque tweezers (MTT), electromagnetic torque tweezers (eMTT), and an optical torque wrench (OTW). Using the AD analysis, we arrive at clear recommendations, e.g., for the optimal in-plane magnetic field strength in the eMTT and for choosing an optimal trapping laser power in the OTW.

## MATERIALS AND METHODS

### Definition and properties of AD

Given a time series of  $N$  observations of some quantity  $\theta$  recorded at a sampling frequency  $f_s$  over a total measurement time  $t_{meas} = N/f_s$ , the Allan variance (AV) of  $\theta$  for the time interval  $\tau$  is defined as follows (42,43,45):

$$\sigma_{\theta}^2(\tau) = \frac{1}{2} \left\langle (\bar{\theta}_{i+1} - \bar{\theta}_i)^2 \right\rangle, \quad (1)$$

where  $\bar{\theta}_i$  is the mean of the  $i^{\text{th}}$  measurement interval of length  $\tau$ . The angle bracket  $\langle \dots \rangle$  denotes the arithmetic mean over all measurement intervals. In other words, the AV is one-half of the averaged square distance between the means of neighboring intervals. From its definition, the value of the AV is always greater than zero; it can only be computed for time intervals  $\tau \leq t_{meas}/2$ ; it is additive for independent signals, i.e., the AV is the sum of the individual AVs; and it is linear, i.e., a linear scaling of  $\theta$ ,  $\theta' = \alpha \cdot \theta$ , will simply scale the AV as follows:  $\sigma_{\theta'}^2(\tau) = \alpha^2 \cdot \sigma_{\theta}^2(\tau)$ . The property of linearity is convenient because it allows for analysis of uncalibrated signals with the AV (e.g., one can analyze the voltage signal from a quadrant photodiode, position-sensing detector, or photodiode without having to first convert to position or torque units). In addition, the linearity enables simple conversion from angle to torque signal (by multiplication with the rotational trap stiffness,  $\kappa_{\theta}$ , in units of pN · nm/rad) before or after evaluation of the AV. AD is defined as the square root of the AV:  $\sigma_{\theta}(\tau) = (\sigma_{\theta}^2(\tau))^{1/2}$ . Because AD has the same units as the quantity under investigation, it may be more intuitive to report ADs rather than AVs.

### Computation of the AV

In practice, the AV is estimated from a data set with a finite number of measurements using a discrete form of Eq. 1. In the simple form of the AV, the data are split in  $M$  bins of  $m$  data points each, and the value of each bin is the mean over its  $m$  data points. The mean-square difference of consecutive bins estimates the AV:

$$\sigma_{\theta}^2(m\tau_s) = \frac{1}{2(M-1)} \sum_{i=1}^{M-1} (\bar{\theta}_{i+1} - \bar{\theta}_i)^2, \quad (2)$$

where  $\tau_s$  is the sampling period and  $\bar{\theta}_i$  is the mean of the  $i^{\text{th}}$  bin of length  $m\tau_s$ . The sampling period is taken to equal the integration time. For camera-based detection in the magnetic tweezers, this assumes no dead time between frames, which is justified given the typical dead time ( $\sim 10 \mu\text{s}$ ) relative to the integration time ( $\sim 10 \text{ms}$ ). For photodiode-based detection in the OTW, the situation is quite different; whereas the effective integration time is very fast ( $\sim 10 \text{ns}$ ), the photodiode is only read out at  $\sim 100 \text{kHz}$ . The inverse of this rate ( $\sim 10 \mu\text{s}$ ) is analogous to a dead time, as no signal averaging occurs. Thus, in the OTW, the dead time far exceeds the integration time. However, the application of Eq. 2 remains valid in all situations

considered in this work because the sampling period is much shorter than the characteristic time of the system (Supporting Materials and Methods, Section 1). For each value of  $m$ ,  $m$  frameshifts exist to compute the AV (Fig. 1 A). The use of all of these frameshifts improves the estimate of the AV and is known as the ‘‘overlapping’’ AV (Eq. S3 in Supporting Materials and Methods, Section 2).

Whereas the AV is defined for all values of  $m$  (up to the maximum  $m = N/2$ ), the AVs for successive values of  $m$  are not independent and can be nearly identical because most values in a bin of size  $m$  are identical to the values in a bin of size  $m+1$ . For fitting of the AV data, it is therefore advantageous to calculate the octave-sampled AV by choosing  $m = 2^{\text{integer}}$ , which ensures nearly independent differences (46,47). We compute the AV (39) using a publicly available MATLAB (The MathWorks, Natick, MA) function (49). All AV curves are fit using maximum likelihood estimation with the shape factor by Lansdorp and Saleh (47) (Eq. S4 in Supporting Materials and Methods, Section 3).

### Analytic expression for the AV of a Brownian particle in a harmonic trap

We employ the analytical expression given by Lansdorp and Saleh (47,48) for the AV of a particle undergoing Brownian motion in a harmonic well and apply it to the case of rotational motion, as follows:

$$\sigma_{\theta}^2 = A \left( \frac{\tau_c}{\tau} \right)^2 \left( 2 \frac{\tau}{\tau_c} + 4 \exp\left(-\frac{\tau}{\tau_c}\right) - \exp\left(-2 \frac{\tau}{\tau_c}\right) - 3 \right), \quad (3)$$

where  $A = k_B T / \kappa_{\theta}$  and  $\tau_c = \gamma_{\theta} / \kappa_{\theta}$ . Here,  $\gamma_{\theta}$  is the rotational-friction coefficient and  $\kappa_{\theta}$  is the trap stiffness of the rotational trap. Note that  $k_B T / \kappa_{\theta} = \text{Var}(\theta)$  according to the equipartition theorem. We determine the friction coefficient  $\gamma_{\theta}$  and the trap stiffness  $\kappa_{\theta}$  by fitting the expression (Eq. 3) to our data using a maximum likelihood estimation algorithm (47). In the short time averaging limit, where diffusion is dominant, the AV reduces to the following:

$$\sigma_{\theta}^2 = \frac{2}{3} D \tau, \quad (4)$$

where  $D$  is the diffusion constant, which, according to the Einstein-Smoluchowski relation, equals  $k_B T / \gamma_{\theta}$ .

