Signature of frustrated moments in quantum critical CePd$_{1-x}$Ni$_x$Al

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CePdAl with Ce 4$f$ moments forming a distorted kagome network is one of the scarce materials exhibiting Kondo physics and magnetic frustration simultaneously. As a result, antiferromagnetic (AF) order setting in at $T_N = 2.7$ K encompasses only two-thirds of the Ce moments. We report measurements of the specific heat, C, and the magnetic Grüneisen parameter, $\Gamma_{\text{mag}}$, on single crystals of CePd$_{1-x}$Ni$_x$Al with $x \leq 0.16$ at temperatures down to 0.05 K and magnetic fields $B$ up to 8 T. Field-induced quantum criticality for various concentrations is observed with the critical field decreasing to zero at $x_c \approx 0.15$. Remarkably, two-dimensional AF quantum criticality of Hertz-Millis-Moriya type arises for $x = 0.05$ and $x = 0.1$ at the suppression of three-dimensional magnetic order. Furthermore, $\Gamma_{\text{mag}}(B)$ shows an additional contribution near 2.5 T for all concentrations, which is ascribed to correlations of the frustrated one-third of Ce moments.

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New quantum states of matter, arising in materials with competing interactions and multiple energetically degenerate configurations are of strong interest in condensed matter physics. For example, unconventional superconductivity is found near quantum critical points (QCPs) [1–5], and spin-liquid phases—driven by strong frustration—have been realized in magnetic insulators [6,7]. However, there are only a few studies on metallic frustrated magnets [8], and the effect of frustration on quantum criticality in metals has rarely been investigated experimentally. Rare-earth heavy-fermion (HF) metals, consisting of 4$f$ moments coupled to conduction electrons by an exchange interaction $J$, are ideally suited for this purpose. Since $J$ governs the competition between the indirect Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange and the Kondo interaction [9], QCPs can be realized by variation of $J$ with pressure, chemical composition, or magnetic field [10–12]. Unconventional quantum criticality with a Kondo breakdown and a spin-liquid phase of localized 4$f$ moments being decoupled from conduction electrons has been predicted for high degree of frustration [13]. The “global phase diagram”, which classifies the electronic and magnetic ground states for HF systems, treats $J$ and the strength of quantum fluctuations arising from frustration as two independent parameters [14–16].

The effect of geometrical frustration in Kondo lattices has been recognized in hexagonal systems crystallizing in the ZrNiAl structure. Here, the 4$f$ electrons form a structure of equilateral corner-sharing triangles in the $ab$ plane, which can be described as a distorted kagome network. For YbAgGe, the geometrical frustration leads to a series of almost degenerate magnetic states tuned by magnetic fields and novel quantum bicritical behavior [17–19]. CeRhSn does not display long-range order and is located close to a QCP driven by geometrical frustration [20]. In CePdAl the magnetic frustration gives rise to unusual magnetic ordering [21–24]. It has been shown previously using polycrystals that the material can be tuned through a QCP with the aid of chemical pressure, realized by partial substitution of Pd by Ni [25].

CePdAl exhibits a strong magnetic anisotropy with the susceptibility ratio $\chi_c/\chi_{ab} \approx 15$ at $T \approx 5$ K, which is attributed to crystalline-electric-field and exchange anisotropies [26]. Upon cooling, the electrical resistivity exhibits a $-\ln T$ dependence from 20 to 6 K, followed by a coherence maximum at 4 K and a subsequent decrease [27,28]. The presence of the Kondo effect in CePdAl is confirmed by a maximum of the thermopower at 8 K [29]. Below $T_N = 2.7$ K partial AF order is observed [21]: despite being crystallographically equivalent, there appear three magnetically inequivalent sites. Ce(1) and Ce(3) exhibit long-range ordered moments, while Ce(2) does not, even down to lowest $T$ [30]. The ordered Ce moments form ferromagnetic chains in the basal plane, which are coupled antiferromagnetically and separated by the latter [21,31]. Along the crystallographic $c$ axis an incommensurate sinusoidal modulation of the magnitude of the ordered moments indicates an overall three-dimensional (3D) magnetic structure of the ordered Ce moments [21]. The reduced entropy of less than 0.5$R \ln 2$ at $T = 8$ K [32] indicates that all Ce moments are subject to the onset of Kondo screening. Since all Ce sites have a similar local environment, it is, however, unlikely that the Ce(2) moments are completely Kondo screened already at $T_N$. Thus, magnetic frustration prevents their long-range order.