In most single-molecule experiments, the short time regime provides little information about the system under study because the particle can barely respond to changes on these timescales, particularly for often relatively slow torque measurements. For long averaging times, the AV reaches the so-called thermal limit, where it reduces to the following:

$$\sigma_{\theta}^2 = 2 A \frac{\tau_c}{\tau} = 2 \frac{\text{Var}(\theta)}{n} = \frac{2 k_B T \gamma_{\theta}}{\kappa_{\theta}^2 \tau}, \quad (5)$$

where  $n = \tau / \tau_c$  defines the number of independent observations. The averaging reduces the variance with the number of independent measurements  $n$ , and therefore, the AV decreases in a manner that is inversely proportional to  $\tau$ , improving the angle precision. In between these two limits, the AV peaks at  $\tau_{max}$ , with the best estimate of  $\tau_{max}$  ( $\approx 1.8926 \tau_c$ ) coming from the numerical solution of Eq. 3 as opposed to the analytical solution ( $= \sqrt{3} \tau_c$ ) of Eqs. 4 and 5.

Equations 3, 4, and 5 can be converted from angle to torque AV by straightforward application of the property of linearity; in the harmonic approximation, torque  $\Gamma$  is proportional to angle  $\theta$  ( $\Gamma = -\kappa_{\theta} \cdot \theta$ ), and hence,  $\sigma_{\Gamma}^2 = \kappa_{\theta}^2 \cdot \sigma_{\theta}^2$ . Thus, the thermal limit of the torque AV is given by the following:

$$\sigma_{\Gamma}^2 = \frac{2 k_B T \gamma_{\theta}}{\tau}. \quad (6)$$

In this limit, the AV for torque is independent of the trap stiffness  $\kappa_\theta$ , suggesting that stiffness has no effect on the torque precision in the regime in which the measurement precision is limited by thermal fluctuations (32).

## Stochastic simulations of rotational motion

To test our AD analysis and to illustrate the effects of various system parameters, we simulate stochastic time traces of rotational motion using numerical solutions to the corresponding overdamped Langevin equation (Fig. 1). To simulate the rotation angle as a function of time  $\theta(t)$ , we discretize time into time steps  $\Delta t$ . The angle at time step  $i + 1$ ,  $\theta_{i+1}$ , is given by the discretized overdamped Langevin equation as the following:

$$\theta_{i+1} = \theta_i + \left( \frac{\Gamma_{external} + \Gamma_{thermal}}{\gamma_\theta} \right) \Delta t, \quad (7)$$

where the right-hand side only involves quantities known at time step  $i$ ,  $\gamma_\theta$  is the rotational friction coefficient (in units of  $\text{pN} \cdot \text{nm} \cdot \text{s}$ ),  $\Gamma_{external}$  is the external torque, and  $\Gamma_{thermal} = N(0, 1) \cdot (2k_B T \gamma_\theta / \Delta t)^{1/2}$  with thermal energy  $k_B T \approx 4.1 \text{ pN} \cdot \text{nm}$  at room temperature and with  $N(0, 1)$  being Gaussian-distributed noise with zero mean and unit SD. The Langevin dynamics simulations were implemented using custom MATLAB routines (Supporting Materials and Methods, Section 4).

## AD measurements with magnetic tweezers

Torque application in magnetic tweezers relies on the alignment of superparamagnetic micron-sized beads or microspheres (referred to as “beads” from here on after) with an externally applied magnetic field (5,29,50). Both MTT and eMTT employ a predominantly vertical-oriented field generated by a cylindrical magnet and a smaller field in the horizontal direction generated by a side magnet in the MTT (32) (Fig. 2 A) or by electromagnets in the eMTT (35) (Fig. 3 A). The in-plane field generates a sufficiently weak angular trap to perform experiments on soft molecules, like DNA. Torque measurements in MTT and eMTT rely on tracking the rotational angle of the bead and observing changes in the equilibrium angle position of the bead inside the trap upon applying twist to a molecule of interest tethered between a surface and the magnetic bead. The torque is determined from the product of the angular shift and the trap stiffness, and hence, the angle AD can be determined directly from the angular traces, whereas the torque AD requires a calibrated trap stiffness. Limitations in angular tracking will therefore also affect the torque precision.

Our MTT and eMTT measurements of the AD use custom-built instruments described in detail elsewhere (32,35). In brief, they employ double-stranded DNA constructs bound to a flow cell surface via multiple digoxigenin-antidigoxigenin interactions and to superparamagnetic beads via multiple biotin-streptavidin interactions in phosphate-buffered saline. Bead sizes and DNA tether lengths are indicated in the main text and figure legends.

## AD measurements with optical tweezers

The OTW is an extension of conventional optical tweezers that exploits the exchange of angular momentum between a nanofabricated, birefringent particle and a polarized trapping beam to apply and measure torque (16–28). Unlike the magnetic tweezers, which employ standard commercially available magnetic beads (whose magnetic anisotropy governs the achievable torque levels (50) and in which a choice of diameters permits control over the drag coefficient), for the OTW no comparable particles exist. Instead, one typically custom-fabricates birefringent dielectric particles using one of several fabrication routes (top-down, bottom-up, etc.), materials (quartz  $\text{SiO}_2$  (0.009), vaterite  $\text{CaCO}_3$  (0.1), calcite  $\text{CaCO}_3$  (–0.16), rutile  $\text{TiO}_2$  (0.26); optical birefringences specified in parentheses), shapes

(spherical, cylindrical, etc.), and dimensions (with a size scale of a few micrometers being most prevalent) (23–28). In our custom-built instrument (22), we use cylindrically shaped rutile  $\text{TiO}_2$  nanoparticles (diameter  $\sim 215 \text{ nm}$ , height  $\sim 765 \text{ nm}$ ) fabricated in our cleanroom facility (26).

In the OTW, the optical tweezers trap a birefringent cylinder with its long axis aligned with the propagation direction of the light (Fig. 4 A). The linear polarization of the trapping laser clamps the angular position of the rutile  $\text{TiO}_2$  cylinder, and rotation of this polarization controls rotation of the particle about its long axis (26). The imbalance between left and right circularly polarized components in the output of the trap provides a direct measure for the exchange of angular momentum inside the trap and, hence, a measure for the optical torque transferred to the particle. In the AD measurements, we fixed the direction of the linear polarization and measured the fluctuations around this equilibrium position (Figs. S8 A and S9 A). The power of the trapping laser is tuned using a half-wave plate and a polarizing beam splitter, in the range of 10–80 mW at the laser focus.

## RESULTS

The AD is the square root of the AV, which is a type of variance that uses samples averaged over variable time intervals  $\tau$  and that is computed from the difference between neighboring intervals (Materials and Methods). Although other approaches to quantifying precision exist (e.g., other variances, autocorrelation, or power spectrum analyses (Supporting Materials and Methods, Sections 5 and 6)), we find AD to be a particularly convenient measure for several reasons: 1) the AD at time  $\tau$  provides a direct and intuitive measure of the precision expected for a measurement of a given duration; 2) being a real space quantity, the AD is immediately in the same units as that of the measured quantity of interest; 3) the AD is powerful in detecting low frequency, long-time scale drifts (43), which are critical for single-molecule measurements of torque and twist; and 4) the AD can be straightforwardly computed from the raw experimental data without the need to be calibrated a priori. In the following section, we explore the use of AD to quantify the angle and torque precision of single-molecule measurements. First, we present the results of stochastic simulations to introduce the concept of AD and validate our approach. We then use AD to compare the precision of three different single-molecule torque spectroscopy techniques: MTT, eMTT, and an OTW.

## AD analysis of simulated traces

To explore the effects of the various system parameters on the AD, we simulated traces of the stochastic rotational motion of a bead subject to Brownian fluctuations while held in a harmonic trap (Fig. 1, B–D; Fig. S1). The simulated rotational motion (about an axis through the bead’s center of mass) reveals the effects of varying rotational trap stiffness  $\kappa_\theta$  and rotational drag coefficient  $\gamma_\theta$  on the angular time trace (Fig. 1 B) and on the angle AD (Fig. 1 C) and torque AD (Fig. 1 D). In the green data set,  $\gamma_\theta = 10 \text{ pN} \cdot \text{nm} \cdot \text{s}$  and  $\kappa_\theta = 1000 \text{ pN} \cdot \text{nm}/\text{rad}$  such that the characteristic time is  $\tau_c = \gamma_\theta / \kappa_\theta = 10 \text{ ms}$ . To compare the effect of

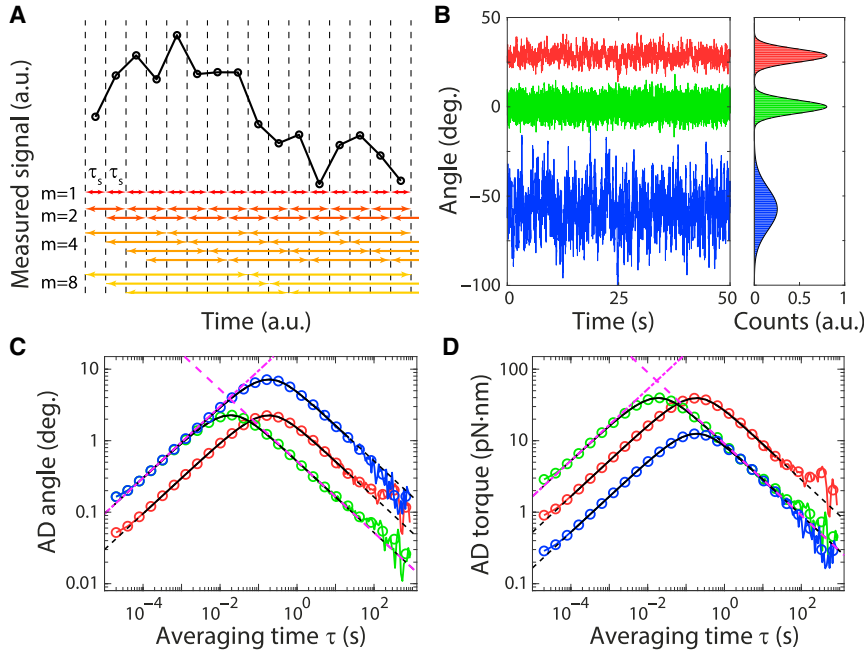


FIGURE 1 AD of simulated traces. (A) An illustration of the octave-sampled overlapping AD is shown. The example trace (*black*) contains 16 data points. Each data point is recorded during the sampling period  $\tau_s$ . The data are split into bins of  $m$  data points. In octave-sampled data,  $m = 2^{\text{integer}}$  (going from *red* to *yellow*,  $m = 1, 2, 4, 8$ ). Splitting in bins is possible in  $m$  different frame shifts. For  $m = 8$ , only three frame shifts are displayed for clarity. (B) Simulated angle traces of  $\sim 1700$  s each sampled at 50 kHz (corresponding to  $8.5 \times 10^7$  data points) are shown for rotational Brownian motion of particles in harmonic traps. The left panel shows a zoom-in on the first 50 s of the traces, and the right panel shows the histograms for the full traces. The traces are offset vertically for clarity. The red, green, and blue traces (from top to bottom) are simulations with drag coefficient  $\gamma_\theta = 100, 10$ , and  $10$  pN  $\cdot$  nm  $\cdot$  s and trap stiffness  $\kappa_\theta = 1000, 1000$ , and  $100$  pN  $\cdot$  nm/rad, respectively. (C and D) Angle and torque ADs for the traces in (B) are shown. Colored lines (*circles*) reflect the normal AD (octave-sampled overlapping AD). The results of the fits are indicated by solid black lines, and their extrapolations are indicated as dashed black lines (Eq. 3). The fitted parameters are  $\gamma_\theta = 99.4 \pm 0.1, 9.9 \pm 0.01$ , and  $10.0 \pm 0.01$  pN  $\cdot$  nm  $\cdot$  s and  $\kappa_\theta = 1009.6 \pm 36.6, 998.9 \pm 9.7$ , and  $99.6 \pm 2.9$  pN  $\cdot$  nm/rad for the red, green, and blue data, respectively, from  $N = 5$  independent simulated traces for each condition. The dash-dotted and dashed magenta lines are the diffusion and thermal limits, shown for the green data sets only. To see this figure in color, go online.