We report a detailed thermodynamic study of quantum criticality in single-crystalline CePd$_{1-x}$Ni$_x$Al ($x \leq 0.16$) down to 50 mK for fields $B$ up to 8 T applied along the $c$ axis. Besides heat capacity, $C(T,B)$, we focus on the magnetic Grüneisen parameter $\Gamma_{\text{mag}} = -(dM/dT)_B/C = T^{-1}(dT/dB)_S$ ($M$: magnetization; $S$: entropy). Hence, $\Gamma_{\text{mag}}$ can either be calculated from $T$ dependencies of $M$ and $C$ [33] or obtained directly as adiabatic magnetocaloric effect [34]. At any field-tunable QCP, $\Gamma_{\text{mag}}$ displays a universal divergence and sign change upon tuning the field across the critical field [35,36]. Our thermodynamic investigation of CePd$_{1-x}$Ni$_x$Al reveals 2D field-induced quantum criticality for $x = 0.05$ and $x = 0.1$ and a (zero-field) concentration tuned QCP at $x_c \approx 0.15$ in accordance with previous results on polycrystals [25]. Most
interestingly, we find a positive contribution in $\Gamma_{\text{mag}}(B)$ near 2.5 T, in addition to quantum critical behavior, indicative of a field-induced suppression of magnetic entropy. Since this feature is observed even beyond $x_c$, and thus cannot be related to the QCP, we associate it with the frustrated Ce(2) moments.

Single crystals of CePd$_{1-x}$Ni$_x$Al were grown by the Czochralski method. The Ni content was determined by atomic absorption spectroscopy (AAS). The homogeneity of the Ni content of the samples was checked by energy dispersive x-ray spectroscopy (EDX). The samples were investigated as cast, since annealing causes a structural phase transition [37,38]. The samples were oriented by Laue backscattering x-ray diffraction. The magnetic field was always applied along the crystallographic $c$ axis. The specific heat was measured by the relaxation method in a physical property measurement system at $T > 0.4$ K and by both the relaxation and the quasiadiabatic heat-pulse technique in a dilution refrigerator. The adiabatic magnetocaloric effect was measured using a high-resolution alternating-field technique [34].

Figure 1 shows the $4f$-electron contribution $C_{4f}$ to the heat capacity for all investigated single crystals. $C_{4f}$ was obtained after subtraction of a nuclear contribution $C_{\text{nuc}} = A_0(B)/T^2$ and phonon and conduction-electron contributions approximated by $C(T)$ of the isostructural nonmagnetic reference compound LuPdAl [see Supplemental Material (SM) [39] for details]. A sharp peak due to the partial AF order at $T_K = 2.7$ K for $x = 0$ is suppressed with increasing $x$ to $T_K = 1.9$ K for $x = 0.05$, as determined by the peak temperatures of $C_{4f}/T$. No long-range order is detectable for $x = 0.14$ and 0.16, again in accordance with the phase diagram obtained on polycrystals [25]. However, while a logarithmic increase of $C/T$ upon cooling down to 0.06 K has been found for a polycrystal with $x = 0.144$ [25], the data for $x = 0.14$ clearly display curvature, which may be related to residual order, corroborated by the finite critical field extracted from the field dependence of the specific heat (see below).