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different drag coefficients, we simulate the red data set with the same stiffness but with a 10-fold-higher drag coefficient,  $\gamma_\theta = 100$  pN  $\cdot$  nm  $\cdot$  s. To compare the effect of different stiffnesses, we generate the blue data set with the same drag coefficient as that of the green data set but with 10-fold-lower trap stiffness,  $\kappa_\theta = 100$  pN  $\cdot$  nm/rad. All other parameters are identical for the three simulated traces.

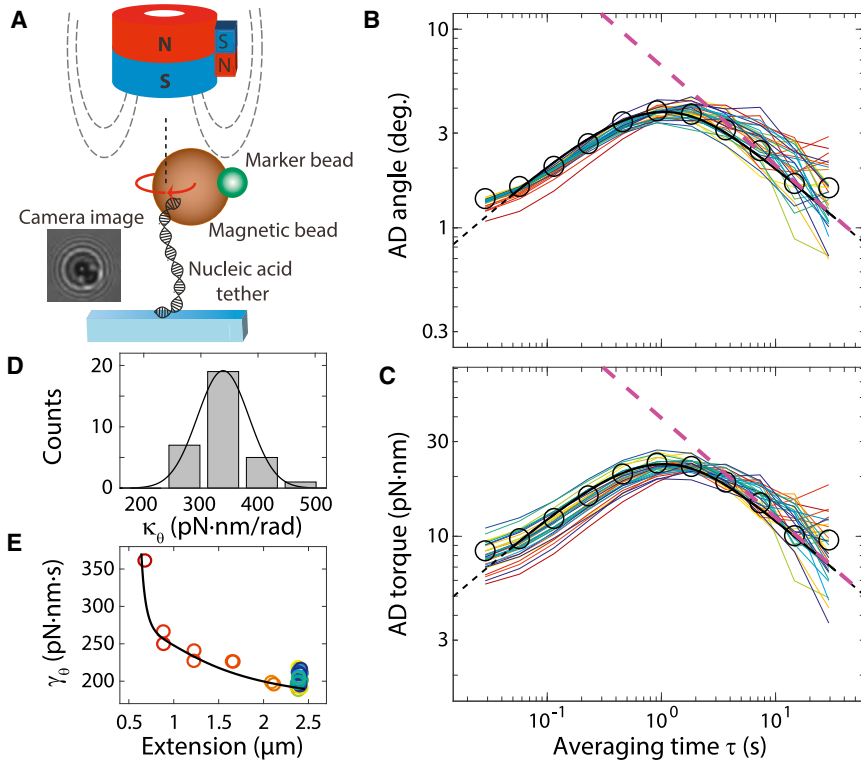
The simulated angle traces provide an instructive example of how the system parameters affect the observed behavior. The widths of the histograms (Fig. 1 B)—and thus, the amplitude of the angular fluctuations—are indifferent to changes in drag coefficient (compare *green* and *red* data sets) but are affected by changes in stiffness (compare *green* and *blue* data sets); a decrease in stiffness causes increased angular fluctuations, as expected from the equipartition theorem. Another feature visible in the angle traces is the timescale over which the angular fluctuations occur. The fluctuations in the green data appear “denser” on the time axis compared to the red and blue data because the characteristic time  $\tau_c$  for the green data set (10 ms) is smaller than for the red and blue data sets (100 ms).

The ADs (Fig. 1, C and D) for our simulated traces all display the expected trend of an initial rise proportional to  $\tau^{1/2}$  and a transition to a decrease proportional to  $\tau^{-1/2}$  for larger  $\tau$  (43). Changing the drag coefficient causes a shift of the curve on the time axis in both angle and torque ADs (*green* and *red* data sets). This shift indicates that a higher drag coefficient is linked to slower dynamics, which is

consistent with the higher characteristic time  $\tau_c$ . For the angle AD (Fig. 1 C), the change in stiffness initially has no effect; the curves overlap in the diffusion limit (*green* and *blue* data sets, Eq. 4). However, at longer timescales, a higher stiffness results in an improved angular precision (Eq. 5). In contrast, different stiffnesses do not alter the torque precision for large  $\tau$  (Fig. 1 D) because in the thermal limit, the torque precision is independent of the trap stiffness  $\kappa_\theta$  (Eq. 6). The analytical expression for the AV (Eq. 3) provides an excellent fit to the data, and we recover the values for  $\kappa_\theta$  and  $\gamma_\theta$  input into the simulations, confirming the validity of the method (Fig. 1, C and D, where the range of fitted data indicated by the black solid lines is constrained at the shortest and longest integration time limits to avoid the influence of noise not taken into consideration in Eq. 3); the same approach was followed in Figs. 2, 3, and 4.

### Angle and torque precision in the MTT

The MTT employ a cylindrical magnet to generate a predominantly vertical-oriented field and a side magnet to apply an additional, smaller field in the horizontal direction. MTT measure torque by detecting changes in the equilibrium position of the bead-rotation angle about the tether axis upon over- and underwinding nucleic acid tethers (30–32) (Materials and Methods and Fig. S2, A–C). Here, we analyze traces of angular fluctuations recorded in our MTT implementation (Fig. 2 A) using a 2.8- $\mu$ m-diameter magnetic bead and a 1- $\mu$ m-diameter nonmagnetic fiducial