In Figs. 2(a)–2(d) the field dependence $(B//c)$ of $C_{4f}/T$ of CePd$_{1-x}$Ni$_x$Al single crystals at the lowest attainable temperature, obtained from $T$-dependent measurements in constant field shown in the SM [39], is analyzed. Assuming a field-induced QCP, $C_{4f}/T = -\gamma_0 \ln (\alpha_x b)$ using $b = (B - B_c)/B_c$ and $C_{4f}/T = \gamma_0 - c \sqrt{B - B_c}$ are predicted by scaling theory for 2D and 3D antiferromagnetic quantum criticality, respectively [35]. Note that in the 3D case, the critical contribution is subtracted from a constant $\gamma_0$ which equals the saturation value. Therefore the fitted $\gamma_0$ must not be smaller than the largest measured $C_{4f}/T$ value. Both equations have three free parameters which allows an unbiased comparison of the quality of the fits. The obtained fit parameters are listed in Table I and the fits are indicated in Figs. 2(a)–2(d). Clearly, for $x = 0.05$ the quality of the 2D fit is much better compared to its 3D counterpart. On the other hand, with increasing $x$ a clear distinction between 2D and 3D behavior becomes more difficult and finally impossible for $x = 0.16$. Fits of the $x = 0.16$ data result in (physically meaningless) negative critical fields, indicating that this sample already lies beyond the concentration-tuned QCP as noted above. Analysis of the field dependence of $C_{4f}$ thus indicates 2D quantum critical fluctuations for $x = 0.05$ while more isotropic (3D) criticality at larger $x$, possibly related to the enhanced disorder in the

![Figure 1](image1.png)

**FIG. 1.** $4f$-electron part of the specific heat plotted as $C_{4f}/T$ vs $T$ (on logarithmic scale) for CePd$_{1-x}$Ni$_x$Al single crystals at zero magnetic field. $C_{4f}$ is obtained after subtracting the nuclear and phonon contributions (see text for details).

![Figure 2](image2.png)

**FIG. 2.** (a)–(d): Field dependence $(B//c)$ of $C_{4f}/T$ of CePd$_{1-x}$Ni$_x$Al for $x = 0.05, 0.10, 0.14$, and 0.16 at the lowest temperatures. The black solid and gray dashed lines represent fits of the data according to the prediction for AF quantum criticality in 2D and 3D, respectively, using the parameters listed in Table I. (e)–(h): Field dependence of the magnetic Grüneisen parameter, $\Gamma_{\text{mag}}$, at $T = 0.2$ and 0.8 K of CePd$_{1-x}$Ni$_x$Al for $x = 0.05, 0.10, 0.14$, and 0.16. The blue solid line in panel (e) indicates a fit of the magnetic Grüneisen parameter according to $\Gamma_{\text{mag}} = G_1(B - B_c)^{-1}$ with $B_c = 3.02 \pm 0.02$ T and $G_1 = 0.81 \pm 0.01$. The black dotted line in panel (e) has been obtained by assuming point inversion symmetry of the fit near the critical field. The arrows in panels (f)–(h) indicate the positions of broad maxima.
TABLE I. Fit parameters for the curves shown in Figs. 2(a)–2(d).
The following functions were fitted [35]: (a) 2D AF quantum criticality according to $C_{4f}/T = -a_1 \ln (a_2 b) + b (B - B_c)/B_c$; (b) 3D AF quantum criticality according to $C_{4f}/T = \gamma_0 - c \sqrt{B - B_c}$.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$B_c$ (T)</th>
<th>$a_1$ (J/mol K$^2$)</th>
<th>$a_2$ (J/mol K$^2$)</th>
<th>$\gamma_0$ (J/mol K$^2$)</th>
<th>$c$ (J/mol K$^2$)</th>
</tr>
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<tbody>
<tr>
<td>$x = 0.05$</td>
<td>3.4</td>
<td>0.43</td>
<td>0.58</td>
<td>1.6</td>
<td>0.81</td>
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<tr>
<td>$x = 0.10$</td>
<td>1.5</td>
<td>0.56</td>
<td>0.18</td>
<td>1.6</td>
<td>0.63</td>
</tr>
<tr>
<td>$x = 0.14$</td>
<td>0.52</td>
<td>0.48</td>
<td>0.052</td>
<td>1.5</td>
<td>0.56</td>
</tr>
<tr>
<td>$x = 0.16$</td>
<td>-1.55</td>
<td>0.48</td>
<td>-0.11</td>
<td>1.4</td>
<td>0.42</td>
</tr>
</tbody>
</table>

Ni-substituted samples, cannot be excluded. Also, it is under debate whether a 2D spin-density wave scenario holds exactly at a QCP or some dimensional crossover always occurs at sufficiently low temperatures [40].