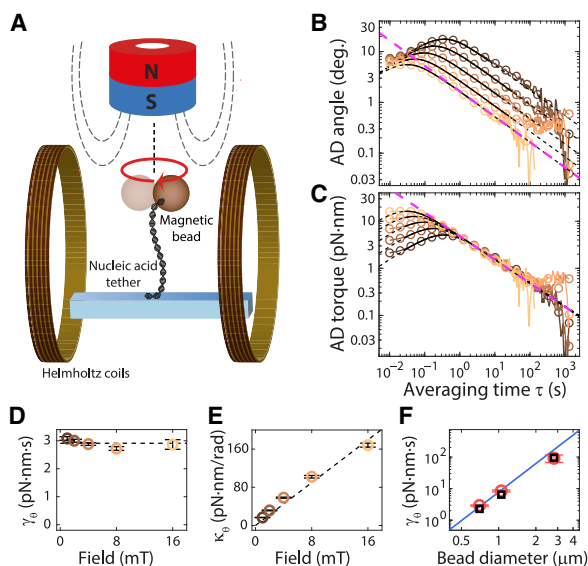
**FIGURE 2** Angle and torque precision in the magnetic torque tweezers (MTT). (A) A schematic of the “classical” MTT implementation is shown (32). Angle tracking is achieved by attaching a smaller ( $1\ \mu\text{m}$  diameter) nonmagnetic marker bead (green) to a larger ( $2.8\ \mu\text{m}$  diameter) magnetic bead (brown) and tracking the rotation of the bead pair from charge-coupled device images (inset). The magnetic bead is tethered to a glass slide (blue) by a single DNA molecule (black), held, and manipulated in a weak rotational trap set up by vertically aligned permanent magnets with a side magnet added (top). The axis of bead rotation is indicated by the vertical dashed black line. (B) Octave-sampled overlapping ADs of 32 angle traces of 100 s each sampled at 35 Hz (corresponding to  $3.5 \times 10^3$  data points) are shown, recorded in a torque measurement on a single 7.9 kbp DNA molecule (each trace is shown as a distinctly colored solid line, denoting the number of applied turns). The octave-sampled points for a single trace are shown as black circles. The fit of the analytical expression for the AV (Eq. 3) is shown as a solid black line, and its extrapolation is shown as a dashed black line. The thermal limit is indicated as a dashed magenta line. (C) Torque AD of the same traces as (B) obtained by multiplication with the corresponding trap stiffnesses (color-coding is as in (B)) is shown. Similar to (B), octave-sampled points for one trace are shown as black circles, the fit to Eq. 3 (multiplied by  $\kappa_\theta^2$ ) is shown as a solid black line, and its extrapolation

is shown as a dashed black line. The thermal limit is indicated as a dashed magenta line. (D) The values for the trap stiffness  $\kappa_\theta$  determined from the fits for all traces in (B) are shown. The data are approximately Gaussian distributed (solid black line) with a SD of  $45\ \text{pN} \cdot \text{nm}/\text{rad}$ . (E) Rotational friction coefficients  $\gamma_\theta$  (distinctly colored circles) determined from the AV fits for all traces in (B) are shown as a function of the height of the bead above the flow cell surface. The color-coding denotes the number of applied turns. The solid black line reflects a prediction for the rotational friction coefficient of a  $2.8\text{-}\mu\text{m}$ -diameter bead rotating on a circular trajectory, taking into account corrections due to the presence of the surface. To see this figure in color, go online.

marker bead to track the rotation angle about the tether axis from analysis of camera images (51) (Fig. 2 A, inset). We focus on a representative data set consisting of 32 angle traces, recorded while over- and underwinding a 7.9 kbp DNA molecule tethered between the magnetic bead and the flow cell surface and held at a stretching force of  $\sim 2\ \text{pN}$ . Upon over- and underwinding the DNA by integer numbers of turns, systematic changes of the equilibrium angle position are visible (Fig. S2 C, middle panel, left axis). These can be related to the changes in the torque exerted by the molecule (Fig. S2 C, middle panel, right axis) by multiplying with the mean trap stiffness (deduced from the fits to AD curves, as detailed below, and equivalent to deducing the trap stiffness from the SD of the angular fluctuations; Fig. S2 C, top panel). In addition, we observe that tether extension decreases rapidly past the buckling point of the DNA molecule for positive turns (corresponding to overwinding) but stays approximately constant for negative turns (corresponding to underwinding) because of torque-induced DNA melting (32,52) (Fig. S2 C, bottom panel).

Applying our AD analysis to the angle traces recorded in the MTT at different numbers of applied turns reveals some variability but indicates that we generally reach an angle

precision of  $\sim 1^\circ$  for a 50 s measurement (Fig. 2 B). From fits of the analytical expression (Eq. 3) to the angle AV data, we obtain the trap stiffness for each trace (Fig. 2 D), revealing a  $\sim 13\%$  variation from trace to trace without any systematic changes throughout the measurement (Fig. S2 D). This yields a mean trap stiffness of  $339 \pm 45\ \text{pN} \cdot \text{nm}/\text{rad}$ , which is in excellent agreement with the value obtained from directly computing the SD of the angular fluctuations ( $330 \pm 46\ \text{pN} \cdot \text{nm}/\text{rad}$ ). Multiplying each angle AD curve by its fitted value of the trap stiffness, we convert the angle to a torque signal (Fig. 2 C). AD analysis of the torque signal indicates that the torque precision in the MTT follows the thermal limit (Fig. 2 C, dashed magenta line) for measurement times longer than  $\sim 2\ \text{s}$  and reaches  $\sim 5\ \text{pN} \cdot \text{nm}$  after 50 s (Fig. 2 C). These results are consistent with our previous torque precision estimate for this setup (32) of  $1\text{--}3\ \text{pN} \cdot \text{nm}$  for a 300 s measurement. In addition, we obtain values for the drag coefficient from the AV fits that exhibit systematic changes with DNA tether extensions, increasing by 70–80% upon decreasing the extension from 2.4 to  $0.7\ \mu\text{m}$  (Fig. 2 E). Both the observed value for the drag coefficients and the dependence on DNA extension are in reasonable agreement with the predictions



**FIGURE 3** Angle and torque precision in the electromagnetic torque tweezers (eMTT). (A) A schematic of the eMTT setup (35) is shown. A magnetic bead (brown) is tethered to a glass slide (blue) by a single 3.4 kbp DNA molecule (black). The bead is lifted off from the surface by a cylindrical magnet (top). Four coils (only two are shown here) generate an in-plane magnetic field to orient the bead. Here, the angular orientation of the magnetic bead is deduced from its spatial position within a circular annulus whose radius is set by the distance between the tether attachment point and the pole of the magnetic bead (35). The axis of bead rotation is indicated by the vertical dashed black line. (B) The angle ADs of angle traces of  $\sim 2600$  s each (except at 16 mT; 280 s) sampled at 100 Hz (corresponding to  $2.6 \times 10^5$  data points) are shown, recorded on a single DNA-tethered bead at 1, 2, 4, 8, and 16 mT (going from dark brown to light brown). Colored lines (circles) reflect the normal AD (octave-sampled overlapping AD). The octave-sampled data are used to fit (solid black lines) the data to the analytical expression (Eq. 3), and their extrapolations are shown as dashed black lines. The dashed magenta line indicates the thermal limit for the stiffest trap. (C) The torque ADs of the same traces as (B) obtained by multiplication with the corresponding trap stiffnesses are shown. The color-coding is the same as in (B). The dashed magenta line indicates the thermal limit. (D and E) The values of the rotational drag coefficient  $\gamma_\theta$  and the rotational trap stiffness  $\kappa_\theta$  obtained from the fits in (B) are shown. The data points and their corresponding error bars denote the average and SD, respectively, from  $N = 5$  independent measurements. In (D), the dashed black line is a constant-value fit to the drag coefficients. In (E), the dashed black line is a linear fit to the data through the origin. (F) Drag coefficients from AV fits for three different bead sizes ( $d = 0.7, 1.05, \text{ and } 2.8 \mu\text{m}$ ; Figs. S3–S5) are shown. Red circles and error bars are the drag coefficients (mean  $\pm$  SD) determined from AV fits for differently sized beads (Figs. S3 G–S5 G) averaged over measurements at different field strengths. Black squares are the predictions from Eq. S10. The solid blue line is a fit of the scaling relation  $\gamma_\theta \sim d^3$ . To see this figure in color, go online.

of a model (Fig. 2 E, solid black line) that describes the rotation of a 2.8- $\mu\text{m}$ -diameter bead along a circular trajectory, taking into account the increase in friction coefficient due to the proximity of the flow cell surface (53,54) (see Eq. S10 in Supporting Materials and Methods, Section 7). The observed dependence of the friction coefficient on DNA tether extension highlights the ability of our AD analysis to detect subtle changes in measurement parameters and

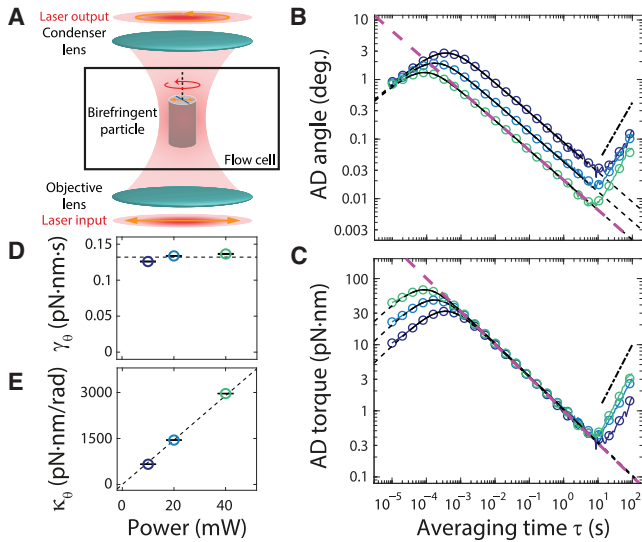
demonstrates the importance of taking into account surface proximity effects when evaluating friction coefficients in single-molecule measurements (55).

### Angle and torque precision in the eMTT at different fields

eMTT (Fig. 3 A) are similar to MTT; the main difference is that in the eMTT, electromagnets (implemented as two pairs of Helmholtz coils) generate a field in the horizontal direction. eMTT have an advantage over MTT in that the horizontal field component is readily tunable by altering the current in the Helmholtz coils (35). The ability to tune the trap stiffness, however, raises the question of what stiffness is optimal for a given torque measurement application. To explore the effects of trap stiffness and bead size, we measured angular fluctuations and analyzed the ADs of several differently sized DNA-tethered beads in the eMTT (Figs. S3–S5); for each bead size, measurements were carried out at different applied currents in the Helmholtz coils, corresponding to the different applied fields in the horizontal direction. We present the results of a single 0.7- $\mu\text{m}$ -diameter bead trapped at different magnetic field strengths in Fig. 3.

From the AD of the angle signal in the eMTT, it is apparent that higher fields, corresponding to higher trap stiffnesses, give rise to a better angle precision (Fig. 3 B). For the 0.7- $\mu\text{m}$ -diameter beads, the measurements reach  $\sim 1^\circ$  precision in 3 s at the highest field strength of 16 mT (Fig. 3 B, lightest brown). This is much faster than what was observed in the MTT ( $\sim 50$  s, Fig. 2 B) despite the lower trap stiffness employed in the eMTT and results from our use of much smaller beads in the eMTT measurement. Converting the angle AD to torque AD by multiplication with the trap stiffness (itself deduced by fitting the corresponding angle AD curve), we find that the torque precision measurements are independent of trap stiffness in the thermal limit, i.e., at times longer than  $\sim 1$  s (Fig. 3 C), as is expected from Eq. 6. The torque AD is identical for all employed trap stiffnesses for times between 1 and 100 s and already reaches a torque precision of  $\sim 5$  pN  $\cdot$  nm after 1 s, which is again much faster than in the MTT ( $\sim 50$  s, Fig. 2 C) because of the smaller beads used here. The torque precision reaches  $\sim 0.5$  pN  $\cdot$  nm for 100 s measurements (Fig. 3 C). The angle ADs are well described by the analytical expression in Eq. 3, yielding fitted drag coefficients  $\gamma_\theta$  (Fig. 3 D) that are independent of the magnetic field, as expected, and fitted trap stiffnesses  $\kappa_\theta$  (Fig. 3 E) that increase monotonically with the magnetic field. In the field range used in our implementation of the eMTT (1–16 mT), the dependence of  $\kappa_\theta$  on field can be reasonably approximated as linear (35) (Fig. 3 E, dashed black line).