To further explore the nature of quantum criticality in CePd$_{1-x}$Ni$_x$Al, we consider the magnetic Grüneisen parameter $\Gamma_{\text{mag}}$. In the vicinity of any generic field-induced QCP, at low temperatures, a $1/(B - B_c)$ divergence with universal prefactor, as well as a sign change near the critical field $B_c$, arising from the accumulation of entropy, are expected [36]. Figures 2(e)–2(h) show $\Gamma_{\text{mag}}(B)$ at $T = 0.2$ and 0.8 K for our samples. For $x = 0.05$ and $x = 0.1$ a zero crossing is observed at $B = 3.35$ and 1.8 T, which equals almost exactly the respective critical fields obtained from the 2D fits of $C_{4f}(B)$.

On closer inspection, an asymmetry of the zero crossings, i.e., a larger positive and smaller negative wing for $x = 0.05$ and 0.1, can be seen. This hints at the presence of a positive additional contribution to $\Gamma_{\text{mag}}(B)$ peaked at $B = 2.5$ T. Indeed, the field dependence of $\Gamma_{\text{mag}}(B)$ for $x = 0.05$ above the critical field nicely follows the expected $1/(B - B_c)$ dependence for field-induced quantum criticality [cf. the blue line in Fig. 2(e)]. However, the low-field wing of the $\Gamma_{\text{mag}}(B)$ curve deviates from $1/(B - B_c)$ (cf. black dotted line) due to an additional positive contribution to $\Gamma_{\text{mag}}(B)$ between 2 and 3 T, which is of similar size to the broad humps at larger $x$ [cf. Figs. 2(f)–2(h)].

This unexpected contribution, mostly located in the paramagnetic regime above $B_c$, therefore must have a different origin than quantum criticality [36]. For $x = 0.14$ no zero crossing is found. However, the nonmonotonic behavior of $\Gamma_{\text{mag}}$ is compatible with a sign change around $B_c \approx 1$ T, concealed by a positive contribution with a maximum around 2.5 T not captured by quantum criticality. This value of $B_c$ would be in agreement with the kink of $C_{4f}(B)/T$ [cf. Fig. 2(c)]. Finally for $x = 0.16$ only a broad background, again with a maximum around 2.5 T, is observed. This unexpected positive contribution to $\Gamma_{\text{mag}}(B)$ is observed for all samples and peaks independent of $x$ at $B = 2.5$ T. In particular, this contribution occurs independent of whether $B_c$ falls above or below. In fact, it is observed mostly within the paramagnetic regime of quantum criticality and therefore must have a different origin than quantum criticality [36].

Using $\Gamma_{\text{mag}} = -(dM/dT)/C$, the temperature derivative of the magnetization can be calculated from the data. The Maxwell relation $dM/dT = dS/dB$ then allows one to calculate the field dependence of the entropy by integration (SM) [39]. Figure 3 shows the entropy $S(B)$ for all four investigated single crystals of CePd$_{1-x}$Ni$_x$Al. Entropy maxima are found for $x = 0.05$ and 0.1 near the respective critical fields. The colored arrows indicate the positions of the broad maxima in $\Gamma_{\text{mag}}(B)$ (see respective arrows in Fig. 2) and are close to the inflection points of the respective entropy curves. A decrease of magnetic entropy generally points to a field-induced suppression of magnetic correlations.