In these eMTT measurements, we start to see deviations from the thermal limit behavior ( $\propto \tau^{-1/2}$ ) after  $\sim 100$  s, and the torque AD signals for different field strengths begin



**FIGURE 4** Angle and torque precision in the optical torque wrench (OTW). (A) A schematic of the OTW setup (22) is shown. The objective lens focuses a linearly polarized laser beam input (red) and traps a birefringent cylinder (gray) near the focus within a flow cell. Manipulation of the linear polarization allows us to control the angular position of the particle. At the output of the trap, the laser light is collected by a condenser lens. The polarization state of the output reports on the torque transferred from beam to particle. The axis of cylinder rotation is indicated by the vertical dashed black line. (B) The angle AD obtained from (C) by division with the corresponding trap stiffnesses is shown. Colored lines (circles) reflect the normal AD (octave-sampled overlapping AD). The color-coding is the same as in (C). The dashed magenta line indicates the thermal limit for the stiffest trap. (C) The torque ADs of torque traces of 200 s each sampled at 100 kHz (corresponding to  $2.0 \times 10^7$  data points) are shown, recorded on a single rutile  $\text{TiO}_2$  cylinder at 10, 20, and 40 mW (going from dark blue to light green). The octave-sampled data are used to fit (solid black lines) the data to the analytical expression (Eq. 3, multiplied by  $\kappa_\theta^2$ ), and their extrapolations are shown as dashed black lines. The fits only provide two independent parameters,  $\gamma_\theta$  and  $\kappa_\theta$ , so the system was precalibrated (22) to obtain the detector sensitivity in units of  $\text{pN} \cdot \text{nm}/\text{mV}$ . The dashed magenta line indicates the thermal limit. The dash-dotted black line has slope of +1, corresponding to linear drift. (D and E) The values of the rotational drag coefficient  $\gamma_\theta$  and the rotational trap stiffness  $\kappa_\theta$  obtained from the fits in (C) are shown. The data points and their corresponding error bars denote the average and SD, respectively, from  $N = 5$  independent measurements. In (D), the dashed black line is a constant-value fit to the drag coefficients. In (E), the dashed black line is a linear fit to the data through the origin. To see this figure in color, go online.

to differ. In general, for times longer than  $\sim 100$  s, the torque AD is higher for higher field strengths because of pronounced drifts that become apparent with increases in the torque AD with time for long times (Fig. 3 C, see traces at 4 and 8 mT). The drifts are very likely due to heating of the coils when relatively high currents are run to achieve high fields for extended periods of time. Our present implementation of the eMTT requires  $\sim 16$  A to achieve  $\sim 16$  mT field and is air-cooled only (35). The heating is most dramatically visible in the trace at 16 mT, which had to be terminated after  $\sim 280$  s (Fig. S3 A) as the coils reached a temperature of  $60^\circ\text{C}$ , at which point they are shut down by an automatic safety switch. A clear recommendation

that emerges from the AD analysis is, therefore, to run at low field strengths (and thus low trap stiffnesses) in the eMTT for optimal torque measurements. In the absence of drift, higher trap stiffnesses do not confer any disadvantages in the torque precision; yet, the high currents required for high trap stiffnesses tend to cause significant drifts because of heating and thus deterioration of the torque precision for times longer than  $\sim 100$  s. In contrast, for low currents and trap stiffnesses, we observe very low levels of drifts even for (very) long measurements, and reach, e.g., a best precision of  $\sim 0.1 \text{ pN} \cdot \text{nm}$  for  $\sim 1000$  s measurements at  $\leq 2$  mT.

### Angle and torque precision in the eMTT for different bead sizes

In addition, in the eMTT experiments, we probe the effect of different drag coefficients by comparing different bead sizes at a roughly constant trap stiffness (Fig. S6). Similar to the simulations (Fig. 1, C and D), a higher drag coefficient shifts the AD curve to longer timescales. At intermediate averaging times  $\tau = 10\text{--}100$  s, the smaller the bead, the better the angle and torque precision, as expected from the corresponding thermal limits (Eqs. 5 and 6, respectively). The rotational drag coefficients obtained from the AV fits (Fig. 3 F, red circles) are in good agreement with predictions of the model (Fig. 3 F, black squares) that take into account the bead and tether geometry and surface effects (Eq. S10) and that roughly follow a  $\gamma_\theta \sim d^3$  scaling, where  $d$  is the bead diameter (Fig. 3 F, solid blue line). The bead size analysis confirms that a decrease in drag coefficient improves the precision in both angle and torque.

As an independent test of the torque precision achieved in the eMTT, we analyzed a high-precision DNA torque measurement that employed  $1.05\text{-}\mu\text{m}$ -diameter beads and a measurement time of 200 s per measurement point (Fig. S7 A). The torque AD analysis (Fig. S4 F) suggests that this measurement should achieve a torque precision of  $0.5\text{--}0.9 \text{ pN} \cdot \text{nm}$  at  $\sim 200$  s. We analyzed the deviations of the measured torque values from a strictly linear behavior in the elastic response regime (Fig. S7 B) and the deviations from constant torque in the DNA melting regime (Fig. S7 C). The deviations are approximately Gaussian distributed with SDs of 0.9 and  $0.6 \text{ pN} \cdot \text{nm}$  for the two regimes, respectively, which is in excellent overall agreement with the expected precision from the AD analysis.

### Angle and torque measurements in the OTW

In the OTW measurements, we keep the linear polarization of the trapping beam fixed and measure the torque transferred from the laser beam to a trapped, birefringent cylinder undergoing thermal fluctuations (Materials and Methods, Fig. 4 A). The cylinders are fabricated out of rutile  $\text{TiO}_2$ , which is selected over other materials (e.g., quartz  $\text{SiO}_2$ ) for its extraordinarily high birefringence. Whereas

the OTW directly measures angular momentum transfer and thus torque, the torque traces are recorded in voltage. The corresponding AD can be converted to either the angle AD in degrees (Fig. 4 B) or the torque AD in pN · nm (Fig. 4 C) using parameters obtained through a separate calibration process (22). We also fit the torque AD (Eq. 3, multiplied by  $\kappa_\theta^2$ ) to obtain values for the parameters  $\kappa_\theta$  and  $\gamma_\theta$ . The drag coefficient  $\gamma_\theta$  is nearly independent of laser power (Fig. 4 D) and averages to  $0.13 \pm 0.01$  pN · nm · s, which is in good agreement with a theoretical value of  $\sim 0.12$  pN · nm · s (56). The angular trap stiffness  $\kappa_\theta$  increases linearly with the laser power (Fig. 4 E), i.e., quadratically with the electric field amplitude (9). The ADs for the OTW data (Fig. 4, B and C) report on the precision of this experimental apparatus. As in the eMTT, we observe that angular precision improves, e.g., from  $\sim 0.03^\circ$  to  $\sim 0.007^\circ$  at  $\sim 10$  s (Fig. 4 B) with increased stiffness (achieved by increasing laser power from 10 to 40 mW). At the highest laser power, the measurements reach an angular precision of  $\sim 1^\circ$  after only 0.3 ms, which is a much shorter timescale than in the MTT and eMTT measurements, and it results from the higher trap stiffness and lower drag coefficient in the optical tweezers (compare D and E in Figs. 2, 3, and 4). For the torque AD (Fig. 4 C), all curves converge to the thermal limit. Similar dependencies for laser powers up to 80 mW were observed in a separate data set (Fig. S9).