Finally, we turn to an analysis of quantum criticality in $\Gamma_{\text{mag}}$ for $x = 0.05$. Scaling theory predicts a universal prefactor, $G_c = 0.5$, of the $\Gamma_{\text{mag}}$ divergence for field-induced 3D AF quantum criticality [35]. The value of $G_c = 0.81$ for $x = 0.05$ obtained from the fit in Fig. 2(e) deviates from this prediction. For 2D AF quantum criticality $G_c$ is nonuniversal and thus compatible with our data. Figure 4(a) shows the temperature dependence of $\Gamma_{\text{mag}}$ at various fixed magnetic fields $B \parallel c$, $B = 1$ T, 2 T, 3 T, 3.5 T, 4 T, 5 T, and 6 T.

FIG. 3. 4f contribution to the entropy of CePd$_{1-x}$Ni$_x$Al (see text) vs magnetic field $B$ at $T = 0.2$ K for $B \parallel c$. The colored arrows indicate the positions of anomalies in the magnetic Grüneisen parameter (cf. Fig. 2).

FIG. 4. (a) $T$ dependence of $\Gamma_{\text{mag}}$ for CePd$_{0.9}$Ni$_{0.1}$Al ($x = 0.05$) at various fields along the $c$ axis on semilogarithmic scale. (b) Quantum critical scaling $\Gamma_{\text{mag}}(B - B_c)$ vs $T/(B - B_c)^{1.2}$ using $B_c = 3$ T. The solid and dashed lines represent $\Gamma_{\text{mag}} \propto T^{1/2}$ and $\Gamma_{\text{mag}} = G_c$. 220405-3
while panel (b) shows a scaling plot of $\Gamma_{\text{mag}}(B-B_c)$ vs $T/(B-B_c)^{1/2}$ for data at $B \geq 3.8$ T. The zero crossings in panel (a) arise from the entropy accumulation at the phase boundary [36]. The fact that the 3-T data display such a zero crossing is consistent with the critical field of 3.4 T obtained from the heat capacity analysis. Quantum critical scaling holds for the data beyond the critical field [panel (b)]. Such scaling neglects the logarithmic correction $\log \frac{B_c}{B-0}$ predicted for 2D quantum criticality [35]. Respectively, the best scaling is obtained for a somewhat low critical field of 3 T.

Our thorough thermodynamic investigation of CePd$_{1-x}$Ni$_x$Al single crystals provides evidence for field-induced quantum criticality with the critical field being continuously suppressed towards zero for $x_c \approx 0.15$. Previously, the equivalence of pressure and composition tuning has been demonstrated for CeCu$_{6-x}$Au [41,42] where unconventional quantum criticality with 2D critical fluctuations has been found [43]. Suppressing, on the other hand, magnetic ordering for $x > x_c$ by a magnetic field, yields conventional quantum critical behavior corresponding to 3D fluctuations [44,45]. Our study of the heat capacity of CePd$_{1-x}$Ni$_x$Al reveals 2D quantum criticality for field and concentration tuning at $x \geq 0.05$. This is thus the second example for a material with 3D long-range order, displaying a reduced dimensionality of quantum critical fluctuations. The strong geometrical frustration, leading to disordered moments separating chains of ordered moments, provides a natural explanation of 2D quantum criticality in CePd$_{1-x}$Ni$_x$Al [21,31]. Most interestingly, we have discovered an anomaly in the magnetic Grüneisen parameter for $x \geq 0.1$ that occurs in addition to the generic signatures of field-induced quantum criticality. For $x = 0.05$ the deviation from generic $1/(B-B_c)$ behavior on the low-field side also hints at an additional contribution of similar order of magnitude in the same field range. Thus, this anomaly is independent of the AF QCP due to Ce(1) and Ce(3) moments and consequently ascribed to the frustrated Ce(2) moments. We note that the observed maximum of the magnetic Grüneisen parameter is incompatible with the behavior of a heavy Fermi liquid composed of fully Kondo-screened Ce(2) moments. This indicates that magnetic frustration remains important as the material is concentration tuned across the QCP even beyond $x_c$ as long as magnetic fluctuations lead to the nonequivalence of Ce moments.

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[39] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevB.94.220405 for the determination of the nuclear contribution to the specific heat and the estimation of the field dependence of the magnetic entropy of CePd$_{1-x}$Ni$_x$Al single crystals at 0.2 K.