The best torque precision in the OTW achieved is  $\sim 0.3$  pN · nm, which is comparable to  $\sim 0.1$  pN · nm precision achieved in the eMTT measurements. This requires the optimized environmental conditions reflected in Fig. 4 and Fig. S8 (see, for comparison, Fig. S9, where air currents induced earlier onset of drift) and is achieved after an averaging time of  $\sim 10$  s at a laser power of 10 mW (Fig. 4 C). On longer timescales, we find that drift in the OTW becomes dominant and deteriorates the precision. Similar dominance of drift only appears after  $\sim 100$  s in the eMTT and only at high Helmholtz fields ( $\geq 4$  mT). The earlier onset of drift in the OTW compared to the eMTT derives from the increased number of optical and electronic components present, coupled to laser-power-dependent heating (observable from  $\sim 10$  s onwards in Fig. 4, B and C). These clear differences observed in the noise highlight the ability of our AD analysis to detect and compare noise components among different setups and environmental conditions.

## DISCUSSION

Examination of the AD provides insights into the achievable precision and optimal measurement duration and parameters. For a hypothetical measurement without drift, the AD can become arbitrarily small, provided that the trace is averaged long enough, as the AD decreases in the thermal limit as  $\tau^{-1/2}$ . This would imply that the precision achievable experimentally could be arbitrarily high. In practice, of course, noise other than the white noise deriving from

thermal fluctuations will kick in and limit further improvements in precision. Given the additive nature of the AD (Eq. 2), at a certain averaging time  $\tau$ , drift will start to dominate over the thermal limit; on longer timescales, the precision will no longer improve with averaging but rather worsen. The resulting minimum in the AD then designates the best achievable precision and, hence, the optimum measurement time. Different sources of drift will exhibit distinct signatures in the AD. For example, for linear drift, the AD should increase as  $\tau^1$  (Supporting Materials and Methods, Section 6), as we observe for the OTW traces (Fig. 4, B and C,  $\tau = 10$ – $100$  s). If the dominant source of noise has a  $1/f$  character, then the AD scales as  $\tau^0$  (i.e., becomes constant; Supporting Materials and Methods, Section 6), as we observe around 2 s in the AD plots for the OTW data set presented in Fig. S9, E and F.

In this work, we have introduced the use of the AD to evaluate the performance of several instruments designed to measure torque on individual (biological) molecules. In both the MTT and eMTT measurements, drift does not appear to significantly limit the measurements, even for very long measurement times (Fig. 3, B and C,  $\tau = 100$ – $1000$  s), provided that low enough Helmholtz fields ( $\leq 2$  mT) are used to avoid drifts through heating of the coils in the eMTT configuration. It might be possible to avoid this limitation in future implementations, e.g., by configuring water-cooled coils. Nonetheless, even the current instrument enables measurements with a torque precision better than 1 pN · nm (Fig. 3 C; Figs. S3 F–S5 F and S7). We achieved a similar torque precision ( $\sim 0.3$  pN · nm in 10 s, Fig. 4 C; for direct comparison with the eMTT, see Fig. S10) in the OTW under the best conditions (low laser power and blocking of air current). Potentially, the precision of the OTW can be enhanced by further improvements to the instrument's long-term stability.

A general lesson from our analysis is that to optimize torque and/or angle precision, the drag coefficient should be minimized particularly by using smaller particles (8). The eMTT data sets clearly demonstrate the improvements in precision obtained through using smaller beads; recent approaches to angle and torque measurements using gold nanoparticles push this development even further (15). Furthermore, once a particle size has been selected, it is generally advisable to maximize the trap stiffness for improved angle (but not torque) precision, given measurement times in which precision is thermally limited. However, there are important caveats to this general advice: first, smaller particles usually result in reduced stiffness and achievable torque because they contain less volume for torque exchange (lower magnetic content in magnetic beads and a shorter light path in birefringent particles); second, increasing the trap stiffness can result in increased drift because of practical limitations (e.g., heating from increased current in eMTT or laser power in OTW), deteriorating the precision for longer measurement timescales; third, the use

of ever-smaller particles may push the limits of the detection systems (e.g., pixel size for camera-based signal acquisition and diode sensitivity for photodiode-based signal acquisition); fourth, maximization of the trap stiffness and minimization of the drag coefficient reduce the characteristic time  $\tau_c$ , which demands faster acquisition systems, as most calibration methods (and particularly AD analysis; see [Supporting Materials and Methods](#), Section 1) require measurements on timescales shorter than  $\tau_c$ ; and finally, the timescale of dynamics in the system under investigation and the quantity of interest, angle or torque, ultimately determine the optimal drag coefficient and stiffness of operation.

The AD provides a direct and quantitative measure for the precision in single-molecule experiments. It can therefore be employed as a tool for optimizing experimental assays; it can be used to systematically track down sources of drift and other forms of noise and to determine the optimal measurement time at the desired precision. We foresee that usage of the AD analysis will instruct researchers about optimal measurement strategies and will thus facilitate new breakthroughs in the field of single-molecule torque spectroscopy.

## SUPPORTING MATERIAL

Supporting Materials and Methods and eleven figures are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(18\)30325-4](http://www.biophysj.org/biophysj/supplemental/S0006-3495(18)30325-4).

## AUTHOR CONTRIBUTIONS

M.M.v.O., J.L., and N.H.D. designed the research. J.L. and N.H.D. directed the research. T.J. and M.L. performed the MTT and eMTT experiments, respectively. M.M.v.O. and S.H. conducted the OTW experiments. M.M.v.O., S.H., and J.L. analyzed the data. All authors discussed the data and M.M.v.O., S.H., J.L., and N.H.D. wrote the manuscript.

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## SUPPORTING CITATIONS

References (57–61) appear in the [Supporting Material](#).

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